

# A Numerical Study of Thermoelectric Properties of Layered Platinum Chalcogenides and Oxide

## Hamza Adam Haroun Mohammed

1695895@students.wits.ac.za

Supervisor Professor Daniel P. Joubert daniel.joubert2@wits.ac.za Co-Supervisor Doctor G.M. Dongho-Nguimdo moise@aims.ac.za

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# Declaration

I declare that the thesis hereby submitted to the University of Witwatersrand for the degree of Doctor of Philosophy has not previously been submitted by me for a degree at this or any other university, that is my own investigations, and that all material contained herein has been duly acknowledged.

Hamza Adam Haroun Mphammed,

16 March 2020

# Abstract

The research reported in this thesis was motivated by the pressing need for novel materials for thermoelectric and photovoltaic applications. We numerically explored properties of Platinum dichalcogenides dioxide to examine if these compounds have potential as active components in thermoelectric and photovoltaic devices. Transition metal dichalcogenides (TMDs), in layered structures, have diverse properties that complement and potentially extend beyond promising properties of graphene, the prototypical layered material. Structural, stabilities (mechanical and dynamical), electronic, optical and thermoelectric properties of the bulk, bilayer and monolayer trigonal platinum dioxide and dichalcogenides  $PtX_2$ , (X = O, S, Se and Te) were investigated based on density functional theory (DFT) and many-body perturbation theory (MBPT) as implemented in the Vienna *ab-initio* simulation package. The structural properties of the bulk, bilayer and monolayer  $PtX_2$  (such as optimized lattice parameters, cohesive and formation energies) were extracted from relaxed structures. Elastic coefficients and phonon dispersion studies showed that the relaxed structures are mechanically and dynamically stable. Investigation of the electronic band structure and densities of states of the bulk, bilayer and monolayer  $PtX_2$  show that, at the DFT level of approximation, all the compounds are indirect band gap semiconductors apart from bulk  $PtO_2$ ,  $PtS_2$ ,  $PtS_2$  and  $PtTe_2$  which are semi-metals.

To calculate optical properties, we implemented the Bethe-Salpeter equation (BSE) calculations on top of non-self-consistent  $G_0W_0$  calculations to determine the dielectric matrix. The obtained results for absorbance in the visible light range for single layers in bulk, bilayer and a monolayer PtX<sub>2</sub>, are from 0.9 - 35.27% for in-plane absorbance. which is higher than 2.3% for graphene and 5-10% for layered MoS<sub>2</sub>, MoSe<sub>2</sub> and WS<sub>2</sub> of

similar thickness. The BSE optical gaps are in the range 0.37 to 2.75 eV for monolayer and bilayer  $PtX_2$ , while there is no gap bulk  $PtO_2$ ,  $PtS_2$ ,  $PtSe_2$  and  $PtTe_2$ . Monolayer and bilayer  $PtX_2$  may have potential for application in tandem solar cell applications.

Lattice and electronic transport coefficients were obtained within the relaxation-time approximation to the Boltzmann transport equations as implemented in PHONO3PY package and BoltzTraP2 packages. We calculated the lattice thermal conductivity for PtX<sub>2</sub> structures per layer, for ease of comparison between few layer and bulk systems. The obtained results are in range from  $24.61 \times 10^{-8}$  to  $0.07 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 300 K for bulk PtO<sub>2</sub> to monolayer PtTe<sub>2</sub>, respectively. The out-of-plane coefficients of bilayer and monolayer are zero. The obtained values of the figure of merit (ZT) were in a range from 0.04 to 0.74, with the highest ZT values achieved by bilayer and monolayer PtO<sub>2</sub> (0.62 and 0.74), while the lowest ZT value was obtained by bulk PtS<sub>2</sub> of 0.04. Also, we observed the increase of figure of merit from bulk to monolayer which was expected due to their low lattice thermal conductivity. Most, the highest values of the calculated ZT were dominated by the electron charge carriers. The investigation suggests that of the compounds explored, n-type monolayer PtO<sub>2</sub> has the most promise for thermoelectric applications.

# **Publications**

- Hamza AH Mohammed, GM Dongho-Nguimdo and Daniel P Joubert. Structural stability, electronic, optical and lattice thermal conductivity properties of bulk and monolayer PtS<sub>2</sub>. *Materials Today Communications*, 21:100661, 2019. Ref. [1].
- Hamza AH Mohammed, GM Dongho-Nguimdo and Daniel P Joubert. Lattice thermal conductivity of bulk PtTe<sub>2</sub> and PtSe<sub>2</sub>. In South African Institute of Physics 62<sup>nd</sup> Annual Conference (SAIP 2018), edited by Prof. Japie Engelbrecht (SU/2018), pp. 50 - 55. ISBN: 978-0-620-85406-1, Dec 2018. Available online at http://events.saip.org.za/getFile.py/access?resId=53&materialId= 3&confId=100.
- 3. Hamza AH Mohammed, GM Dongho-Nguimdo and Daniel P Joubert. Structural stability and electronic properties of bulk, bilayer and monolayer  $PtX_2$  (X = Se and Te). Accepted for publication
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# Presentations

- Lattice thermal conductivity of bulk PtTe<sub>2</sub> and PtSe<sub>2</sub> poster presentation. 63<sup>rd</sup> Annual Conference of the South African Institute of physics (SAIP2018), University of Free state, Bloemfontein, South Africa.
- 2. Structural stability and electronic properties of bulk, bilayer and monolayer  $PtX_2$ (X = Se and Te) poster presentation.  $64^{th}$  Annual Conference of the South African Institute of physics (SAIP2019), University of Venda, polokwane, South Africa.

# DEDICATION

This thesis is dedicated to my beloved parents.

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# Introduction

# 1.1 Motivation and Overview

The necessity for alternative and renewable energy technologies to decrease our dependence on fossil fuels has lead to different directions of research, including hightemperature energy harvesting via the direct recovery of waste heat and its conversion into useful electrical energy using thermoelectric devices. During the past few decades research on thermoelectric materials has been intensified. Such interest has been driven by the need for more efficient use of energy and a need for thermoelectric materials that can be used for converting heat into electricity and electronic refrigeration [2, 3]. The investigation of a different system of potential thermoelectric materials has been studied by various research groups. Dresselhaus M S et al., are investigate the thermoelectric properties of some low-dimensional materials, and they found their figure of merit are in range from  $\sim 0.08$  to  $\sim 0.75$  at temperature range from 300 to 1400 K [4]. The figure of merit for the some selected materials were in range from  $\sim 0.95$  at 400 K for Bi<sub>2</sub>Te<sub>3</sub> up to 1.7 at 800 K for  $ZN_4Sb_3$  [5]. Nanostructuring approach are used to study the enhancement of thermoelectric figure of merit of bulk materials, their obtained were in range from 0.25 to 1.4 at temperature range from 0 to 1000 K [6]. The main two research efforts are focused on the materials are maximization of the power factor PF and minimization of the thermal conductivity, (especially lattice thermal conductivity). The proposed application of thermoelectric materials increased the activity in this field by optimizing greater performance and higher temperature thermoelectric materials

compared with the current materials. Recently, the thermoelectric solar hybrid system has been investigated to improve absorption in the infrared zone in the solar spectrum and for thermoelectric solar power generation [7]. Nowadays, of more importance is the higher performance development of thermoelectric materials. Novel applications of thermoelectrics such as enhanced performance of optoelectronics coupled with solid-state thermoelectric cooling, power provision for deep-space probes via radioisotope thermoelectric generators and biothermal batteries to power heart pacemakers. Recently, thermoelectric generators have been installed in automobiles to capture waste heat from the exhaust system and to transform it into useful electrical energy for automotive electrical systems and for increased fuel efficiency for use in the next-generation vehicles [8]. Thermoelectric refrigeration is an environmentally green method of small-scale such as infrared detectors, optoelectronics and localized cooling in computers, and many other applications [9].

## **1.2** Photovoltaic

Photovoltaic technology is one of the ways to generate electricity from the sun energy [10]. In a semiconductor, the PN-junction is incorporated of practically for all photovoltaic devices to develop the photovoltage. The solar cell system operation is based on photovoltaic effects, reported by Becquerel in 1839 [10, 11]. To produce direct voltage and current, the PV cell should be connected in series, and this direct voltage can be converted to alternative current power, when required. Many publications have described its operating principles [12, 13]. However, the efficiency depends on the energy absorbed which also depends on the band gap, taking into account the nature of transition as a direct and an indirect band gap [14].

# **1.3** Thermoelectric Phenomena

One of the most right challenges of our time is to find renewable alternative energy sources which are environmentally friendly. The technology of thermoelectric is considered a kind of energy conversion technology. The description of the conversion of thermal energy to electrical energy, or vice-versa is a phenomenon that is called the thermoelectric effect [15]. There are three important transport effects, namely the Seebeck effect, the Peltier effect and the Thomson effect. Details about those effects are summarised in section (1.3.1). Thermoelectric performance of materials determine the energy efficiency of thermoelectric devices. The figure of merit (ZT) is a quantity used as a gauge for novel thermoelectric materials. Bismuth telluride-based alloys have long be considered as the best thermometric materials because of their high ZT, which is slightly above unity. Through the last decade, the search for promising bulk thermoelectric materials has intensified. Nowadays, new material systems are being developed to achieve ZT well above unity. This also forms the aims of our study.

#### **1.3.1** Thermoelectric effects

There are three important thermoelectric effects are namely, Seebeck, Peltier and Thomson effect. The Seebeck effect describes the voltage gradient in a conductor subjected to a gradient of temperature. Which was discovered by Seebeck, when a compass needle deflected when placed in the vicinity of a closed-loop formed of two dissimilar metals with a temperature difference between the junctions. This observation provides direct evidence that a current flows through the closed circuit driven by the temperature difference. On the other hand, the Peltier effect describes the conversion of electrical current into heat transfer, which is a reverse technique of the Seebeck [15]. The Peltier effect is the underlying foundation for thermoelectric refrigeration. When an electric current passes through two dissimilar materials such as metals or semiconductors that are connected at two junctions, heat will be absorbed in one junction and liberated at the other junction. As a result, one junction cools off while the other heats up, depending on the direction of the current [16]. Figure 1.1 show Seebeck and Peltier effects. The Thomson effect is the rate of heat absorbed or emitted when a conductor is subjected to a temperature difference along its length. There is tow type of Thomson effect the positive and negative effect, that depends on the direction of the current movement, from the high to a low potential or vice versa [17]. In this research, we focused on how heat energy is converted to the electricity, which depends on charge carriers moving through a gradient of temperature, which is called the Seebeck effect.



Figure 1.1: Seebeck and Peltier effects.

#### 1.3.2 Thermoelectric figure of merit

The figure of merit concept is used to describe the efficiency of a thermoelectric material. It is expressed as;

$$ZT = \frac{S^2 \sigma T}{\kappa} = \frac{S^2 \sigma T}{\kappa_e + \kappa_L},\tag{1.3.1}$$

where S,  $\sigma$ , T and  $\kappa$  are the Seebeck coefficient, electrical conductivity, temperature in Kelvin scale and thermal conductivity, respectively.  $\kappa_e$  and  $\kappa_L$  are electronic and phononic contributions, which is a combination of  $\kappa$  ( $\kappa = \kappa_e + \kappa_L$ ). The stander way to figure out good thermoelectric material is to determine the figure of merit. Thus, the efficiency of energy conversion has a direct relation to the figure of merit [18]. Hence, a good thermometric material should have a large Seebeck coefficient for increasing the conversion of heat to electricity, a high electrical conductivity to reduce the Joule effect and a low thermal conductivity to make a large gradient of temperature [15].

