





```

C      2 = IMPACT
C      3 = TIRACTION FREE SURFACE
C      9 = MIMED WITH COMPLETE CLOSURE RESTRICTION
C     11 = SHEAR FAILED INTERFACE
C     10 = TENSILE FAILED INTERFACE
C
C      IF(KOBR.LT.7 OR KOBR.EQ.8)GO TO 1
C      LOAD TDIAG AND UDIAG
C
C     57 I=1,3
C      UDIAG(I)=SUM(I)*OMEGA/UDIAG(I)
C     57 TDIAG(I)=SUM(I)*OMEGA/HALF
C
C      CALCULATE IRAC, DIS AND PMS
C
C     41 I=1,3
C      PRS(I)=ZERO
C      TRAC(I)=ZERO
C      DIS(I)=ZERO
C      SUMT=ZERO
C      SUMU=ZERO
C     53 J=1,3
C      DCI=DECO(I,J)
C      SUMU=SUMU+DCI*UDIAG(J)
C      SUMT=SUMT+DCI*TDIAG(J)
C      PRS(I)=PRS(I)+DCI*PRS(J)
C      TRAC(I)=TRAC(I)+DCI*TRAC(J)
C     53 DIS(I)=DIS(I)+DCI*(U(M,J)-U(IFP,J))
C
C      CHANGE IJC 3 AND 4 UNKNOWNS.
C
C     IEB=IBC(M,1)
C      IF(IEB.EQ.3)DIS(I)=DIS(I)+SUMT
C      IF(IEB.EQ.4)TRAC(I)=TRAC(I)+SUMU
C      RES(I)=IRAC(I)-PRS(I)
C     41 CONTINUE
C
C      CHECK FOR FAILURE
C
C     IF(KOBR.EQ.9)GO TO 42
C     IF(KOBR.EQ.10)GO TO 47
C     SHSTR=CON-FMI*RES(3)
C     SHEAR=SUMT/RES(1)**2*RES(2)**2
C     IF(KOBR.EQ.11)GO TO 43
C     IF(SHEAR.GT.SHSTR)GO TO 43
C     GO TO 45
C     43 IF((RES(3)).GT.TENSIG)GO TO 44
C
C      SHEAR FAILURE
C
C     IBC(M,1)=3
C     IBC(M,2)=3
C     IBC(M,3)=4
C     DIS(3)=ZLRD
C
C     54 TRAC(1)=(RES(1)*SHSTR/SHEAR)+PRS(1)
C     TRAC(2)=(RES(2)*SHSTR/SHEAR)+PRS(2)
C     KOBR=11
C     TYPE="S",M
C     GO TO 45

```





























RETURN  
END

\*\*\*\*\*

SUMUP IS THE EQUIVALENCE OF LOAD

SUBROUTINE SUMUP(SUM,DIS,TRAC)

JACO

COMBIN MOD(220), IBC(220,3), T(220,3), U(220,3), AREA(220), IFACE(220), INDEX(220,4),  
2 Y(220,3), ALIMP(50), XLIMP(50,3), DLIMP(50,3), LIND(50), LIMP(50,12), LIIMP(50), LMOD(50),  
3 MINE(5,25), IZ(25,25), DX(5,25), DY(25,25), OZT(25,25),  
4 AIC(9,9), EIC(9,9), DK(9,9), ERA(9,9), ZLARG(9,9), XLARG(9,9), VLARG(9,9),  
5 FRINC(3), PRIM(3,3), ALPMA(3,3), IAO(3,3), TT(3,3), INDIR(3,3), DELTRAC(3), ALT(3,3,3),  
6 E1(3), E2(3), M(3), IEC(3), IEM(3), ICOM(3), SYM(3), FAL(3), ORIG(3),  
7 EMOD(10), UNIC(10), FRIC(10), THETA, EEPH, RING, ISYM, RSYM(10), NDIR(8,8), MDEL(10,3),  
8 TRAN42, TRAN21, TRAN2, TRANS, TRANLL, TRANL, TRANUL, TRANUL, FAC, MARI(11), CORR(11,3),  
9 NDIR, NELT, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR, NDIR,  
# ZENO, DHE, TONE, I1, I2, I3, IIRG, HALF, TWD, NITER, OMEGA, DEL, PI, A, E, G, R, H, H, H, H,  
1 E, V, V1, V2, V3, V4, V5, V6, V7, V8, V9, CONS, CK, LB, G, CONN, CFAR, THIN, ESEAN, GSEAN, CPH, PHI,  
2 IUP(2), ICHIAN, LIM, IDISC, IUP, ISTAR, IUP(1152), INEAR, IKITE, NELLE, NIELD, KONE, ISSW(15), ISW(15)

