

DECLARATION

I declare that this review is my own unaided work. It is being submitted for the Degree of Master of Science in engineering to the University of the Witwatersrand, Johannesburg. It has not been submitted before for any degree or examination to any other University.

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.....day ofyear.....

ABSTRACT

The resistance to flow in rivers over the years has been largely an issue of great concern. There have been many suggestions as to how to compute the resistance to flow especially in a composite channel.

This work looks into the factors that contribute to the total flow resistance as a result of the elements that may be present in the body of water.

A critical review of previous work done to determine the total resistance to flow in a composite channel was made in this work and existing formulas were tested to see their reliability.

Ways of predicting resistance coefficients for individual elements were tested using those of James (2012), Meile et al. (2011) and Hirschowitz and James (2009).

This work has been limited to sparse arrangements of obstructions, vegetation and bank irregularities.

After careful observation, recording of data and analysis, formulas were developed for calculating the total resistance to flow for composite channel with permutations of three different elements these formulas were tested and seen to be useful in computing the total resistance to flow in a channel with low flow in a composite channel.

ACKNOWLEDGEMENTS

It has been a long journey to this point. A journey filled with uncertainties and happy times as well. I will not have even started if not for the financial encouragement and moral support from so many people who I shall mention below

First and foremost I offer my sincere gratitude to my supervisor professor C.S. James who supported me throughout my research with finance, patience knowledge and guidance without which I was never going to graduate.

I also thank the school coordinator Dr Ndiritu for his guidance from the beginning.

I also thank the School of Civil and nvironmental Engineering at the University of the Witwatersrand for providing the necessary laboratories and the staff among which Mr Waine Costolopus was a great anchor in terms of technical experience.

Finally I will like to thank my parents for their moral support and prayers throughout my study time.

TABLE OF CONTENTS

1. Introduction.....	1
1.1 Specific research objectives/problem statement.....	1
1.2 Justification for research.....	1
1.3 Scope of the study.....	2
1.4 Layout/structure of the research.....	3
2 Background.....	4
2.1 Intoduction.....	4
2.2 Composite resistance coefficient.....	5
2.3. The combined resistance of bed shear and form roughness.....	9
2.4 Resistance component of a river with low flow.....	12
2.5 Investigations on Emergent Bank Vegetation.....	13
2.6 Effects of bank irregularities to total resistance.....	14
2.6.1 Semi-empirical Drag-Coefficient Model.....	16
3. Methodology.....	18
3.1. Brief overview of conditions tested.....	18
3.2. Description of apparatus.....	18
3.3 Figure schematic of flume.....	19
3.4 Depth of flow.....	28
3.5 Stage one.....	28
3.6 Stage two.....	29
4.1 Experimental investigations of friction factors and Manning's n	30
4.2 Group A (Smooth bed flume).....	30

4.3 Group B (Rough bed flume).....	34
4.4 List of experimental series.....	34
4.4.1 Series 1.2 Smooth bed flume with irregularities.....	35
4.4.2 Series 1.3 smooth bed flume with obstructions.....	36
4.4.3 Series 1.4 Smooth bed flume with Vegetation.....	36
4.4.4 Series 1.5 Smooth bed flume with combination of irregularities and obstructions.....	37
4.4.5 Series 1.6 Smooth bed flume with combination of irregularities and vegetation.....	37
4.4.6 Series 1.7 Smooth bed flume with combination of obstructions and vegetation.....	38
4.4.7 Series 1.8 Smooth bed flume with a combination of irregularities, obstructions and vegetation.....	38
4.4.8 Series 2.1 rough bed flume.....	39
4.4.9 Series 2.2 rough bed flume with irregularities.....	39
4.4.10 Series 2.3 rough bed flume with obstructions.....	40
4.4.11 Series 2.4 Rough bed flume with vegetation.....	40
4.4.12 Series 2.5. Rough bed flume with combination of irregularities and obstructions.....	41
4.4.12 Series 2.5. Rough bed flume with combination of irregularities and obstructions.....	41
4.4.14 Series 2.7. Rough bed flume with combination of obstruction and vegetation.....	42
4.4.15 Series 2.8 Rough bed flume with combination of irregularities, obstruction and Vegetation.....	42
5. Analysis of results.....	44
5.1 Introduction.....	44
5.2 Useful guide to tables.....	45
5.3 Darcy-Weisbach friction factor and Manning's roughness coefficient.....	45
5.3.1. Using Darcy-Weisbach friction factor.....	45