#### **1.3.3** Optimization of thermoelectric materials

Good thermoelectric materials should have a low thermal conductivity and a large power factor. Usually, semiconductors have a large (S) and low  $(\sigma)$ , compared to metals. Doping a material might increase its electrical conductivity. But at the same time, the heavy doping can reduce the Seebeck coefficient due to shifting of the Fermi level close to band edge or into the band. Then, it is necessary to find a doping level where the power factor is optimized. There are many ways to reduce the thermal conductivity, for example, adding a short-range disorder into the crystal structure, or substitution by isoelectronic elements, which may affect the electrical conductivity. Unfortunately, to increase the figure of merit through reducing thermal conductivity is considered as a main challenge [19, 20].

# 1.4 Transition-metal dichalcogenides (TMDS)

The word chalcogen comes from the Greek word "chalcos" which is means ore or metal and "genes" which means formation, so ore former is considered the general mean of the term chalcogen [21]. The chalcogenide elements belong to group sixteen of the periodic table. This group consists of oxygen, sulphur, selenium, tellurium and polonium, however, oxygen is usually excluded from this group because it has different chemical behavior compare to others. For example, the wide contribution of band gaps to various electrical and optical properties. The chalcogenide compounds were discovered recently compared to oxygen compound, nevertheless, it is not considered from the chalcogenide compounds. The minerals pyrite (FeS<sub>2</sub>) and calaverite (AuTe<sub>2</sub>) are the most common form chalcogenide compounds. Generally, chalcogenides can exist over a wide range of compounds, like glass-forming [22]. Transition metal dichalcogenides and dioxide have a general form of MX<sub>2</sub>, where M represents the transition metal and X an atom of the oxygen family (X = O, S, Se and Te). Some TMDs are layered compounds in a sandwiched form (X-M-X), held together by covalent bonds, as shown in Figure 1.2.

The van der Waals forces are stacking the layers together. This phenomenon of bonding is helpful to create the two dimensional structure [23, 24, 25, 26]. However, these compounds have two important differences from the iso-structural group IVb, Vb and VIb TMDs. First, a large number of electrons in *d*-shell in the group VIIIc metal compounds compared with other groups of metal. The small value of the ratio c/ais considered second difference when it compares to the ideal value of 1.633 [27]. The group VIIIc layered TMDs have electronic structure and related behavior quite different from the other groups of those the TMDs. Previous calculations on the group VIIIc were done on PdTe<sub>2</sub> compound, using both the KKR (Korringa-Kohn-Rostoker) and LMTO (linear muffin-tin orbital) methods. Substituting chalcogen atoms, from S to Te shows the variation on the electronic structure [26]. Most works have been focused on group VI TMDs, MoS<sub>2</sub> and WS<sub>2</sub>, while other groups remain in uncharted waters [28]. Their electronic structure properties studies have been reported and discussed for group X TMDs [29, 30], which differentiates them from others.



**Figure 1.2:** Figure of the general form of layered TMDs  $(MX_2)$ . The M and X are represented by brown and yellow colours. (a) top of  $MX_2$  2D and (b) side of  $MX_2$  2D

#### Platinum dioxide $(PtO_2)$

Platinum dioxide is a trigonal phase layered structure with space group  $P\bar{3}m1$  (No. 164). Stability of  $\alpha$ -PtO<sub>2</sub> phase were examined using surface x-ray diffraction (SXRD), the experiments observed that  $\alpha$ -PtO<sub>2</sub> is fully stable [31, 32]. X-ray was used to measure lattice parameters of PtO<sub>2</sub> and other phases,  $\alpha$ -PtO<sub>2</sub> has hexagonal structure a CdI<sub>2</sub>-like structure with lattice parameters  $a_0 = 3.11$  Å,  $c_0 \sim 4.34$  Å and  $V_0 = 36.44$  Å<sup>3</sup> [33]. The photoelectron spectroscopic shows that its optical gap ranges from 1.30 to 1.47 eV [34], while optical reflectance measurement gives optical gap of ~1.2 eV [35]. Zhensheng *et al.* investigated the electronic properties of  $\alpha$ -PtO<sub>2</sub>, and they reported that is a semiconductor with optical gap of 1.84 eV [36]. Metal oxide has a wide range of applications in optical devices, catalysis, photo-sensors and electronics [37].

#### Platinum disulfide $(PtS_2)$

Bulk, bilayer and monolayer PtS<sub>2</sub> crystallise in a CdI<sub>2</sub> structure, with space group  $P\bar{3}m1$ (No. 164) [26]. The lattice parameters  $a_0 = 3.54$  Å,  $c_0 = 5.04$  Å and  $V_0 = 54.78$  Å<sup>3</sup> for bulk structure were investigated using x-ray diffraction [30, 38, 39]. The structural, electronic and optical properties of monolayer PtS<sub>2</sub> have also been well investigated [40, 41, 42]. They are predicted to have promising photocatalytic properties [25], but their thermoelectric properties are yet to be well understood. Previous spectroscopic studies at 300 K show that bulk PtS<sub>2</sub> is a semiconductor with an indirect band gap of 0.95 and 0.87 eV parallel and perpendicular to the trilayers, respectively [43, 44]. Electronic structure calculations of infinite periodic bulk PtS<sub>2</sub> confirmed that bulk and monolayer PtS<sub>2</sub> are indirect band gap semiconductors [40, 41, 42].

#### Platinum diselenide ( $PtSe_2$ )

Platinum diselenide also has a trigonal phase structure, with space group  $P\bar{3}m1$  (No. 164). X-ray measurements showed that  $PtSe_2$  possess crystallises in a  $CdI_2$  like-structure and the lattice parameters are  $a_0 = 3.73$  Å,  $c_0 = 5.08$  Å and  $V_0 = 61.15$  Å<sup>3</sup> [45]. Experiments showed that bulk PtSe<sub>2</sub> has a metallic behaviour at a temperature from 5 to 380 K with a high residual resistance ratio of 184 [46]. It also has a semi-metal character [26], while monolayer and bilayer structures are semiconductors with a band gaps of 1.2 eV and 0.21 eV, respectively [47]. Phonon dispersion and electronic properties of bulk, monolayer, and bilayer  $PtSe_2$ , were investigated using DFT with the Tkatchenko and Scheffler van der Waal's correction (DFT-TS) [48]. This study confirm that the bulk is semi-metallic while monolayer and bilayer configurations are semiconductors with an indirect band gap of  $\sim 1.6$  eV and  $\sim 0.8$  eV, respectively. Yim C. et al [49] demonstrated that multilayer PtSe<sub>2</sub> is easy to synthesise and showed that vertically stacked heterostructures of PtSe<sub>2</sub> on Si can be used as photodiodes and in photovoltaic cells. The electronic structure of monolayer and bilayer  $PtSe_2$  have been calculated using the Perdew-Burke-Ernzerhof (PBE) exchange-correlation approximation with band gaps of 1.39 and 0.99 eV for  $PtSe_2$ , respectively [50]. The calculated lattice thermal conductivity of monolayer  $PtSe_2$  with a vacuum of 20.12Å, was found to be 16.97  $Wm^{-1}K^{-1}$ at 300 K [51]. The investigation of electronic and transport properties for monolayer  $PtSe_2$  reported in reference [52], suggests that this compound has promising properties for thermoelectric applications.

#### Platinum ditelluride (PtTe<sub>2</sub>)

Platinum ditelluride is a third compound of the PtX<sub>2</sub> family, with trigonal phase structure and space group  $P\bar{3}m1$  (No. 164). The lattice constant of bulk PtTe<sub>2</sub> are  $a_0 =$ 4.01 Å,  $c_0 = 5.20$  Å and  $V_0 = 72.43$  Å<sup>3</sup> was obtained experimentally using x-ray [39]. As in the case of PtSe<sub>2</sub>, bulk PtTe<sub>2</sub> has a metallic behaviour at a temperature from 5 to 380 K with a high residual resistance ratio of 29 [46]. Recently, the bulk PtTe<sub>2</sub> has been reported to be a type-II Dirac semi-metal [53]. Mechanical, electronic and optical properties were calculated for a monolyaer PtTe<sub>2</sub> using DFT, and they found a monolyaer PtTe<sub>2</sub> is a semiconductor with in direct band gap of 0.70 eV [41]. Zhishuo H *et al.* reported that a monolayer PtTe<sub>2</sub> is dynamically stable, and it is a semiconductor with an indirect band gap of 0.61 eV [42]. Biaxial strain effects on electronic structures and thermoelectric properties in monolayer  $PtTe_2$  have been investigated. The lattice thermal conductivity of monolayer  $PtTe_2$  was found to be 7.89 Wm<sup>-1</sup>K<sup>-1</sup> at 300 K [52]. Also, the electronic and transport properties for monolayer  $PtTe_2$  have been studied and reported in reference [52], and the obtained results suggest that it is promising for thermoelectric applications. The spin-orbit coupling has been shown to have an important effect on electronic structures and power factors for semiconducting TMD monolayers [54, 51, 55].

# 1.5 Aims

The aims and the specific objectives of this thesis are:

- To investigate physical properties of the layered structure of trigonal phase platinum dioxide and dichalcogenides, (PtX<sub>2</sub>; (X = O, S, Se and Te)).
- To investigate the structural and electronic properties.
- To examine the mechanical and dynamical stabilities, the elastic constants and phonon band structure through the computational approaches.
- To investigate the optical properties of most stable phases.
- To calculate the lattice thermal conductivities of the structure, the single-mode relaxation-time approximation.
- A comparison between the bulk, bilayer and monolayer, for  $PtX_2$ ; (X = O, S, Se and Te), in order to know the best one for thermoelectric applications.
- Transport properties will then be evaluated by solving Boltzmann transport equations to obtain the figure of merit, Seebeck coefficient, charge carrier concentration, lifetime, thermal and electrical conductivity as well as power factor. This will help to identify the PtX<sub>2</sub> phases which are potential candidates for thermoelectric applications.

## **1.6** Structure of this Thesis

This thesis has been arranged in the following manner: In Chapter 1, we introduce a motivation for this research as well as briefly discuss on the platinum oxide and chalcogenides. The background of density functional theory, many-body perturbation theory and Boltzmann transport theory are presented in Chapter 2. in Chapter 3, we give details of the computational methods. Chapter 4 is dedicated to our calculated results and discussions. In this section, structural, mechanical, dynamical, electronic, optical and thermoelectric properties of each compound in studied in separated section. In section 4.1 we study the the properties for  $\alpha$ -PtO<sub>2</sub>. Section 4.2 is devoted to the properties for PtS<sub>2</sub>. Section 4.3 is devoted to the properties for PtSe<sub>2</sub>. The properties for PtTe<sub>2</sub> are investigated in section 4.4. Finally, Chapter 5 summarises the main results, concludes the study.

# $\left[2\right]$

# Theoretical background

# 2.1 Many-body Schrödinger equation

In this section, we discussed the many-body systems and Born Oppenheimer approximation. The many-body systems are very complex, to study the physical and chemical properties of materials, since this material have a large number of interacting particles, so, we must then consider it as many-body problems. An *ab-initio* method was used to solve the Schrödinger equation for many-body problems. The Schrödinger equation can be expressed in the form:

$$\ddot{H}|\psi\rangle = E|\psi\rangle,$$
 (2.1.1)

where  $|\psi\rangle$  is the wave function, E is the eigenvalue of energy and  $\hat{H}$  is the Hamiltonian operator, which can be in form:

$$\hat{H} = -\frac{\hbar^2}{2m_e} \sum_{i=1}^N \nabla_i^2 - \sum_{j \neq j}^N \frac{Z_I e^2}{|\mathbf{r}_i - \mathbf{R}_I|} + \sum_{j \neq i}^N \frac{e^2}{|\mathbf{r}_i - \mathbf{r}_j|} -\frac{\hbar^2}{2M_I} \sum_{I=1}^N \nabla_I^2 - \sum_{J \neq I}^N \frac{Z_I Z_J e^2}{|\mathbf{R}_I - \mathbf{R}_J|},$$
(2.1.2)

where  $m_e$ ,  $M_I$  and N represent the electrons mass, nuclei mass, electrons and nuclei number, respectively, while  $R_I$ ,  $r_{i,j}$  and Z represent the nuclei position number  $i^{th}$ , electron position number  $i^{th}$  or  $j^{th}$  and nuclei charge, respectively.  $\hbar$  and e are the conventional fundamental constants. We can rewrite the Hamiltonian operator as follows;

$$\hat{H} = \hat{T}_n + \hat{V}_{nn} + \hat{T}_e + \hat{V}_{en} + \hat{V}_{ee}, \qquad (2.1.3)$$

whereby,  $T_n$  and  $V_{nn}$  are the kinetic energy and the potential energy of the nuclei, respectively,  $T_e$  and  $V_{ee}$  are the kinetic energy and potential energy of the electrons, respectively and  $V_{ne}$  stands for the nuclei-electron interaction.