DIMENSION SUM(3), TRAC(3), DIS(3)  
IF(IUP.GT.LIM)CALL IUPFQ(IUPF, IDISC, IUP, ISTAR, 2)  
DO 1 I=1,3  
DO 1 J=1,3  
IUPF=IUP+2  
1 SUM(I)=SUM(I)+IUP\*(IBUP)\*TRAC(J)+IUP\*(IUP-1)\*DIS(J)  
RETURN  
END

\*\*\*\*\*

SUBROUTINE TO FIX SYMMETRY OF A VECTOR

SUBROUTINE SYMFI(SYM,MMULT,VECT,IS)  
DIMENSION SYM(3),MMULT(8,3),VECT(3)  
DO 1 I=1,3  
IF(MMULT(I,1), NE, 1)VECT(I)=SYM(I)-VECT(I)  
1 CONTINUE  
RETURN  
END

\*\*\*\*\*

TRANSFORM A TENSOR FROM GLOBAL TO LOCAL COORDS.

SUBROUTINE IGRM(I,A)  
DIMENSION T(3,3),A(3,3),S(3,3)  
DO 1 K=1,3  
DO 1 L=1,3  
S(K,L)=0  
DO 1 I=1,3  
DO 1 J=1,3  
1 S(K,L)=S(K,L)+A(K,I)\*A(L,J)\*T(I,J)

```
DO 2 I=1,3
DO 2 L=1,3
TOL=SQRT(L)
2 TOR=L=SQRT(L)
RETURN
END
```

```
*****
SUBROUTINE TUDU(XED, XRD, WCR, LCO)
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IACTD
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```
COMMON KOD(ZZ0), IBC(ZZ0,3), T(ZZ0,3), U(ZZ0,3), AREA(ZZ0), IFACE(ZZ0), INDEX(ZZ0,4),
X(ZZ0,3), ALINE(50), XLIMP(50,3), DLINE(50,3), LIMP(50), LIMP(50,12), LFCO(50), LMOD(50),
3 NINE(25,25), HZ(25,25), DX(25,25), DV(25,25), OZ(25,25),
4 AK(9,9), BK(9,9), DK(9,9), EMAT(9,9), ZLARG(9,9), XLARG(9,9), YLARG(9,9),
5 PRIN(3,3), PRIN1(3,3), ALPHAT(3,3), UIC(3,3), T1(3,3), INJUM(3,3), DELTA(3,3), ALT(3,3,3),
6 E1(3), E2(3), M(3), EC(3), ISU(3), XINH(3), KOD(3), SYM(3), FALL(3), ORIG(3),
7 EMOD(10), DEN(10), PR(10), THEA, DEPTH, RHO, ISYM, NESYM(10), NDIR(3,3), NMLL(3,3),
8 TRANA2, TRANA1, IPRAT, TRANS, TRANEL, TRANEL, TRANEL, TRANEL, FAC, WGT(11), EQUAT(11,3),
9 NODE, NELL, NLLNC, NH, NH, NLSX, NLSY, NDIWL, NDIWN, NDIW, ISMEL, JSMAL, NMMON, NSL, IF, NLL, MORDD, NS,
* ZEND, ONE, IONE, I1, I2, I3, THEED, HALF, TWO, NITER, OREGA, DEL, PI, A, B, C, K, ISSB, EW, H, HL,
1 E, V, V1, V2, V3, V4, V5, V6, V7, V8, V9, CONS, CK, CF, G, CONU, CFAN, THIC, ESEAM, GSEAM, CH, PHI,
2 IUP57, ICHIAN, LIM, IDISK, IEOF, ISTAR, IUP(1152), INCAR, IRITE, NELL, NMLL, KODL, ISM(15), ISM(15)
```

```
DIMENSION XED(3), XND(3), DCO(3)
SUBROUTINE TO CALCULATE T1 AND UU COEFFS.
```

```
DRON=ZERO
DO 1 K=1,3
RCOM(K)=(XED(K)-XRD(K))/R
1 DRON=DRON+RCOM(K)*DICO(K)
DO 2 I=1,3
RMLI=RMULT(I,ISYM,I)
RCI=RCOM(I)
RIV3=RCI*V3
RIVZ=RCI*VZ
DCI=DCO(I)
T(I,I)=T(I,I)+DRON*(1+RIV3*RCI)*RMLI
UB(I,I)=UB(I,I)+DGR*(V4+RIVZ*RCI)*RMLI
IF(I,ER,3)H=H+RNM
IP1=IP1+1
DO 2 J=IP1,3
RCJ=RCOM(J)
RMLJ=RMULT(J,ISYM,J)
TF=(DCI*RCJ-DCJ*RCI)*MCK
TFUNC=DRON*RIV3*RCJ
T(I,J)=T(I,J)+TFUNC*TF)*RMLJ
FAC=WCRT(RIVZ*RCJ)
UU(I,J)=UU(I,J)+FAC*RMLJ
2 UU(I,I)=UU(I,I)+FAC*RMLI
RETURN
END
```