5.3.2 Using Manning's roughness coefficient.....	46
5.3.3 Different Darcy-Weisbach friction factors for rough bed and smooth bed flume.....	46
5.3.4 Different Manning roughness coefficients for rough bed and smooth bed flume.....	46
5.4 Analysis to verify the total resistance coefficient is for both Darcy-Weisbach friction factors and Manning's roughness coefficient.....	61
5.4.1 Using Darcy-Weisbach friction factors.....	63
5.4.2 Using Manning,s roughness coefficient.....	65
5.5 Analysis to check the form roughnesses of elements for different permutations of elements in the flume.....	64
5.5.1 For the rough bed flume using Darcy-Weisbach friction factor.....	65
5.5.2. For the smooth flume using Darcy-Weibach friction factor.....	68
5.5.3 For the rough bed flume using Manning's roughness coefficient.....	71
5.5.4 For the smooth channel.....	75
5.6 Testing of the existing formulas that account for the total resistance in channel.....	77
5.6.1 SCS method.....	77
5.6.2. For the rough bed flume.....	79
5.6.3 For the smooth bed flume.....	81
5.7 HR Wallingford method.....	83
5.7.1 For the rough bed flume.....	85
5.7.2 For the smooth bed flume.....	86
5.8 Empirical formulas.....	89
5.81. For the rough bed flume.....	91
5.8.2 For the smooth bed flume.....	93

5.9 Computing Resistance Coefficient by prediction.....	95
5.9.1. Bank irregularities calculation (Semi-empirical Drag-Coefficient Model).....	95
5.9.2 Rough bed flume.....	95
5.9.3 Smooth bed flume with irregularities.....	99
5.9.4 Analysis of resistance due to Obstacles.....	102
5.9.5. Rough bed flume with obstructions.....	102
5.9.6 Smooth bed flume with obstructions.....	107
5.9.7 Vegetation formulation.....	110
5.9.8 Rough bed flume with vegetation.....	111
5.9.9 Smooth bed flume with vegetation.....	112
5.10 Retesting of the formulas that account for the total resistance in a channel using the predicted resistance results.....	114
5. 10.1 SCS method.....	114
5.10.2 SCS method retested with the predicted resistance result for rough bed flume.....	115
5.10.3 SCS method retested with the predicted resistance result for smooth bed flume.....	116
5.10.4 HR Wallingford's method retested with the predicted resistance results for rough Bed flume.....	117
5.10.5 Empirical formula retested with predicted total resistance results.....	121
5.11 Discussion.....	125
6. Conclusion and recommendation	128
References	130
Appendix	138

List of figures

Figure 2.4.1(a) Plan view of the test flume with (b) the definition of the parameters of the macrorough configurations L_b , L_c , and ΔB	13
Figure 2.4.2.Observed basic flow types as a function of the aspect ratio of the large-scale depressions: (a) reattachment flow type; (b) normal recirculating flow type; and (c) square-grooved flow type; grey zones indicate the range of performed experiments.....	13
Figure 3.3.1.Smooth bed flume.....	20
Figure 3.3.2. Smooth bed flume with bank irregularities.....	20
Figure 3.3.3. Smooth bed flume with obstructions.....	21
Figure 3.3.4. Smooth bed flume with vegetation	21
Figure 3.3.5. Smooth bed flume with irregularities obstructions.....	21
Figure 3.3.6. Smooth bed flume with irregularities, obstruction and vegetation.....	22
Figure 3.3.7. Smooth bed flume with irregularities and vegetation.....	22
Figure 3.3.8.Smooth bed flume with vegetation and obstructions.....	23
Figure 3.4.1.Rough bed flume.....	23
Figure 3.4.2. Rough bed flume with bank irregularities.....	24
Figure 3.4.3. Rough bed flume with obstructions.....	24
Figure 3.4.4. Rough bed flume with vegetation	25
Figure 3.4.5. Rough bed flume with irregularities obstructions.....	25
Figure 3.4.6. Rough bed flume with irregularities, obstruction and vegetation.....	26
Figure 3.4.7. Rough bed flume with irregularities and vegetation.....	26