The Born-Oppenheimer approximation suggests that to treat the movement the movement of electrons and nuclei independently because the latter has a heavy mass compared to that of electron [56]. The born-Oppenheimer approximation can be illustrated in the form of an equation as;

$$\psi(\mathbf{R}_j, \mathbf{r}_i) = \psi_e(\mathbf{R}_j, \mathbf{r}_i)\psi_n(\mathbf{R}_j), \qquad (2.1.4)$$

where  $\psi_e(\mathbf{R}_i, \mathbf{r}_i)$  is the electron wave-function and  $\psi_n(\mathbf{R}_i)$  is the nucleus wave-function.

## 2.2 Density Functional Theory

This section is focused on density functional theory description, (Hohenberg-Kohn Theorems a Kohn-Sham equation) and some approximations which have been used in this thesis. We will also talk of periodic boundary and Bloch's theorem, k-points, Brillouin zone and pseudopotentials. To simplify the original problem of many-body-system, the movement of the electrons and ionic must be treated separately and hence allows us to treat the ions in a classical formalism. Density functional theory, based on two theorems first proved by Hohenberg and Kohn [57, 58] in the 1960s, makes it possible to describe the ground-state properties of a real system in terms of its ground state charge density instead of the far more complicated wave function. This theory allows us to find the ground-state properties of a system in terms of the ground state charge density without explicit recourse to many-particle wave functions.

#### 2.2.1 The Hohenberg-Kohn Theorems

**Theorem I:** Interacting particles system in an external potential  $V(\mathbf{r})$ , this external potential is unique, for the ground state electronic charge density.

**Theorem II:** A universal functional for the energy in terms of the density can be defined, valid for any external potential  $V_{ext}(\mathbf{r})$ . For any particular  $V_{ext}(\mathbf{r})$ , the exact ground state energy of the system is the global minimum value of this functional, and the density  $\rho(\mathbf{r})$  that minimizes the functional is the exact ground state density  $\rho_0(\mathbf{r})$ . The first and second theorems have been proved in many articles. [59, 60, 57, 61, 62, 63].

#### 2.2.2 Kohn-Sham equation

Kohn and Sham assumed a practical ansatz based on non-interacting electron system, the interacting electrons system can be represented by the auxiliary ground state density system, the auxiliary Hamiltonian usually has the main term of kinetic energy operator and effective potential  $V_{eff}$  [58, 59, 60]. Where the ground state density is given by;

$$\rho[\mathbf{r}] = 2\sum_{i} |\psi_i(\mathbf{r})|^2, \qquad (2.2.1)$$

and the Hamiltonian formula is expressed as;

$$\hat{H} = \left(-\frac{\hbar^2}{2m_e}\nabla^2 + V_{KS}(\mathbf{r})\right)\psi_i = \varepsilon_i\psi_i, \qquad (2.2.2)$$

where  $V_{KS}$  is the Kohn-Sham potential operator which is consist of three components as;

$$V_{KS} = V_{ext} + V_H + V_{xc}, (2.2.3)$$

where  $V_{ext}$  is the external,  $V_H$  is the Hartree and  $V_{xc}$  is the exchange-correlation potentials.

### 2.2.3 The local density approximation

The basis of all the approximations of the exchange-correlation is the local density approximation (LDA). In the LDA, the inhomogeneous electronic system is treated as a homogeneous electron gas with uniform density. The exchange-correlation potential is dependent on the exchange-correlation energy from the electronic density, this is the local density approximation (LDA) [61] :

$$E_{xc}[\rho] = \int \rho(\mathbf{r}) \varepsilon_{xc}(\rho(\mathbf{r})) d\mathbf{r}, \qquad (2.2.4)$$

where  $\varepsilon_{xc}(\rho(\mathbf{r}))$  is the exchange-correlation energy density.

## 2.2.4 Generalised gradient approximation

Hohenberg and Kohn proposed the gradient expansion approximation (GEA) [62, 63, 60, 64] because the LDA does not works for real systems. Notwithstanding, the disappointing results, the GEA provided the basis for the generalised gradient approximation (GGA) which is currently the most popular exchange-correlation functional [61, 65] defined as;

$$E_{xc}^{GGA}[\rho] = \int \rho(\mathbf{r}) \varepsilon_{xc}(\rho(\mathbf{r})), \nabla \rho(\mathbf{r}) d^3 \mathbf{r}.$$
(2.2.5)

The GGA is considering inhomogeneity for electron density gradient. However, GGA results in almost underestimation, for example, the lattice constant and band gap results, compared to LDA results. GGA has many different types, but in this research the Perdew-Burke-Ernzerhof (PBE) [66, 67] exchange-correlation functional,

#### 2.2.5 Van der Waal's

The LDA and GGA are among stander exchange correlation functionals in DFT, to describe the structural parameters, electronic structure and other properties. However, fail to account for long-range electron correlations that are the primary cause of van der Waals interactions, resulting from dynamical correlations between fluctuating charge distributions, which play a significant role in layered structures [68]. The optimized Becker 86b van der Waals (optB86b-vdW) [69] is consider a attempt to improve approximate functionals to account for van der Waals effects.

#### 2.2.6 Periodic Boundary Conditions and Bloch's Theorem

Since the crystal solid is periodic in three dimensions (3D) and the calculations problem of that is a large number of electrons; the periodic boundary conditions (PBC) can reduce the system size to just one particular unit cell taking the symmetry into account. For a layered crystal (monolayers and surfaces), which have periodicity in two dimensions, it can be represented as slabs, with a vacuum region. To prevent the interaction between the layer, the vacuum region must be enough large to ensure the layers are decoupled.

The periodic boundary conditions in Blochs theorem [70, 71, 72], was described using the wave function in Bloch's theorem can be expressed as:

$$\psi_{\mathbf{k}}(\mathbf{r}) = e^{i\mathbf{k}\cdot\mathbf{r}} u_{\mathbf{k}}(\mathbf{r}), \qquad (2.2.6)$$

where  $\psi_{\mathbf{k}}(\mathbf{r})$  is the electronic wave function,  $\mathbf{r}$  is a position vector,  $\mathbf{k}$  is a wave vector, in the right side of the above expression, is the plane wave  $e^{ik\cdot\mathbf{r}}$  and the periodic function  $u_k(\mathbf{r})$ .

#### K-points and Brillouin zone

Three independent lattice vectors are required to define the reciprocal lattice vectors of the cell. The Wigner-Seitz size cell of the reciprocal lattice is represented as a first Brillouin zone. The volume ( $\Omega_{BZ}$ ) is defined as [73];

$$\Omega_{BZ} = \mathbf{b}_i \cdot \mathbf{b}_j \times \mathbf{b}_k = \frac{(2\pi)^2}{\Omega},$$
(2.2.7)

where  $\Omega$  is the unit cell volume. Note that the accurate method to sample the Brillouin zone has been devised by Monkhorst-Pack [74] and Chadi and Cohen [75].

#### Pseudopotentials

The physical properties of the materials depends more on valence than core electrons. The advantage of pseudopotential is substituting the core electrons and strong ionic potential by a weaker pseudopotential [76, 73, 61]. The pseudopotential represents a set of pseudo wave functions in place of the true valence wave function [73, 77]. There are many types of pseudopotentials one can construct from first-principles such as ultrasoft pseudopotentials [78], the potentials based on the projector augmented wave (PAW) method [79] and norm-conserving pseudopotentials [80].

# 2.3 Many-body perturbation theory

The Green function, GW Approximation and Bethe-Salpeter equation were covered briefly. The many-body perturbation theory (MBPT) is based on quasi-particle and Green function concepts. It is best method to accurately describe the exited states properties than DFT [60, 64].

## 2.3.1 Green's function

The Green function can be used to extract physical informations in many-body theory [81]. The energy, lifetime and expectation values of single-particle operators are the quasi-particle properties, which are obtained from the Green function [82].

## 2.3.2 GW Approximation

The solution of many-body system can be used to obtain the self-energy of two particles Green's function [83], but this is not practicable. Hedin [84] proposed GW Approximation to obtain the self-energy which is practicable method given by;

$$\sum_{GW} (\mathbf{r}, \mathbf{r}'; t) \simeq i G(\mathbf{r}, \mathbf{r}'; t) W(\mathbf{r}, \mathbf{r}'; t), \qquad (2.3.1)$$

where  $G(\mathbf{r}, \mathbf{r}'; t)$  is the interacting Green function and  $W(\mathbf{r}, \mathbf{r}'; t)$  is the dynamically screened coulomb.  $\mathbf{r}, \mathbf{r}'$  and t are the conventional fundamental constants.

#### 2.3.3 Bethe-Salpeter equation

The description of excitation state requires propagation of two particles (electron-hole pair) which is beyond the one-particle Green function GW approach. GW approach required the improvement in the response functions to account for two-particle Green function. The electron-hole pairs interaction can now be included by adding the vertex correction in vertex function which is beyond the RPA. This is done by including the vertex function  $\Gamma$  into polarizability function equation P through the second iteration and solve for polarizability <sup>3</sup>P, four-point screened-interaction function <sup>4</sup>W(1,2,3,4) and four-point Kernal function K(1,2,3,4) [85, 86]. In practice to perform BSE calculations requires one first to determine the static screened electron-hole interaction term  $W(\mathbf{x},\mathbf{x}';\omega=0)$  and the quasiparticle band structure, typically from a GWA calculation [87, 86]. With this the effective two-particle Hamiltanion  $H^{2P}$  is built,  $H^{2P}$  is diagonalized to derive the expression of macroscopic dielectric function  $\epsilon_M(\omega)$  directly related to measurable quantities. If one considers the positive resonance part of  $H^{2P}$  the resultant operator is Hermitian and its eigenstate orthogonal [85, 86].  $H^{2P}$  contributes to the bare Coulomb interaction called the electron-hole exchange and contribution due to the screen electron-hole W is responsible for the appearance of bound states, and it can even lead to hydrogen like spectral features in insulators [85].

## 2.4 Boltzmann equation

The Boltzmann equation provides description of electrons motion, which changes their position and momentum when subjected to diffusion. The linearised Boltzmann equation is given by [88, 89];

$$\sum_{\mathbf{q}'p'} \left[ \left( n_{\mathbf{q}p} - n_{\mathbf{q}p}^0 \right) - \left( n_{\mathbf{q}'p'} - n_{\mathbf{q}'p'}^0 \right) \right] Z_{\mathbf{q}p}^{\mathbf{q}'p'} - \mathbf{v}_p(\mathbf{q}) \cdot \nabla T \frac{\partial n_{\mathbf{q}p}^0}{\partial T} = 0, \quad (2.4.1)$$

where  $n_{\mathbf{q}p}$  is the distribution for phonon, (**q**) is the wave-number, p is the polarization,  $n_{\mathbf{q}p}^{0}$  is the equilibrium distribution,  $Z_{\mathbf{q}p}^{\mathbf{q}'p'}$  is the intrinsic probability and  $\mathbf{v}_{p}(\mathbf{q})$  is group velocity of phonon (**q**, p) T is temperature. The Phonon-phonon umklapp scattering can be written in the form [90];

$$\tau_U^{-1}(\omega) = B_U \omega^2 T e^{-\theta/3T}, \qquad (2.4.2)$$

with

$$B_U \approx \frac{\hbar \gamma^2}{M v^2 \theta},\tag{2.4.3}$$

where  $\gamma$  is the Grüneisen parameter,  $\omega$  is the frequency, M is the average mass of an atom and  $\theta$  is the Debye temperature [?].