\*\*\*\*\*





APPENDIX 4

PARTIAL LISTING OF PROGRAMME MINAPH

\*\*\*\*\*

PARTIAL SOURCE LISTING FOR PROGRAM MINAP

PROGRAM WRITTEN BY S. L. CROUCH (1976)  
PROGRAM MODIFIED BY J. A. C. DIERING (1980/81)

ONLY PARTIALLY RELEVANT TO THE USE OF SUBREGIONS INCLUDED HERE

\*\*\*\*\*

DEFINE LOCATIONS, SIZES, ORIENTATIONS AND BOUNDARY CONDITIONS OF  
DISPLACEMENT DISCONTINUITIES.  
ALSO SET MATERIAL PROPERTIES FOR DIFFERENT SUBREGIONS

IF(ISSW(3), EQ, 0)WRITE(UNIT, 39)  
IF(ISSW(3), EQ, 0)WRITE(UNIT, 40)

NUMRD=0  
NBS=NUMDS  
DO 115 M=1, NUMDS  
READ(FILE)NUM, XB, YE, XE, YE, KODE, TN, TS, THIK  
READ(FILE) ESAMP, GSEAM, COHESN, PHI, MEDI, MEDZ  
IF(KODE, EQ, 9)STOP KODE 9 AFTER STEP 1 ONLY  
IF(KODE, EQ, 13)STOP KODE 13 ILLEGAL  
IF(MEDI, NE, MEDZ)NBS=NBS+1  
XD=(XE-XB)/NUM  
YD=(YE-YB)/NUM  
SW=SWRT(XD\*XD+YD\*YD)  
DO 115 NI=1, NUM  
NUMSDI=NUMSDI+1  
M=NUMSDI  
L(NI)=M  
X(NI)=XB+Q, 5\*(2, \*NI-1, 3)\*XD  
Y(NI)=YB+Q, 5\*(2, \*NI-1, 3)\*YD  
A(NI)=Q, 5\*SW  
SINAL, F(NI)=YD/SW  
COSAL, F(NI)=XD/SW  
KODE 15 REPRESENTS AN INTERFACE  
IF(KODE, EQ, 15)I-DIE=-1  
KOD(M)=KODE  
MEDI(M)=MEDI  
EN(M)=TH  
US(M)=15  
THICK(N)=THIK  
EEL(N)=EELAM  
GEL(N)=GSEAM  
COHES(M)=COHESN  
TANPHI(N)=TAN(PHI\*PI/180)