Figure 3.4.8. Rough bed flume with vegetation and obstructions.....	27
Figure 4.1 Smooth flume without any element	31
Figure 4.2 Stage-discharge graph for smooth bed flume.....	32
Figure A1 Smooth bed flume with irregularities.....	138
Figure A2 Stage-discharge graph for smooth bed flume with irregularities.....	139
Figure A3 Smooth bed flume with obstructions.....	140
Figure A4 Stage-discharge graph for smooth bed flume with obstructions	141
Figure A5 Smooth bed flume with vegetation.....	142
Figure A6 Stage-discharge graph for smooth bed flume with vegetation	143
Figure A7 Smooth bed flume with irregularities and obstructions	144
Figure A8 Stage-discharge graph for smooth bed flume with irregularities and obstructions	145
Figure A9 Smooth bed flume with irregularities and vegetation.....	146
Figure A10 Stage-discharge graph for smooth bed flume with irregularities and obstructions.....	147
Figure A11 Smooth bed flume with combination of obstructions and vegetation	148
Figure A12 Stage-discharge graph for smooth bed flume with vegetation and obstructions.....	149
Figure A13 Smooth bed flume with a combination of irregularities, obstructions and vegetation	150
Figure A14 Stage-discharge graph for smooth bed flume with vegetation, irregularities and obstructions	151

Figure A15 Rough bed flume with only water and no elements.....	153
Figure A16 Stage-discharge graph for rough bed flume	153
Figure A17 Rough bed flume with irregularities	154
Figure A18 Stage-discharge graph for rough bed flume with irregularities	156
Figure A19 Rough bed flume with obstructions	156
Figure A20 Stage-discharge graph for rough bed flume with obstructions	158
Figure A21 Rough bed flume with vegetation	158
Figure A22 Stage-discharge graph for smooth bed flume with vegetation.....	160
Figure A23 Rough bed flume irregularities and obstructions.....	160
Figure A24 Stage-discharge graph for smooth bed flume with irregularities and obstructions	161
Figure A25 Rough bed flume with irregularities and vegetation.....	161
Figure A26 Stage-discharge graph for rough bed flume with irregularities and vegetation.....	163
Figure A27 Rough bed flume with obstruction and vegetation.....	155
Figure 28A Stage -discharge graph for smooth bed flume with vegetation and obstructions.....	166
Figure A29 Rough bed flume with a combination of irregularities, obstruction and vegetation	166
Figure A30 Stage-discharge graph for rough bed flume with vegetation, irregularities and obstructions.....	168

Figure 5.1. Graph showing the correlation between computed Manning's n values using the empirical formulas against the Manning's n values computed from the actual measured discharges and depths for the rough bed flume.....92

Figure 5.2 Graph showing the correlation between computed Manning's n values using the empirical formulas against the Manning's n values computed from the actual measured discharges and depths for the smooth bed flume.....94

Figure 5.3. Graph showing the correlation between predicted and observed Manning's n values for the rough bed flume after using the empirical formulas for the prediction123

Figure 5.4 Graph showing the correlation between predicted and observed Manning's n values for the smooth bed flume after using the empirical formulas for the prediction.....125

List of tables

Table 4.1 Summary of measured depths on the calibrated stilling pots at the given discharge for smooth flume bed.....	31
Table 4.2 Summary of the normalised depth in metres against the stilling pots for smooth flume bed.....	32
Table 4.3 Summary of measured depths, resistance coefficients (f and n) at given discharges for the smooth flume bed.	33
Table 4.4. Summary of measured depths, resistance coefficients (f and n) at given discharges for the smooth bed flume with irregularities.....	35
Table 4.5. Summary of measured depths, resistance coefficients (f and n) at given discharges for the smooth bed flume with obstructions.....	36
Table 4.6. Summary of measured depths, resistance coefficients (f and n) at given discharges for the smooth bed flume with vegetation.....	36
Table 4.7. Summary of measured depths, resistance coefficients f and n) at given discharges for the smooth bed flume with irregularities and obstructions.....	37
Table 4.8. Summary of measured depths, resistance coefficients (f and n) at given discharges for the smooth bed flume with irregularities and vegetation.....	37
Table 4.9. Summary of measured depths, resistance coefficients (f and n) at given discharges for the smooth bed flume with vegetation and obstructions.....	38
Table 4.10. Summary of measured depths, resistance coefficients (f and n) at given discharges for the smooth bed flume with irregularities, obstructions and vegetation.....	38