# 2.5 Transport theory

It is good to understand the electrical and thermal transport behavior of thermoelectric materials, to help in finding a suitable material [91].

#### 2.5.1 Transport equation

The expression of transport equation was stated by Liouville theorem, for a distribution function of particles;

$$\frac{df}{dt} = \frac{\partial f}{\partial t} + \left[\frac{\partial f}{\partial t}\right]_{\text{external}} + \left[\frac{\partial f}{\partial t}\right]_{\text{internal}},\tag{2.5.1}$$

where  $f(\mathbf{r}, \mathbf{k}, t)$  is the carrier distribution function,  $\mathbf{r}$  and  $\mathbf{k}$  are position and wave vectors, respectively, and t is time, and also, the internal and external are denote the changes of f under external forces and internal phenomena, respectively. The carriers equation can be also written as;

$$-\left[\frac{\partial f(\mathbf{r},\mathbf{k})}{\partial t}\right]_{\text{external}} = \mathbf{v} \cdot \nabla_r f + \frac{d\mathbf{k}}{dt} \cdot \nabla_k f = \left[\frac{\partial f}{\partial t}\right]_{\text{internal}},$$
(2.5.2)

where  $\mathbf{v}$  is the carriers velocity.  $\nabla_r, \nabla_k$  are gradients with respect to position and wave vector, respectively. The relaxation time can be define as  $\tau(\mathbf{k})$ , which can represent  $\left[\frac{\partial f}{\partial t}\right]_{\text{internal}} = -\frac{f-f_0}{\tau(\mathbf{k})}$ , where f and  $f_0$  are the slightly and the equilibrium perturbed distribution function, respectively [92]. The expression of transport equation including relaxation time becomes;

$$-\frac{f-f_0}{\tau(\mathbf{k})} = \mathbf{v} \cdot \nabla_r f + \frac{d\mathbf{k}}{dt} \cdot \nabla_k f.$$
(2.5.3)

#### 2.5.2 Seebeck coefficient and electrical conductivity

The definition of the Seebeck coefficient can be written as;

$$S = \frac{dV}{dT} = \frac{1}{e} \left( \frac{\partial E_f / \partial \mathbf{r}}{\partial T / \partial \mathbf{r}} \right), \tag{2.5.4}$$

where S in equation above is given by;

$$S = \pm \frac{1}{eT} \Big[ E_f - \int_0^\infty g(E) \tau E^2 \frac{\partial f_0(E)}{\partial E} dE / \int_0^\infty g(E) \tau E \frac{\partial f_0(E)}{\partial E} dE \Big],$$
(2.5.5)

where g(E) is the electron density of states. The negative sign of the Seebeck coefficient indicates that carriers are electrons, and the positive sign of the Seebeck coefficient indicates carriers are holes [93]. On the other hand, the expression of electrical conductivity
can be given as;

$$\sigma = \frac{2e^2}{3m^*} \int_0^\infty g(E)\tau E \frac{\partial f_0(E)}{\partial E} dE, \qquad (2.5.6)$$

where  $m^*$  is the effective mass.

## 2.5.3 Thermal conductivity ( $\kappa$ )

To understand how the material response to the heat transfer, one should examine its thermal conductivity. The thermal conductivity has two main components, the electronic and lattice contributions to total thermal conductivity.

### Electronic thermal conductivity $(\kappa_e)$

The electronic thermal conductivity is due to the collision between the electrons during their movement when the temperature is raised. The electronic thermal conductivity component is an important part, especially when we have heavy doped semiconductor. The expression of  $\kappa_e$  can be written as;

$$\kappa_e = \frac{3}{2} \left(\frac{k_B}{e}\right)^2 \sigma \mathrm{T},\tag{2.5.7}$$

where  $k_B$  is Boltzmanns constant,  $\sigma$  is the electrical conductivity, and T is kinetic energy of carriers.

#### Lattice thermal conductivity $(\kappa_L)$

The lattice thermal conductivity means, heat conduction via vibrations of the lattice ions in a solid [94]. Hence, the lattice thermal conductivity can be determine using the Boltzmann equation [88, 89]. In the single-mode relaxation-time approximation [95], the lattice thermal conductivity can be expressed as;

$$\kappa_L = \frac{1}{Z\Omega} \sum C \mathbf{v} \otimes \mathbf{v}\tau, \qquad (2.5.8)$$

where Z,  $\Omega$  and  $\tau$  are the unit cell number, unit cell volume and the relaxation time or phonon lifetime respectively. C is the heat capacity that is expressed as;

$$C = k_B \left(\frac{\hbar\omega}{k_B T}\right)^2 \frac{e^{(\hbar\omega/k_B T)}}{[e^{(\hbar\omega/k_B T)} - 1]^2},$$
(2.5.9)

where  $\omega = \omega(\mathbf{q})$  is the phonon frequency, T is the temperature whereas  $k_B$  and  $\hbar$  indicate the reduced Boltzmann constant and Planck constant, respectively.  $\mathbf{v}$  is phonon group velocity that given by;

$$\mathbf{v} = \nabla_{\mathbf{q}} \omega(\mathbf{q}, j), \tag{2.5.10}$$

# [3]

# Computational details

In this chapter, we address the calculation details of DFT, MBPT and Boltzmann transport equations that have been applied in this thesis.

# 3.1 DFT Calculations

All ground state calculations were carried out using Density Functional Theory (DFT) with plane wave projector-augmented (PAW) pseudopotential formalism [96], as implemented in the Vienna *ab-initio* simulation package (VASP) [97, 98]. Within the generalised gradient approximation (GGA), the exchange-correlation functional was approximated by the Perdew-Burke-Ernzerhof (PBE) [69] formulation, while the optB86b-vdW [99] functional was used to capture the van der Waal's interactions as a result of the layered nature of the structure. The electron wave function was expanded in a plane wave basis set with an energy cut-off of 520 eV for bulk and 350 eV for bilayer and monolayers, in all calculations. A sampling of the Brillouin zone was performed using Monkhorst-Pack grid, [74] an  $8 \times 8 \times 6$  the Gamma centred k-point mesh for bulk, and a  $12 \times 12 \times 1$  the Gamma centred k-point mesh for bilayer and monolayer. Ground-state geometry of bulk, bilayer and monolayer were fully relaxed until the force on each atom was less than  $1 \times 10^{-3}$  eV/Å. The energy-convergence criterion was  $1 \times 10^{-8}$  eV, for bulk, bilayer and monolayer. For the thermal properties calculations, were created a supercell of  $4 \times 4 \times 4$  for bulk and  $5 \times 5 \times 1$  for bilayer and monolayer from their relaxed pristine unit-cell. In order to avoid any artificial interlayer interaction, a vacuum layer

of 15 Å along c direction was added for bilayer and monolayer calculations.

# 3.2 Structural Properties

#### 3.2.1 Lattice parameter

The equilibrium lattice constant for  $PtX_2$  compounds were optimized by finding the minima of the energy as a function of the lattice constant. The total energy as a function of lattice spacing is obtained by varying the lattice constants, with full relaxations of all the atoms. The fully relaxed structure from PBE and optB86b-vdW are used to perform the EOS static calculation using the Blöchl tetrahedron correction to extract energy. From which the lattice parameter is extracted [100].

#### 3.2.2 Cohesive energy

Cohesive energy was investigated at the equilibrium lattice structures. It is the negative of the energy that must be supplied to the solid to separate its constituents into neutral free atoms at rest and at infinite separation, the cohesive  $E_{\rm coh}$  can be written in form;

$$E_{\rm coh}^{\rm (PtX_2)} = \frac{E_{\rm comp.}^{\rm (PtX_2)} - N \times (xE_{\rm atom}^{\rm (Pt)} + yE_{\rm atom}^{\rm (X)})}{N \times (x+y)},$$
(3.2.1)

where N is the number of  $PtX_2$  unit per unit cell,  $E_{atom}^{Pt}$  and  $E_{atom}^{X}$  are the atomic energies of Pt and X, while x and y are the number of Pt and X atoms per unit cell, respectively.

#### 3.2.3 Formation energy

Formation energy,  $E_{\text{form}}$ , is used to verify the relative phase stabilities for any compound. Formation energy is that energy required to decompose a compound into its most stable constituent compounds. which is given by

$$E_{\rm form}^{\rm (PtX_2)} = E_{\rm coh}^{\rm (PtX_2)} - \left[\frac{xE_{\rm coh}^{\rm (Pt)} + yE_{\rm coh}^{\rm (X)}}{x+y}\right].$$
 (3.2.2)

where  $E_{\text{form}}^{(\text{PtX}_2)}$  is the total cohesive energy per PtX<sub>2</sub> unit cell;  $E_{\text{coh}}^{(\text{Pt})}$  and  $E_{\text{coh}}^{(X)}$  the cohesive energy per atom for Pt and X atoms, respectively. The parameters x and y are defined is section (3.2.2)

## 3.3 Stabilities

#### 3.3.1 Mechanical stability

Elastic constants are crucial parameters, through their knowledge, one can predict and derive a useful mechanical coefficient of a material. For bulk PtX<sub>2</sub>, in crystal structure of a trigonal, has six independent elastic constants,  $C_{11}$ ,  $C_{12}$ ,  $C_{13}$ ,  $C_{14}$ ,  $C_{33}$  and  $C_{66}$  which are similar to tetragonal crystal. The elastic matrix satisfy the Born criterion  $C_{66} = (C_{11}, C_{12})/2$ ,  $C_{11} > |C_{12}|$  and  $2C_{13}^2 < C_{33}(C_{11}, C_{12})$  [101, 102].

In this research, we calculated the elastic constants and investigated the elastic properties by two independents coefficient, Young's modulus Y and Poisson's ratio  $\nu$ . The Young's moduli describes the hardness of materials, while Poisson's ratio ( $\nu$ ) provides information on bonding nature [103]. The elastic constants ( $C_{ij}$ ) (*i* and *j* are matrix dimensions) were used to define these coefficients. For bulk, we used the Young's modulus in formula

$$Y = \frac{1}{V_0} \left( \frac{\partial^2 E_s}{\partial \varepsilon^2} \right), \tag{3.3.1}$$

where  $E_s$ ,  $\varepsilon$  and  $V_0$  are the strain energy, the uniaxial strain and volume, respectively, since the bulk is a 3D (three-dimensional) structure which depends on volume  $V_0$ . Since the bilayer and monolayer is 2D (two dimensional), so we focus of the in-plane Young's moduli which is depends on the equilibrium in-plane area,  $A_0$ , of the supercell and the strain energy. The Young's moduli is defined as

$$Y = \frac{1}{A_0} \left( \frac{\partial^2 E_s}{\partial \varepsilon^2} \right),. \tag{3.3.2}$$

To obtain the Young's modulus and Poisson's ratio  $\nu$  for a bulk we used Hill's approach [104], and for a bilayer and monolayer, we used two independent elastic constants,  $C_{11}$  and  $C_{12}$  [105]. The two dimensional expression for Y can also be written in terms of

elastic constants as [41, 105, 106, 107, 108]

$$Y = (C_{11}^2 - C_{12}^2)/C_{11}, (3.3.3)$$

and the two dimensional Poisson's ratio can be expressed as

$$\nu = C_{12}/C_{11}.\tag{3.3.4}$$

#### 3.3.2 Dynamical stability

The associated collective excitation for crystal lattice vibrations is called the phonons [95]. Highly converged forces were required for the calculations of the dynamical matrix using the direct force constant approach as implemented in the PHONOPY package [109]. We employed a  $4 \times 4 \times 4$  supercell for bulk and  $5 \times 5 \times 1$  supercell for bilayer and monolayer. The phonon dispersion relations were computed along several high symmetry directions using relaxed lattice parameters. The gap usually observes between the acoustic and optical mode, indicates that the difference in mass between Pt atom mass and X atomic mass according to Eq. 3.3.5. It is clear that Pt atoms have more contribution in the low frequency region which is acoustic region, and X atoms have more contribution in the high frequency which is optical mode region.

$$\omega_{\pm}^{2} = K \left( \frac{1}{M_{1}} + \frac{1}{M_{2}} \right) \pm K \sqrt{\left[ \left( \frac{1}{M_{1}} + \frac{1}{M_{2}} \right)^{2} - \frac{4sin^{2}(\mathbf{q}a/2)}{M_{1}M_{2}} \right]},$$
(3.3.5)

where  $\omega$  is frequency  $M_1$ ,  $M_2$  is the mass of Pt and X atoms, respectively, K is spring constant, **q** wave vector and a are the separate distance between two mass [110]. The two solutions of Eq. 3.3.5 are two branches of phonon, the plus sign, for the optical mode, and the minus sign is for the acoustic mode.