MEDI AND MEDZ ARE SUBREGION NUMBERS  
IF(MEDI, EQ, MEDZ)GO TO 115  
ISLIP=30  
NUMSDI=NUMSDI+1  
NM=NUMSDI  
L(NM)=NBS

C TYPE 'NM,N',NM,M  
C IFACE CONTAINS THE SECOND ELEMENT IN AN INTERFACE  
C IFACE(N)=NM  
C IFATE(N)=M  
C X(N)=X(N)  
C Y(N)=Y(N)  
C A(N)=A(N)  
C SHALF(N)=SINALF(N)  
C COSALF(N)=COSALF(N)

C KOD = -1 FOR STRESS SPECIFICATION AT AN INTERFACE  
C KOD = -2 FOR DISPLACEMENT SPECIFICATION AT AN INTERFACE

C KOD(N)=-2  
C IF (KOD(N).NE.-1)KOD(N)=KOD(M)  
C MED(N)=MED  
C EN(N)=2\*ERO  
C ES(N)=2\*ERO  
C THICK(N)=THIK  
C EEL(N)=EELAN  
C GEL(N)=GELAN  
C CONES(N)=CONESN  
C TANPHI(N)=TANPHI(N)  
C LIS CONTINUE

\*\*\*\*\*

C COMPUTE INFLUENCE COEFFICIENTS.  
C ROUT BE SURE TO INCLUDE ELEMENTS IN THE CURRENT SUBREGION

C DO 237 I=1,NUMED  
C TYPE 'I',I,ISTAR  
C XI=X(I)  
C VI=Y(I)  
C KODE=KOD(I)  
C IL(I)  
C CAL1=COSALF(I)  
C SAL1=SINALF(I)  
C CAL12=CALI\*SALI  
C CAL13=CALI\*CALI  
C SCAL=SALI\*CALI  
C MEDR=MED(I)  
C CALL MDSSET(E,V,INF,TSYM,NSYM,MEDR)  
C DO 237 J=1,NUMED  
C IF(I.NE.J.AND.ISSW(1).EQ.1)GO TO 237  
C J=L(J)  
C MEDJ=MED(J)  
C TYPE MEDR,MEDJ,NSYM  
C IF(MEDR.NE.MEDJ)GO TO 237

\*\*\*\*\*

C LOAD BUF FOR INTERFACE CODES.  
C BUF IS THE MAIN BUFFER STORAGE ARRAY FOR INFLUENCE COEFFICIENTS  
C IF(KODE.NE.-1)GO TO 226



ENR=0  
ENR=0

EVALUATE SUMS TRN, TMS, ENR, EMS FOR ELEMENTS IN CURRENT SUBREGION

DO 310 J=1, NIMPAD  
IF(MEID(J).NE.MEIR)GO TO 310  
TRN=TRN-EUF(TH)\*ENR(J)+EUF(NB+1)\*MS(J)  
TMS=TMS-EUF(TH)\*ENR(J)+EUF(NB+3)\*MS(J)  
NE=NB+4  
IF(KODE.GT.0)GO TO 312  
ENR=ENR-EUF(TH)\*ENR(J)+EUF(NB+1)\*MS(J)  
EMS=EMS-EUF(TH)\*ENR(J)+EUF(NB+3)\*MS(J)  
NE=NE+4  
312 CONTINUE

LOAD UP EUP FROM DISK FILE

IF(ND.LI.LIND)GO TO 310  
CALL READK(1, ISTAR, IUF, NE, IER)  
IF(IER.NE.1)TYPE "NOELK", IER  
NE=?  
ISTAR=ISTAR+NDLCK  
310 CONTINUE