4.11. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume only.....	39
Table 4.12. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume with irregularities.....	39
Table 4.13. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume with obstructions.....	40
Table 4.14. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume with vegetation.....	40
Table 4.15. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume with obstructions and irregularities.....	41
Table 4.16. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume with vegetation and irregularities.....	41
Table 4.17. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume with obstructions and vegetation.....	42
Table 4.18. Summary of measured depths, resistance coefficients (f and n) at given discharges for the rough bed flume with obstructions, irregularities and vegetation.....	42
Table 5.1 Summary of Darcy-Weisbach friction factors for the individual elements (obstructions, vegetation & irregularities) and also their permutations in the rough bed flume.....	48
Table 5.2. Summary of total friction factors and friction factors due to form roughness	

(f_{form}) for the individual elements (obstructions, vegetation & irregularities) and also their permutations in the smooth bed flume.....	49
---	----

Table 5.3. Summary showing the difference in form roughness between smooth bed flume and rough bed flume when obstructions, irregularities and vegetation are permuted in the flume using Darcy Weisbach friction factor.....	50
---	----

Table 5.4 Summaries of total Manning's roughness coefficient and Manning's roughness coefficient due to form roughness (n_{form}) for the individual elements (obstructions, vegetation & irregularities) and also their permutations in the rough bed flume.....	53
---	----

Table 5.5 Summary of total Manning's roughness coefficient and Manning's roughness coefficient due to form roughness (n_{form}) for the individual elements (obstructions, vegetation & irregularities) and also their permutations in the smooth bed flume.....	54
--	----

Table 5.6 Summary showing the difference in Manning's form roughness coefficient between smooth bed flume and rough bed flume when obstructions, irregularities and vegetation are permuted in the flume.....	55
---	----

Table 5.7 Summary showing the computed Darcy-Weisbach f values against the Darcy-Weisbach f values (using observed discharge and depth) for the rough bed flume.....	60
--	----

Table 5.7 Summary showing the computed Darcy-Weisbach f values against the Darcy-Weisbach f values (using observed discharge and depth) for the smooth bed flume.....	61
---	----

Table 5.9 Summary showing the computed Manning's n values against the computed Manning's n values (using observed discharge and depth) for the rough bed flume.....	62
---	----

Table 5.10 Summary showing the computed Manning's n values against the computed Manning's n values (using observed discharge and depth) for the smooth bed flume.....	63
---	----

Table 5.11 Summary showing the different form roughness' (f_{form}) for the rough bed with obstructions obtained from all the different permutations of the elements in the rough bed flume using Darcy Weisbach friction factor.....	65
Table 5.12 Summary showing the different form roughness' (f_{form}) for the rough bed with vegetation obtained from all the different permutations of the elements in the rough bed flume using Darcy Weisbach friction factor.....	66
Table 5.13 Summary showing the different form roughness' (f_{form}) for the rough bed with irregularities obtained from all the different permutations of the elements in the rough bed flume using Darcy Weisbach friction factor.....	67
Table 5.14 Summary showing the different form roughness' (f_{form}) for the smooth bed with obstructions obtained from all the different permutations of the elements in the smooth bed flume using Darcy Weisbach friction factor.....	68
Table 5.15 Summary showing the different form roughness' (f_{form}) for the smooth bed with vegetation obtained from all the different permutations of the elements in the smooth bed flume using Darcy Weisbach friction factor.....	69
Table 5.16 Summary showing the different form roughness' (f_{form}) for the smooth bed with irregularities obtained from all the different permutations of the elements in the smooth bed flume using Darcy Weisbach friction factor.....	70
Table 5.17 Summary showing the different form roughness' (f_{form}) for the smooth bed with obstructions obtained from all the different permutations of the elements in the smooth bed flume using Manning's roughness coefficient.....	71