#### **3.4** Electronic properties

A diagram of the electronic energy band is the essential quantity that characterises the electronic structure of a solid and determines its ground state and a series of excitations involving electronic states [111]. Electronic structure properties are defined by band structure and density of states (DOS), which clarify the occupied and unoccu-

pied electronic states. The band gap is the forbidden states that located between the valence and conduction bands, the magnitude of band gap is classifying the materials into insulators, semiconductors or metals. Moreover, the band structure diagram is used to distinguish the nature of the band gap ( direct or indirect ) depending of the position of the maximum valence band (MVB) and minimum conduction band (MCB) with respect to the k-points. The DOS is a simple form describing the condenses of the band structure properties for the occupied state in reciprocal space [112]. Total DOS is combined from the projection DOS that shows the contribution of the orbitals. The band gap can be defined through the DOS by top edge of the valence and bottom edge of the conduction. The calculation of the electronic structure was done in the Brillouin zone along the high symmetry path. We used the optimized lattice parameter for bulk, bilayer and monolayer, and k-point of  $8 \times 8 \times 6$  for bulk and  $12 \times 12 \times 1$  for bilayer and monolayer in carrying out the electronic studies.

# 3.5 Optical coefficient

The optical coefficients were determined as follows, the imaginary part  $\varepsilon_1(\omega)$  of the dielectric function is obtained from the momentum matrix elements between the occupied and unoccupied wave-functions. The real part  $\varepsilon_1(\omega)$ , is defined by the Kramer-Kronig relations [113], whereas the absorption coefficient  $\alpha(\omega)$  is derived from the dielectric function as follows: [114].

$$\varepsilon_{2,\alpha\beta}(\omega) = \frac{4\pi^2 e^2}{\Omega} \lim_{q \to 0} \frac{1}{q^2} \sum_{CV\mathbf{k}} 2w_{\mathbf{k}} \delta(\epsilon_{C\mathbf{k}} - \epsilon_{V\mathbf{k}} - \omega) \\ \times \langle u_{C\mathbf{k}+e_{\alpha}q} | u_{V\mathbf{k}} \rangle \langle u_{C\mathbf{k}+e_{\beta}q} | u_{V\mathbf{k}} \rangle^*, \qquad (3.5.1)$$

$$\varepsilon_{1,\alpha\beta}(\omega) = 1 + \frac{2}{\pi} \mathbf{P} \int_0^\infty \frac{\varepsilon_{2,\alpha\beta}(\omega')\omega'd\omega'}{\omega'^2 - \omega^2},\tag{3.5.2}$$

$$\alpha(\omega) = \frac{\sqrt{2}\omega}{c} \left[ \sqrt{\varepsilon_{1,\alpha\beta}^2(\omega) + \varepsilon_{2,\alpha\beta}^2(\omega)} - \varepsilon_{1,\alpha\beta}(\omega) \right]^{1/2}, \qquad (3.5.3)$$

where  $w_{\mathbf{k}}$  is the k-points weight,  $\Omega$  is the volume of the unit cell,  $e_{\alpha}$  are unit vectors, and V and C are induces restricted to the valence and conduction band, respectively. While **P** refer to the principal value,  $\alpha$  and  $\beta$  are tensor dimensions,  $\omega$  is frequency and c is the speed of light.

The investigation of the optical properties for the bilayer and monolayer were performed using a supercell, where a single layer was included per supercell. For comparison of the bulk, bilayer and monolayer, we obtained the optical absorbance, and the percentage of the radiation absorbed, in the visible photon energy range of 1 - 3 eV, by a single layer in the bulk, bilayer and a monolayer. The computed results for a single layer of bulk, bilayer and monolayer were calculated by using the absorbance,  $A = 1 - exp(-\alpha(\omega)\Delta z)$ , where  $\alpha(\omega)$  is the absorption coefficient and  $\Delta z$  is the thickness of a slab of the material. For comparison with a bilayer and a monolayer, we set  $\Delta z$  equal to the thickness of a single layer in the bulk. While for the bilayer and monolayer, the absorption coefficient scales like the inverse of the length of the supercell perpendicular to the layer for a sufficiently large supercell and the correct value of  $\Delta z$  in a periodic supercell calculation is the length of the supercell perpendicular to the layer [115, 116].

We described the absorption edge using the Tauc plot of the optical dispersion, the Tauc method [117] determine absorption edge by linear extrapolation of  $(\alpha h\nu)^{\frac{1}{n}}$  to zero from an equation  $\alpha h\nu = K(h\nu - E_g)^n$ . Where  $E_g$  is the gap,  $\alpha$  is absorption,  $h\nu$  the photon energy, K the proportionality constant and the exponent n takes values 2,  $\frac{1}{2}$ ,  $\frac{3}{2}$  and  $\frac{1}{3}$  for direct, indirect, allowed and forbidden transitions, respectively.

# **3.6** Lattice thermal conductivity

The lattice thermal conductivity calculation was done using the PHONO3PY package [109] that solves the single-mode relaxation-time approximation of the linearised phonon Boltzmann transport equation. A  $4 \times 4 \times 4$  supercell for bulk and  $5 \times 5 \times 1$  supercell for bilayer and monolayer were used for solving the linearised lattice Boltzmann transport equation in the single-mode relaxation time approximation PHONO3PY package [95]. In the thermal conductivity calculation, 2753 for bulk, while 3700 and 950 for bilayer and monolayer, respectively. A unique triplet displacements were included in the calculation of the scattering terms [95]. The normal unit for thermal conductivity is  $Wm^{-1}K^{-1}$  per unit cross-sectional area, which gives the thermal conductivity of a volume of material

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of a cross-sectional area of  $1 \text{ m}^2$  and 1 m thick, with heat conducted perpendicular to the cross-sectional area. For a single layer, the cross-sectional area for out-of-plane thermal conductivity is taken as  $1 \text{ m}^2$ , but the thickness is that of a single layer. The cross-sectional area for single layer in-plane thermal conductivity is that of the crosssectional area of a single layer perpendicular to the plane of the layer. The 'thickness' is taken as 1 m. For single layers we use units of Wm<sup>-1</sup>K<sup>-1</sup> per cross-sectional area (not per unit cross-sectional area), where the cross-sectional area and thickness depends on the direction in which the heat flow is measured. With this definition, the units for thermal conductivity are consistent for bulk and single layers [1].

# 3.7 Transport phenomena

We used the deformation potential and elastic constants to calculate a set relaxation times of charge carrier which were dependent on k-point and energy, as proposed by Bardeen and Shockley [118]. To determine the electronic transport coefficients, we used these relaxation time. The BoltzTraP2 package [119] was used to solve the Boltzmann transport equations resulting in the approximate values of various transport coefficients such as S,  $\sigma$  and  $\kappa_e$  as the output. The calculation of transport coefficients as a function of temperatures such as Seebeck, power factor, electrical conductivity, and thermal conductivity, was done for a single layer in bulk, bilayer, and monolayer, to investigate the thermoelectric potential of this binary compounds. The in-plane coefficients were considered for a single layer in bulk, bilayer and monolayer calculations. The concentrations of charge carriers which were used are  $10^{19}$  and  $10^{20}$  cm<sup>-3</sup> for all PtX<sub>2</sub> except, the bulk of PtO<sub>2</sub> when we used  $10^{20}$  and  $10^{21}$  cm<sup>-3</sup>. The range of temperature considered varies since it depends on the melting point for each compound.

# 4

# **Results and Discussions**

The structural, mechanical and dynamical stabilities, electronic, optical and thermoelectric properties of trigonal structure  $PtX_2$  (X = O, S, Se and Te) were investigated in this section, based on the theoretical methods (Chapter 2) and computational details (Chapter 3), the obtained results are presented and discussed. Figure 4.1 illustrated the bulk, bilayer and monolayer (a) bulk unit cell, (b) monolayer unit cell, (c) top view of the monolayer, and (d) side view of the monolayer. The Octahedral coordination 1T shows Platinum atoms sandwiched (X-Pt-X) between two layers of X atoms.



**Figure 4.1:** Crystal structure of bulk, bilayer and monolayer PtX<sub>2</sub>. (a) the bulk structure unit cell, (b) the monolayer structure unit cell, (c) top view of monolayer and (d) side view of bilayer. The Pt atoms and X atoms are represented by grey and red ball, respectively.

# 4.1 Platinum dioxide ( $\alpha$ -PtO<sub>2</sub>)

#### 4.1.1 Structural Properties

In Table 4.1, we listed the equilibrium lattice constant  $(a, c \text{ and } V_0)$  of the bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>. The lattice parameters of bulk obtained using optB86b-vdW functional are close to the experimental results, while those from the PBE functional are slightly overestimated. The calculated lattice parameters of bilayer and monolayer are similar to the previous study for monolayer. The optB86b-vdW approximation includes an approximation of long-range interaction. This could explain the difference between the results from the two functionals. On the other hand, we set  $c = 15 \text{\AA}$ as a vacuum layer for bilayer and monolayer which is make the vad der Waal's force between the layers to be weak. The investigation of the phase stability was done using the cohesive and formation energies as defined in Chapter 3, using Equation (3.2.1) and (3.2.2), respectively. In Table 4.1, we listed the cohesive and formation energies per atom for bulk, bilayer and monolayer, and compared with available previous studies. Cohesive and formation energies are used to study phase stability in the solid-state. Our calculations gave a negative of cohesive energy and formation energy, indicative of energetically stable compounds. the values of cohesive energy and formation energy are independent of the approximation used.

**Table 4.1:** Calculated, experimental and theoretical optimized lattice constants of bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>, cohesive ( $E_{coh}$ ) and formation formation energies per atom, and inter-layer distance.

		a (Å)	c (Å)	$V_o$ (Å <sup>3</sup> )	$E_{coh}$ (eV)	$E_{form}$ (eV)
Bulk	PBE	3.15	4.91	42.32	-4.35	-0.49
	optB86b-vdW	3.12	4.36	36.92	-4.54	-0.44
	$\operatorname{Exp}^{[120]}$	3.11	4.34	36.44	-	_
	$\operatorname{Exp}^{[121]}$	3.10	4.16	34.63	-	_
	$\operatorname{Exp}^{[122]}$	3.08	4.19	34.42	-	_
Bilayer	PBE	3.12	15	-	-4.37	-0.51
	optB86b-vdW	3.12	15	-	-3.30	-1.11
Monolayer	PBE	3.12	15	-	-4.37	-0.51
	optB86-vdW	3.12	15	-	-3.27	-0.41
	Previous work <sup>[123]</sup>	3.14	-	-	_	-0.40

#### 4.1.2 Mechanical stability

In this section we examine the mechanical stability for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>. The elastic constants listed in Table 4.2, fulfil the Born stability criteria [102] see section (3.3.1), which indicate that bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub> are mechanically stable. The Young's moduli and Poisson's ratio for  $\alpha$ -PtO<sub>2</sub>, were obtained for bulk, bilayer and monolayer are represented in Table 4.3. We observe that Young's moduli increases with the increase of the number of layers, indicative of increased resistance to deformation under the application of opposing forces as the number of layers are increased. The results agree with previous study [41], for monolayer. In Table 4.3, we present the calculated Young's moduli (Y) and Poisson's ratio ( $\nu$ ) for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>, and bulk moduli and shear moduli for bulk  $\alpha$ -PtO<sub>2</sub>. The calculated results for bilayer and monolayer are in accordance with the calculated value of in-plane stiffness for MoS<sub>2</sub>, which is 123 GPa, while the Poisson's ratio in accordance with Si and MoS<sub>2</sub> which are 0.30 and 0.25, respectively, reported in ref [124].