\*\*\*\*\*

WORK OUT SOR ERROR AND CHECK FOR SLIP ON AN INTERFACE

DIAGN=CM(I)  
DIAGS=CS(I)

INTERFACE ELEMENTS

IF(KODE.NE.-1)GO TO 361  
ITF=ITF+1  
DISN=-ENR  
DISS=-EMS  
SIGMN=-TRN+ENR(I)  
SIGMS=-TMS+ENR(I)  
CNRN(I)=SIGMN+ENR(I)  
DSS(I)=SIGMS+ENR(I)

SWITCH 10 FOR DEPENDENCE ON TOTAL STRESSES.

IF(ISSW(10).NE.1)GO TO 369  
SIGMN=ENR(I)  
SIGMS=DSS(I)

369 CONTINUE  
EN(ITF)=-DISN  
BS(ITF)=-DISS

SEAM ELEMENTS

EN(ITF)={-DISN-SIGMN\*THK/EEL(II)}\*0.5+0.5\*EN(ITF)  
BS(ITF)={-DISS-SIGMS\*THK/GEL(II)}\*0.5+0.5\*BS(ITF)  
IF(N.LI.ISLIP)GO TO 361

```
SIGSF=COSHS(1)+SIGN(1)*TANPHI(1)
IF(QNN(1).LT.ZERO)SIGSF=COSHS(1)
IF(YIELD(1).NE.0)DO 363
IF(AE(COSS(1)).LT.SIGSF)DO 361
363 ESS=SIGSF
IF(QCS(1).LT.ZERO)ESS=-ESS
IYIELD(1)=1
IYIELD(1)=1
ES(1)=ESS+PS(1)
```

```
361 CONTINUE
IF(QDDE.NE.-2)DO 362
ITF=ITFACE(1)
DISN=-TANPHI(1)
DIS=-TANPHI(1)
SIGM=-EMN
SIGS=-EMN
QNN(1)=SIGM+FN(1)
DSS(1)=SIGM+FS(1)
EN(1)=ALPHAN(ITF)+(1-ALPH)*SIGM
ES(ITF)=ALPH*FS(ITF)+(1-ALPH)*SIGM
IF(N.LT.ISLIP)DO 362
IF(YIELD(1).EQ.0)DO 362
ESS=LDES(1)+QNN(1)*TANPHI(1)
IF(QNN(1).LT.ZERO)ESS=COSHS(1)
IF(QSS(1).LT.ZERO)ESS=-ESS
TSS=ESS-PS(1)-SIGM
```

```
C
DIAGS=BDS(1)
362 CONTINUE
```

\*\*\*\*\*

```
C
EVALUATE STRESSES AND DISPLACEMENT CONTRIBUTIONS FOR ELEMENTS IN CURRENT
SUBREGION
```

```
C
DO 850 N=1,NMOS
  NUMP=0
  MEJN=MEJN(N)
  WJ1E(IRITE,62)N,MEJN
  WJ1E(IRITE,63)
  CALL MGETTE,V,INF,ISYM,NSYM,MEJRO
  EVAL=ELMEJN
  VVAL=V(MEJN)
  XD=(XEI(N)-XBI(N))/NUMI(N)
  YD=(YEI(N)-YBI(N))/NUMI(N)
  NF=NUMI(N)
  DO 850 NI=1,NPF
    NUMP=NUMP+1
    XOL=XBI(N)+0.5*(2.*NI-1.)*XD
    YOL=YBI(N)+0.5*(2.*NI-1.)*YD
    SIGX=AXX*YOL+BX
    SIYY=AYY*YOL+BY
    SIGY=AXY*YOL+BY
    PXX=SIGX
    PYY=SIGY
    PXY=SIYX
    LX=0
    LY=0
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EO 630, J=1, N=100  
J=L(1)  
N=JHE(1)  
S=IP ELEMENTS NOT IN CURRENT SUPERREGION  
I=(HEDE, NE, MERR)GO TO 630

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**Author** Diering J A C

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