Table 5.18 Summary showing the different form roughness' (f_{form}) for the rough bed with vegetation obtained from all the different permutations of the elements in the rough bed flume using Manning's roughness coefficient.....	72
Table 5.19 Summary showing the different form roughness' (f_{form}) for the rough bed with irregularities obtained from all the different permutations of the elements in the rough bed flume using Manning's roughness coefficient.....	73
Table 5.20 Summary showing the different form roughness' (f_{form}) for the smooth bed with obstructions obtained from all the different permutations of the elements in the smooth bed flume using Manning's roughness coefficient.....	74
Table 5.21 Summary showing the different form roughness' (f_{form}) for the smooth bed with vegetation obtained from all the different permutations of the elements in the smooth bed flume using Manning's roughness coefficient.....	75
Table 5.22 Summary showing the different form roughness' (f_{form}) for the smooth bed with irregularities obtained from all the different permutations of the elements in the smooth bed flume using Manning's roughness coefficient.....	76
Table 5.23 Summary showing the total Manning's n values computed from the measured discharges and depths for the rough bed flume as seen in the tables of the appendix.....	78
Table 5.24 Comparison of Manning's n values predicted by SCS method and experimental values for rough bed case	79
Table 5.25 Summary showing the total Manning's n values computed from the measured discharges and depths for the smooth bed flume as seen in the tables of the appendix.....	80

Table 5.26 Comparison of Manning's n values predicted by SCS method and experimental values for smooth bed case	81
Table 5.27 Summary of computed form resistances for the permutations of the three elements (obstructions, vegetation and irregularities for the smooth bed flume using Manning's roughness coefficient.....	85
Table 5.28 Summary showing the testing of the HR Wallingford's method for both predicted Manning's n values and the % error due to their differences for the rough bed flume.....	86
Table 5.29 Summary of computed form resistances for the permutations of the three elements (obstructions, vegetation and irregularities for the smooth bed flume using Manning's roughness coefficient.....	87
Table 5.30 Summary showing the testing of the HR Wallingford's method for both predicted Manning's n values and the % error due to their differences for the smooth bed flume.....	88
Table 5.31 Summary showing the testing of the empirical method for both predicted Manning's n values and the experimentally computed (observed) Manning's n values for the rough bed flume.....	91
Table 5.32 Summary showing the testing of the empirical method for both predicted Manning's n values and the experimentally computed (observed) Manning's n values for the smooth bed flume.....	93
Table 5.33. Summary of calculations for f_{bed} for rough bed flume with bank irregularities.....	96
Table 5.34 Summary of calculations for f_{Mr} and f_{total} for rough bed with bank irregularities...	98

Table 5.35 Summary of calculations for f_{bed} in smooth bed with bank irregularities.....	99
Table 5.36 Summary of calculations for f_{Mr} and f_{total} in smooth bed with bank Irregularities.....	101
Table 5.37 Summary of calculations (rough bed channel with no elements except water) of f , n , R , R_e K_s	104
Table 5.39 Summary of calculations for f_{bed} in the rough channel with obstructions.....	105
Table 5.40 Summary of calculations for f_{bed} in the smooth channel with obstructions.....	107
Table 5.41 Summary of calculations for f_{form} and f_{total} with obstructions in the smooth channel.....	109
Table 5.42 Summary of calculations of $V_{inf}^2 \left(\frac{m}{s} \right)$, f_v and f_{total} for the rough bed flume with vegetation.....	111
Table 5.43 Summary of calculations of $V_{inf}^2 \left(\frac{m}{s} \right)$, f_v and f_{total} for the smooth bed flume with vegetation.....	113
Table 5.44 Summary of predicted values of Manning's resistance for rough channel for SCS method.....	116
Table 5.45 Summary of predicted values of Manning's resistance for smooth channel for SCS method.....	117
Table 5.46 Summary of predicted values of Manning's resistance n for rough bed flume using HR Wallingford's method	119