**Table 4.2:** Elastic constants ( $C_{ij}$  (GPa)) for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>.

		C <sub>11</sub>	$C_{12}$	$C_{13}$	$C_{33}$	$C_{66}$
Bulk	optB86b-vdW	270.42	70.26	20.81	25.89	100.08
Bilayer	PBE	122.22	38.12	_	_	_
Monolayer	PBE	178.87	53.12	_	_	—

**Table 4.3:** The obtained Bulk moduli (B) Shear moduli (G), Young's moduli (Y) and Poisson's ratio ( $\nu$ ) in GPa, for bulk, bilayer and monolayer.

		B	Y	G	ν
Bulk	optB86b-vdW	56.78	100.45	41.68	0.21
Bilayer	PBE	-	110.33	_	0.31
Monolayer	PBE	_	116.18	_	0.23

#### 4.1.3 Dynamical Stability

The phonon calculations for the bulk  $\alpha$ -PtO<sub>2</sub> were done using the optb86B-vdw relaxed structure. Since optB86b-vdW and PBE functions gave the same equilibrium lattice parameters for bilayer and monolayer, so we used PBE for phonon calculations since it is computationally less demanding. The phonon dispersion was calculated along with





**Figure 4.2:** The band structure of phonon dispersion for  $\alpha$ -PtO<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.

several high symmetry directions. Figure 4.2 shows the phonon dispersion band structure and 4.3 shows the phonon dispersion density of states and atoms contribution, relations of  $\alpha$ -PtO<sub>2</sub> bulk, bilayer and monolayer, computed at the equilibrium configuration zero pressure using the PHONOPY package [125, 109]. The phonon frequencies are positive throughout the Brillouin with zone, which indicates that the bulk, bilayer and monolayer compounds are dynamically stable. The phonon frequencies are in the range of (0 - 18.73) THz for bulk, (0 - 18.12) THz for bilayer and (0 - 18.83) THz for the monolayer, respectively. Note, the bilayer phonon band structure appears dense compared to the bulk and monolayer. This is due to the increase in the number of atoms per unit cell, while the frequency range is almost unchanged for all three configurations. The bulk and monolayer of the primitive cell of  $\alpha$ -PtO<sub>2</sub> contain three atoms and therefore there are nine phonon modes for each wave vector (three acoustic modes and six optical modes). For the bilayer, the primitive cell of  $\alpha$ -PtO<sub>2</sub> contains six atoms and therefore, there are eighteen phonon modes or each wave vector (six acoustic modes and twelve optical modes). The highest frequency of the acoustic modes, defined here as the acoustic cut-off, is approximately 8.8 THz for bulk, 8.42 THz for bilayer and 8.68 THz for monolayer. Figure 4.2(a-c) depicts the phonon band structure for bulk, bilayer and monolayer, respectively, and the total density of states and atoms contribution are shown in Figure 4.3(a-c). The phonon band structure and density of states for bulk, bilayer and monolayer show the same behaviour. It is evident that (O) controlled in the frequency optical region, and (Pt) contributes more in the frequency acoustic region.



**Figure 4.3:** Phonon total and partial density of states for  $\alpha$ -PtO<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.

Table 4.4: The calculated band gaps compared to the experimental and theoretical (in eV) of  $\alpha$ -PtO<sub>2</sub>.

	optB86-vdW	PBE	$GW_0$	Experimental	Previous work
Bulk	1.61	1.63	2.73	$1.30 - 1.47^{[34]}, 1.2^{[35]} 1.84^{[36]}$	—
Bilayer	1.63	1.74	4.36		
Monolayer	1.72	1.86	$4.73, 4.00^{[123]}$		$2.00^{[123]}$

#### 4.1.4 Electronic structure properties

The electronic band structure of bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub> are presented in Figure 4.4(a-c), respectively. They all exhibited an indirect semiconductor band gap, of values 1.61, 1.73 and 1.86 eV, respectively. MVB and MCB are located between  $\Gamma$ and M points for bulk, and between A and L points for bilayer and monolayer. We also present the total and partial density of states (TDOS and PDOS) in Figure 4.4(a-c) for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>, respectively. The maximum and minimum edge of the band gap in density of states, which is caused by valence and conduction band, respectively, are contributed by Pt(s), Pt(d) in valence band, while the minimum conduction band is mainly due to the Pt(s), Pt(d) and O(p) orbitals for all the three structures. It is important to point out that the band structure of bilayer looks denser than than of the bulk and monolayer while its DOS is also higher. This is due to the difference in the number of atoms in the primitive cell, as we mentioned before. We summarise our calculated fundamental band gap values in Table 4.4 and compared with available experimental values.





**Figure 4.4:** Calculated electronic structure of  $\alpha$ -PtO<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.

Carolyn R A [34] used x-ray photoelectrons spectroscopy to determine the optical properties of the bulk  $\alpha$ -PtO<sub>2</sub>. The absorption coefficient and the optical transitions of infrared show that its optical band gap varies between 1.30 and 1.47 eV. An optical band gap of 1.2 eV was obtained for  $\alpha$ -PtO<sub>2</sub> by Neff H *et al.* [35], using x-ray diffraction, energy-sensitive microanalyses, optical reflectance measurements and resistivity. Scanning tunnelling spectroscopy measurements by Zhensheng J *et al* [36], give a optical gap of 1.84 eV. Hence, our calculated results are range of experimental values which vary from 1.2 to 1.84 eV. The bilayer and monolayer band gap are represented in Table 4.4, the monolayer value is high than bilayer hence, the value of bilayer also higher than of bulk.



Figure 4.5: Calculated total and partial DOS. (a) Bulk (b) Bilayer (c) Monolayer.

#### 4.1.5 Optical properties

In this section, we use Equation 3.5.1, 3.5.2 and 3.5.3 as defined in Chapter 3 to calculate the imaginary and real parts of the dielectric functions. The absorption and absorbance as well as other related parameters were then derived from the dielectric functions. Figure 4.6(a-c) depict the imaginary and real parts of the dielectric functions and the absorbance respectively, computed with the BSE  $GW_0$  approximation. Figure 4.7(c) illustrate the absorbance of bulk, bilayer and a monolayer. The maximum absorbance in in-plane polarization for monolayer is  $\approx 8.06\%$  at 2.92 eV and for bilayer is  $\approx 5.64\%$  at 2.51 eV and 0.91% at 2.12 eV for bulk. The absorbance of a monolayer is considerably greater than the absorbance for a bilayer and bulk. This agrees with  $MoS_2$ ,  $MoSe_2$  and  $WS_2$  results (5–10%) [115, 116], where the single layer absorbance is high in monolayer than bilayer and bulk. Moreover, in the out-of-plane polarisation, the maximum absorbance is  $\approx 0.09\%$  at 2.99 eV for monolayer and  $\approx 0.39\%$  at 2.82 eV for bilayer and 0.14% at 2.15 eV for a single layer of bulk. The optical band gap was obtained by fitting our BSE optical data on the Tauc plot [117]. It is worth mentioning that the BSE is considered up to date as the best of estimation for the optical properties as it included the two particles Green's function. For the bulk  $\alpha$ -PtO<sub>2</sub>, the in-plane and out-of-plane optical band gap polarizations are 1.66 and 1.77 eV, respectively, which is an average of the experimental measurements range. The difference of two values suggests significant optical anisotropy, and it suits to photovoltaic solar cells applications [126]. The calculated optical band gaps of the in-plane and out-of-plane polarization, for the monolayer, are 2.32 and 2.75 eV, and for bilayer are 1.89 and 2.34 eV, while for bulk are found to be 1.63 and 1.77 eV, respectively. Also suits to photovoltaic solar cells applications.

#### 4.1.6 Lattice thermal conductivity

Figure 4.7(a) and (b) show the lattice thermal conductivity against temperature and frequency, respectively, for a single layer of bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub> structure. The average lattice thermal conductivity at 300 K for single layer in bulk, bilayer and monolayer is  $8.47 \times 10^{-8}$ ,  $4.59 \times 10^{-8}$  and  $1.06 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> in-plane direction for bulk, bilayer and monolayer respectively, in the out-of-of the plane direction, we found it to be  $0.05 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> for bulk and zero for the others. The lattice thermal conductivity for a single layer in bulk decreases by about ~46% of the bilayer and



**Figure 4.6:** (a) Imaginary part  $\varepsilon_2(\omega)$ , (b) real part  $\varepsilon_1(\omega)$  of dielectric function and (c) absorbance for bulk, bilayer and monolayer of  $\alpha$ -PtO<sub>2</sub>.

 $\sim 87\%$  of the monolayer, in the in-plane. Furthermore, a high in-plane lattice thermal conductivity was found to be at the low-temperature. For instance, our calculations predict a value of  $24.61 \times 10^{-8} \text{ Wm}^{-1} \text{K}^{-1}$  at 70 K for bulk, and  $18.90 \times 10^{-8} \text{ Wm}^{-1} \text{K}^{-1}$ at 50 K for bilayer and  $2.19 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 100 K for monolayer. The high outof-plane is  $0.52 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 10 K for bulk. The lattice thermal conductivity against frequency at 300 K is presented in Figure 4.7(b), and its cumulative lattice thermal conductivity as a function of the frequency of single layer for bulk, bilayer and monolayer. We observed that the lattice thermal conductivity is highly anisotropic, with the thermal conductivity in-plane of the layers being much higher than that of the out-of-plane direction for two cases bulk, bilayer and monolayer. Furthermore, we calculated the directional projected density of states for each atom as a function of frequency. Figure 4.8 shows the in-plane and out-of-plane contributions, left and right, respectively, which are along [100] and [001]. The results of directional projected density of states look like phonon density of states, but here we have directional contributions. The Pt atoms contributed more in acoustic mode than O atoms and vice versa for optical mode for all bulk, bilayer and monolayer, in the in-plane direction. In the outof-plane direction, we only have the contribution for bulk. To know the contribution ratio of phonon to lattice thermal conductivity, we examine the contribution of acoustic and optical phonons branches mode. At 300 K, the in-plane (out-of-plane) acoustic mode total contribution to the thermal conductivity is 94% (77%), 96.65% (0%) and 93% (0%) for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub> respectively. The contributions of phonon to lattice thermal conductivity per atoms are illustrated in Figure 4.9 (left and



Figure 4.7: Lattice thermal conductivity and heat capacity for bulk and monolayer  $\alpha$ -PtO<sub>2</sub>. (a) Lattice thermal conductivity against temperature, (b) cumulative lattice thermal conductivity against frequency.

right), for bulk, bilayer and monolayer. Through Figure 4.9, we can note that the ratio of contribution is almost the same in in-plane, for bulk, bilayer and monolayer. The out-of-plane contribution of the bulk is given at the right. This is in clear contrast to the conventional understanding, especially in the out-of-plane direction, where the acoustic modes dominate thermal conductivity [127].

#### Phonon lifetime

The phonon lifetime is the time between two phonon-phonon scattering events and it is obtained by third-order force constants [90, 95]. Figure 4.10(a-c) shows how the bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub> phonon lifetime depends on frequency, at 300 K. The highest peak for phonon lifetime is located in acoustic mode, and while the lowest peak for phonon lifetime is located in optical mode for all structures. This is in accordance with a somewhat powerful scattering in the high frequency optical phonon modes. To differentiate the phonon lifetime distribution of acoustic and optical phonon mode [128].





Figure 4.8: Directional projected density of states, left is in-plane and right is out-ofplane for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub> as function of frequency.



Figure 4.9: Contribution ratio of phonon to lattice thermal conductivity, left is inplane and right is out-of-plane for bulk and monolayer  $\alpha$ -PtO<sub>2</sub> as function of frequency. (Recall there is no contribution in out-of-plane for monolayer).



Figure 4.10: Phonon lifetime at 300 K, (a) Bulk, (b) bilayer and (c) monolayer of  $\alpha$ -PtO<sub>2</sub> as function of frequency.





Figure 4.11: Phonon average of directional group velocity, (a) Bulk, (b) bilayer and (c) monolayer of  $\alpha$ -PtO<sub>2</sub> as function of frequency.

#### Group velocity

The group velocity depends on the dispersion as shown in Equation (2.5.10). In this work, we calculated the average of directional group velocities for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>. The obtained results are shown in Figure 4.11(a-c). In the low frequency range, the in-plane group velocities are higher than out-of-plane, while at high frequency the in-plane and out-of-plane are small compared to the low frequency values. The anisotropy in group velocities has a great impact on the lattice thermal conductivity [129]. The group velocities distributions of the bulk, bilayer and monolayer for in-plane are almost similar, except in out-of-plane which have a value of 6 Å.THz for bulk, while it is 0 Å.THz for bilayer and monolayer. The combined effect of the frequency dependence of the phonon lifetimes and group velocities are consistent with the anisotropy in the thermal conductivity as well as the large contribution to the total thermal conductivity from the low frequency phonons.

#### 4.1.7 Transport properties of $\alpha$ -PtO<sub>2</sub>

The calculated Seebeck coefficients are presented in Figure 4.12 for bulk, bilayer, and monolayer  $\alpha$ -PtO<sub>2</sub>. We observed that the maximum values of Seebeck coefficient were obtained for holes concentrations, which are  $429\mu$ V/K at 700 K for bulk and, 573  $\mu$ V/K at 700 K for bilayer, and  $484\mu$ V/K at 700 K for the monolayer. From the plot, we can notice that the Seebeck coefficients increase as the temperature increases.

In Figure 4.13, we illustrated the electrical conductivity for the single layer in bulk, bilayer, and monolayer  $\alpha$ -PtO<sub>2</sub>. We found that the highest values at 200 K are  $1.23 \times 10^{-4}$ 



**Figure 4.12:** Seebeck coefficients of bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>.

S/m,  $3.9 \times 10^{-4} S/m$  and  $28.2 \times 10^{-4} S/m$ , respectively, which are attributed to electrons carriers concentration such as  $10^{21} cm^{-3}$  for bulk, and  $10^{20} cm^{-3}$  for bilayer and monolayer.



Figure 4.13: Electrical conductivity for a single layer in bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>.

On the other hand, we computed the electronic contribution to thermal conductivity for the single layer in bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>, to gauge the contribution to the total lattice thermal conductivity from electronic thermal. Figure 4.14 depicts the highest values, at a high temperature of 700 K for bulk while it is at a low temperature of 200 K for bilayer and monolayer. However, the highest values are determined by the majority charge carriers such as electrons. The obtained results show the lowest electronic contribution is obtained the bulk structure followed by the monolayer, and whereas the bilayer  $\alpha$ -PtO<sub>2</sub> had the highest values of  $\kappa_e$  which could be attributed to the variation in their band gap size.

The power factor was calculated over a temperature range of from 200 K to 700 K for the single layer in bulk, bilayer, and monolayer. The obtained results are plotted in Figure 4.15, where, we see the difference in the behavior between the bulk, and



**Figure 4.14:** Electronic contribution to thermal conductivity for a single layer in bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>.

bilayer and monolayer. The highest values of power factor for the all structures are  $3.95 \times 10^{-12} \text{WK}^{-2} \text{m}^{-1}$  for bulk at 700 K, and  $232 \times 10^{-12} \text{WK}^{-2} \text{m}^{-1}$  for bilayer at 200 K, while, it is  $48 \times 10^{-12} \text{WK}^{-2} \text{m}^{-1}$  at 200 K for monolayer.



**Figure 4.15:** Power factor for a single layer in bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>.

The dimensionless figure of merit (ZT) was calculated from 200 K to 700 K, and the values for the single layer in bulk, bilayer, and monolayer  $\alpha$ -PtO<sub>2</sub> show at 700 K, 400 K, and 300 K, respectively. The obtained ZT values are 0.11 for bulk, 0.62 for bilayer and 0.74 for monolayer, as illustrated in Figure 4.16. The high values of the figure of merit were obtained when the carriers are electrons in all case. As a result, this system provides a broad operational range. These results indicate that at room temperature the monolayer has a high value among the three structures, and is therefore a promising candidates for the thermoelectric power generation applications, with further tuning.



**Figure 4.16:** Figure of merit for bulk, bilayer and monolayer  $\alpha$ -PtO<sub>2</sub>.

## 4.2 Platinum disulfide ( $PtS_2$ )

#### 4.2.1 Structural Properties

The fully optimized equilibrium lattice parameters  $(a, b \text{ and } V_0)$  of the bulk, Bilayer and monolayer  $PtS_2$  are listed in Table 4.5. The lattice parameter of bulk  $PtS_2$ , a = 3.55 Å and c = 5.03 Å calculated by using optB86b-vdW are close to a = 3.54 Å and c = 5.04Å from the experimental measurements [30, 38, 39]. The obtained lattice parameters for the bilayer are similar to the bulk and monolayer. The monolayer lattice parameter is in agreement with the ones from previous studies. Note that for the PBE bulk results, the lattice parameter c of the bulk, perpendicular to the layers, is relatively larger compared to the experimental values, while the optB86b-vdW value is in good agreement. On the other hand, we set  $c = 15 \text{\AA}$  as a vacuum layer for bilayer and monolayer which is make the vad der Waal's force between the layers to be weak. We believe that it is due to the fact that The optB86b-vdW takes into consideration the long-range interactions which are not captured by the PBE. The investigation of the phase stabilities for bulk, bilayer and monolayer, were done using the cohesive and formation energies as defined in Chapter 3, using Equation (3.2.1) and (3.2.2), respectively. In Table 4.9, we listed the cohesive and formation energies per atom for bulk, bilayer and monolayer, and compared with available previous studies. Our calculated cohesive and formation energies are negative, which suggest that the bulk, bilayer and monolayer  $PtS_2$  are energetically stable. The bulk, bilayer and monolayer cohesive and formation energies per atom, respectively, are similar for each approximation, which is consistent with the understanding that the inter-layer bonding is weak and its contribution to the total energy is relatively small.

		a (Å)	c (Å)	$V_o$ (Å <sup>3</sup> )	$E_{coh}$ (eV)	$E_{form}$ (eV)
Bulk	PBE	3.51	5.35	56.92	-4.21	-0.34
	optB86b-vdW	3.55	5.03	54.87	-3.60	-0.45
	$\operatorname{Exp}^{[30]}$	3.54	5.04	54.79	—	_
	$\operatorname{Exp}^{[38]}$	3.54	5.04	54.78	-	_
	$\operatorname{Exp}^{[39]}$	3.54	5.04	54.76	_	_
Bilayer	PBE	3.55	15	-	-4.22	-0.35
	optB86b-vdW	3.54	15	-	-3.43	-2.04
Monolayer	PBE	3.58	15	-	-4.23	-0.36
	optB86b-vdW	3.58	15	-	-3.48	-2.09
	Previous work <sup>[130]</sup>	3.57	_	_	_	_
	Previous work <sup>[41]</sup>	3.58	—	_	-	_
	Previous work <sup>[42]</sup>	3.52	_	_	_	_
	Previous work <sup>[123]</sup>	3 57	_	_	_	-0.33

**Table 4.5:** Calculated, experimental and theoretical optimized lattice constants of bulk bilayer and monolayer  $PtS_2$ , cohesive  $(E_{coh})$  and formation formation energies per atom, and inter-layer distance.

#### 4.2.2 Mechanical Stability

In this section, we investigated the mechanical stability for bulk, bilayer and monolayer  $PtS_2$ . The elastic constants presented in Table 4.6, fulfil the Born stability criteria [102] see section (3.3.1), which indicate that bulk, bilayer and monolayer  $PtS_2$  are mechanically stable. The Young's moduli and Poisson's ratio for  $PtS_2$  were obtained for bulk, bilayer and monolayer are represented in Table 4.7. We observed that Young's moduli increase with the increase of the number of layers, indicative of increased resistance to deformation under the application of opposing forces as the number of layers are increased. The results agree with previous study for monolayer [41]. In Table 4.7, we presented the obtained Young's moduli (Y) and Poisson's ratio ( $\nu$ ) for bulk, bilayer and monolayer  $PtS_2$  which consistent with available previous study [41]. The values of the Young's moduli in Table 4.7 show that the bilayer can withstand deformation more than the monolayer and the bulk.

**Table 4.6:** Elastic constants ( $C_{ij}$  (GPa)), for bulk, bilayer and monolayer PtS<sub>2</sub>.

		$C_{11}$	$C_{12}$	$C_{13}$	$C_{14}$	$C_{33}$	C <sub>66</sub>
Bulk	optB86b-vdW	130.43	62.52	23.41	16.99	11.46	33.96
Bilayer	PBE	122.22	38.12	-	—	-	-
Monolayer	PBE	81.86	24.25	_	—	—	-
Monolayer	Other work <sup>[41]</sup>	91.82	32.10	_	_	_	_

**Table 4.7:** The obtained Bulk moduli (B) Shear moduli (G), Young's moduli (Y) and Poisson's ratio ( $\nu$ ) in GPa, for bulk, bilayer and monolayer, and the other theoretical study.

		B	Y	G	ν
Bulk	optB86b-vdW	31.84	55.85	23.12	0.21
Bilayer	PBE	_	110.33	_	0.31
Monolayer	PBE	—	74.67	—	0.29
Monolayer	Other work <sup>[41]</sup>	—	80.59	_	0.27

#### 4.2.3 Dynamical Stability

For phonon dispersion calculations, we used optB86-vdW approximation for bulk while PBE approximation for bilayer and monolayer, since they have a best lattice parameters compare to experimental and previous study. The phonon dispersion relations were calculated along with several high symmetry directions. Figure 4.17(a-c) show the phonon dispersion band structure and Figure 4.18(a-c) show the phonon dispersion density of states, relations of  $PtS_2$  bulk, bilayer and monolayer, respectively, calculated at the equilibrium configuration with the PHONOPY package [109]. The phonon frequencies are positive throughout the Brillouin zone, which suggests that the bulk, bilayer and monolayer  $PtS_2$  are dynamically stable. The phonon frequencies are in the range of 0 - 11.7 THz for bulk and 0 - 10.57 THz for bilayer and 0 - 10.47 THz for the monolayer, respectively. The reducing in the frequency range for the monolayer is possibly due to the reducing in a number of atomic bonds in the bilayer and monolayer compared to the bulk. The highest frequency of the acoustic modes, defined here as the acoustic cut-off, are approximately 6 THz for both bulk, bilayer and monolayer. Note, the bilayer phonon band structure is dense compared to the bulk and monolayer, which is the same as bilayer  $PtO_2$ . In Figure 4.11(a-c), we plot the total and partial density of states for bulk, bilayer and monolayer, respectively. It is proved, that the Pt atom dominates in the low frequency acoustic region, and the S atom contributes more to the high frequency optical mode region.