Table 5.47 Summary of predicted values of Manning's resistance n for smooth bed flume using HR Wallingford's method	120
Table 5.48 Summary of predicted and observed values of Manning's resistance n for rough bed flume using empirical formulas.....	122
Table 5.49 Summary of predicted & observed values of Manning's resistance n for smooth bed flume using empirical formulas.....	124
Table A1. Summary of measured depths on the calibrated stilling pots at the given discharge for the smooth flume bed with irregularities.....	138
Table A2. Summary of the normalised depth in metres against the stilling pots for smooth flume with irregularities bed after applying procedure for table 4.2.....	139
Table A3 Summary of measured depths on the calibrated stilling pots at the given discharge for the smooth channel with obstruction.....	140
Table A4 Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	141
Table A5. Summary of measured depths on the calibrated stilling pots at the given discharge for the smooth channel with vegetation.....	142
Table A6. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	143
Table A7 Summary of measured depths on the calibrated stilling pots at the given discharge for the smooth channel with irregularities and obstructions.....	144
Table A8. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	145
Table A9. Summary of measured depths on the calibrated stilling pots at the given discharge for the smooth channel with irregularities and vegetation.	146

Table A10. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	147
Table A11. Summary of measured depths on the calibrated stilling pots at the given discharge for the smooth channel with obstruction and vegetation.....	148
Table A12. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	149
Table A13. Summary of measured depths on the calibrated stilling pots at the given discharge for the smooth channel with obstruction and irregularities and vegetation.....	150
Table A14. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	151
Table A15. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough bed flume only.....	152
Table A16. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	152
Table A17. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough channel with irregularities.....	154
Table A18. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	155
Table A19. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough channel with obstructions.....	157
Table A20. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	157
Table A21. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough bed flume with vegetation.....	159

Table A23. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough channel with irregularities and obstructions.....	161
Table A24. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	161
Table A25. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough channel with irregularities and vegetation.....	163
Table A26. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	163
Table A27. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough channel with obstructions and vegetation.....	165
Table A28. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	165
Table A29. Summary of measured depths on the calibrated stilling pots at the given discharge for the rough channel with obstructions, vegetation and irregularities.....	167
Table A30. Summary of the normalised depth in metres against the stilling pots for smooth flume with obstructions bed after applying procedure for table 4.2.....	167

Notation

A_{bf} = bed area subjected to surface shear [m^2]

A_p = projected area of elements [m^2]

a = Constant in friction factor relationship [-]

b = Constant in in friction factor relationship [-]

C_D = drag coefficient [-]

C = constant in friction factor relationship [-]

D = flow depth [m]

d = cylinder diameter [m]

F = downslope weight component of water [N]

F' = surface shear resisting force [N]

F'' = form drag [N]

f = friction factor [-]

f' = friction factor associated with bed shear [-]

f'' = friction factor associated with form drag [-]

f_b = friction factor for bed [-]

g = gravitational acceleration [m/s^2]

k_s = Nikuradse grain roughness [m]

n = Manning resistance coefficient [$\text{s/m}^{1/3}$]

n' = Manning resistance coefficient associated with bed shear [$\text{s/m}^{1/3}$]

n'' = Manning resistance coefficient associated with form drag [$\text{s/m}^{1/3}$]

N = number of elements per unit area of bed [-]

R = hydraulic radius [m]

R_e = flow Reynolds number [-]

R_d = element Reynolds number [-]

S = channel slope [-]

u^* = shear velocity [m/s]

V = average velocity [m/s]

v = volume of water above bed [m^3]

W = channel width [m]

α = factor to account for area of separation zone [-]

δ = kinematic viscosity of water [m²/s]

ρ = water density [kg/m³]

τ_o = boundary shear stress [N/m²]

irr = irregularities

$obst$ = obstructions

veg =Vegetation

f_{to} = a constant to be equal to zero by Hirschowitz and James (2009) for W/D greater than about 5 and between 0.06 and 0.1 for narrow channels.

f_m = total friction factor for bed with irregularities.

f_{Mr} = resistance due to micro-roughness of the sidewalls of the elements causing the irregularities

f_{prism} = the resistance due to the bed.

l = the ratio of water volume to projected plant area,

a_x = longitudinal stem spacing

a_y = lateral stem spacing,

d_p = the stem diameter

V_{inf} = the depth-averaged velocity in the channel as unaffected by vegetation

V_{veg} = the depth-averaged velocity within the vegetated zone,

h_t = the flow depth