#### 4.2.4 Electronic structure properties

The electronic structure investigation is presented in this section for the bulk, bilayer and monolayer  $PtS_2$ . In Figure 4.19(a-c), we plotted the band structure of the bulk, bilayer and the monolayer  $PtS_2$ , respectively. Bulk  $PtS_2$  is an indirect band gap of



**Figure 4.17:** The band structure of phonon dispersion for  $PtS_2$ . (a) Bulk (b) Bilayer (c) Monolayer.



Figure 4.18: TDOS and atomic contributions to acoustic and optical modes of phonon dispersion for  $PtS_2$ . (a) Bulk (b) Bilayer (c) Monolayer.

value 0.81 eV, with a maximum of the valence band at  $\Gamma$  point and the minimum of the conduction band at K point. For bilayer and monolayer PtS<sub>2</sub>, the maximum of the valence is between the K and  $\Gamma$  points, while the minimum of the conduction band lies between  $\Gamma$  and M points, indicating an indirect band gap for bulk, bilayer and monolayer. In Figures 4.20(a-c), we also plotted the total and partial density of states (TDOS and PDOS) for each atom of bulk, bilayer and monolayer PtS<sub>2</sub>, respectively. S(p) has the largest contribution at the top of the valence band followed by Pt(d), for bulk, bilayer and monolayer. In the conduction band, orbital hybridization between the Pt(d) and the S(p) states occurs for bulk, bilayer and monolayer. The dense of bilayer band structure is similar to the bilayer of PtO<sub>2</sub>. To investigate the intrinsic

Table 4.8: The calculated band gaps values compared to the experimental and theoretical (in eV) of  $PtS_2$ .

	optB86-vdW	PBE	$GW_0$	Exp.	Other calculations
Bulk	0.81	1.06	1.10	$0.87^{[44]}, 0.95^{[131]}, 0.7^{[132]}$	$0.48^{[133]}, 1.2^{[26]}, 0.73^{[130]}$
Bilayer	1.13	1.26	3.78		
Monolayer	1.67	1.80	$3.90, 3.14^{[123]}$	$1.6^{[133]}$	$1.81^{[130]}, 1.76^{[41]}, 1.94^{[40]},$
					$1.78^{[134]}, 1.69^{[42, 123]}, 1.80^{[135]}$

band gap we used many approximations namely the optB86b-vdW, PBE and  $GW_0$ . In the calculations involving post DFT approximations, we used the optimized lattice parameters from the optB86b-vdW geometric optimisation in the case of bulk PtS<sub>2</sub> and the values for the PBE calculation for the bilayer and monolayer. In Table 4.8, we summarise the computed values with previous studies and experimental results included for comparison. The measured band gaps of this material vary from 0.7 to 0.95 eV, a relatively wide range of values. We observed that the optB86b-vdW approximation gives value within the range of the reported experimental results, while PBE, surprisingly, gives a value above the experimental range. Such unusual behaviour, where GGA DFT overestimates the band gap of transition metal dichalcogenides has also been reported in previous studies [136]. Note that all the DFT gap energies are approximate fundamental gap energies [137], while the experimental values are optical gap values. Direct comparisons are strictly not justified, but it is a common practice in the literature to compare these values. Experimental band gap values for the bulk  $PtS_2$  have been reported by a number of groups: F. Parsapour et al. reported a band gap of 0.87 eV using optical spectroscopy [44]; H. Tributsch and O. Gorochov measured a band gap of 0.95 eV, by means of photoelectrochemical mechanisms [131]; and diffuse-reflectance measurements by F. Hulliger give a band gap of 0.7 eV [132]. The band gap of the bulk  $PtS_2$  has also been obtained by many authors: Y. Zhao et al. used the optB86bvdW to predict a band gap of 0.48 eV [133]; a band gap of 1.2 eV was obtained by G. Guo and W. Liang [26] using the linear muffin-tin orbital method combined with the atomic sphere approximation method [138], and the PBE calculations by H.L. Zhuang and R.G. Hennig give a 0.73 eV band gap [130]. The only experimental band gap of the monolayer  $PtS_2$  was reported by Y. Zhao et al [133]. They obtained, using the Fourier-transform infra red spectrometry, a band gap of 1.6 eV. Theoretical monolayer gap values have also been reported. Band gaps of 1.76 and 1.94 eV were predicted by J. Du et al. [41] using the PBE, with the spin-orbit coupling included; and S. Ahmed [40] using the PBE, respectively. P. Miró et al. [134] used the dispersion corrected PBE exchange-correlation functional (PBE-BJ-D3) [69, 139] to obtain a band gap of 1.78 eV, whereas the local density approximation calculations by Z. Huang give an estimation of 1.69 eV [42]. The band gap value of bilayer is found to be 1.13 and 1.26 eV, by using optB86b-vdW and PBE approximations, respectively. The difference between our band gap results which we computed with the optB86b-vdW and PBE approximations and the results of other calculations of 0.48 eV using optB86b-vdW approximation [133] and 0.73 eV using PBE approximation [130] for bulk PtS<sub>2</sub>, for monolayer the other calculations are 1.76 using PBE [41] and 1.78 eV using PBE [69, 139], which were performed with the same approximations. Our calculated values are more much close to experimental values. May the reason is can come from differences between DFT implementations and input variables including lattice parameters, k-points and energy cut-offs, after convergence test for all. The calculated band gap values for bulk, bilayer and monolayer were found to be suitable for photovoltaic

#### 4.2.5 Optical properties

For the optical properties, the imaginary and real parts of the dielectric functions were calculate by solving the BSE approximation in conjunction with the GW since the later usually gives a good approximation of the fundamental band gap. Figure 4.21(a) and (b) illustrate the imaginary part and real part of dielectric functions for bulk, and a single layer of bilayer and a monolayer. The absorbance of a single layer in bulk, a single layer of a bilayer and a monolayer  $PtS_2$  was plotted in Figure 4.21(c). The maximum absorbance for in-plane polarisation for a monolayer is  $\approx 13.15\%$  at 2.51 eV, for bilayer  $\approx 7.64\%$  at 1.83 eV and  $\approx 2.00\%$  at 2.90 eV for bulk. For out-of-plane



**Figure 4.19:** Bulk, bilayer and monolayer  $PtS_2$  calculated electronic structure using optB86b-vdW for bulk and PBE for bilayer and monolayer. (a) Bulk, (b) bilayer and (c) monolayer. Along high symmetry directions.



**Figure 4.20:** Bulk, bilayer and monolayer  $PtS_2$  calculated TDOS and PDOS for each atom and orbital using optB86-vdW for bulk and PBE for bilayer and monolayer. (a) Bulk, (b) bilayer and (c) monolayer.



**Figure 4.21:** GW<sub>0</sub> BSE results (a) imaginary part  $\varepsilon_2(\omega)$ , (b) real part  $\varepsilon_1(\omega)$  of dielectric function and (c) absorbance for bulk, bilayer and monolayer of PtS<sub>2</sub>.

polarisation, the maximum absorbance is  $\approx 0.09\%$  at 2.6 eV for monolayer,  $\approx 0.15\%$  at 2.54 eV and 0.9% at 3 eV for bulk. The absorbance of a monolayer is substantially higher than the absorbance of bulk. This is consistent with results for graphene and MoS<sub>2</sub> [115, 116], where the monolayer absorbance is higher than the absorbance of bulk. The optical band gap was estimated by fitting the BSE optical absorption with the Tauc plot [117]. The BSE approximations are expected to give a good estimation of the optical properties. For the bulk PtS<sub>2</sub>, the optical band gap for the in-plane and out-of-plane polarisations are 1.09 and 1.36 eV, respectively. The difference between the two values shows significant optical anisotropy. The value for in-plane polarisation band gap is in accordance with the experimental value. The in-plane and out-of-plane polarisation, respectively. The in-plane optical band gap is once again consistent with the experimental values as given in Table 4.9. The obtained results for bulk and bilayer make them candidates for photovoltaic applications [126].

#### 4.2.6 Lattice thermal conductivity

Figure 4.22 (a) and (b) plots the lattice thermal conductivity dependence of the temperature and frequency for a single layer in bulk, bilayer and a monolayer. As demonstrated in Figure 4.22(a), the average in-plane lattice thermal conductivity for a single layer at 300 K is  $2.30 \times 10^{-8}$ ,  $1.16 \times 10^{-8}$  and  $0.15 \times 10^{-8} \text{ Wm}^{-1}\text{K}^{-1}$  for bulk, bilayer and mono-



Figure 4.22: Lattice thermal conductivity per layer, (a) lattice thermal conductivity against temperature, (b) cumulative lattice thermal conductivity against frequency.

layer, respectively. The out-of-plane thermal conductivity is  $0.08 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> for a single layer of the bulk, whereas it is zero for the monolayer and bilayer. The in-plane lattice thermal conductivity for a monolayer is ~7% and ~49.6% of that of a single layer in bulk and bilayer, respectively. This is a significant decrease and points to a possible technique for decreasing lattice thermal conductivity by decreasing the thickness to a few layers. Further, the highest in-plane value of lattice thermal conductivity found to be in the low-temperature range with  $8.66 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 60 K,  $5.04 \times 10^{-8}$ Wm<sup>-1</sup>K<sup>-1</sup> at 50 K and  $0.61 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 60 K for a single layer in bulk and bilayer, and a monolayer, respectively. The highest out-of-plane thermal conductivity for a single layer in bulk is  $0.34 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 10 K. We observe that the lattice thermal conductivity is highly anisotropic, with the in-plane thermal conductivity much higher than the out-of-plane thermal conductivity for all bulk, bilayer and monolayer.

Furthermore, we calculated the directional projected density of states for each atom as a function of frequency. Figure 4.23 shows the in-plane and out-of-plane contributions, left and right, respectively, which are along [100] and [001]. The results of directional projected density of states look like phonon density of states, but here we have directional contributions. The same behavior of the directional projected for  $PtO_2$ . To perceive the contribution ratio of phonon to lattice thermal conductivity for bulk, bilayer and monolayer  $PtS_2$ , we examine the contribution of acoustic and optical phonons branches mode. We obtained that the in-plane acoustic mode total contribution is



Figure 4.23: Directional projected density of states, left is in-plane and right is outof-plane for bulk, bilayer and monolayer  $PtS_2$  as function of frequency.



Figure 4.24: Contribution ratio of phonon to lattice thermal conductivity, left is inplane and right is out-of-plane for bulk and monolayer  $PtS_2$  as function of frequency. (Recall there is no contribution in out-of-plane for monolayer).

96.23%, 96.42% and 97.12% for bulk, bilayer and monolayer  $PtS_2$  respectively. While the out-of-plane 77.01% for bulk, and 0% for bilayer and monolayer. The contributions of phonon to lattice thermal conductivity per atoms are illustrated in Figure 4.24 (left and right), for bulk, bilayer and monolayer. Through Figure 4.24, we can note that the ratio of contribution is almost the same in in-plane, for bulk, bilayer and monolayer. This is in clear contrast to the conventional understanding, especially in the out-of-plane direction, that the acoustic modes dominate thermal conductivity [127].

#### Phonon lifetime

In this section, we define the phonon lifetime, which is the time between events phononphonon scattering, which is calculated by third-order force constants [90, 95]. Figure



**Figure 4.25:** Phonon lifetime against frequency at 300 K. (a) Bulk, (b) bilayer and (c) monolayer.

4.25(a-c) shows how the bulk, bilayer and monolayer  $PtS_2$  phonon lifetime depends on frequency, at 300 K. The highest peak for phonon lifetime is located in acoustic mode, and while the lowest peak for phonon lifetime is located in optical mode for all structures. This is in accordance with a slightly strong scattering in the high frequency optical phonon modes. The phonon lifetime distribution of acoustic and optical phonon mode can be used to differentiate the phonon lifetime contributions to the total lattice thermal conductivity [128].

#### Group velocity

The group velocity depends on the dispersion as plotted in Equation (2.5.10). In this study, we computed the average of directional group velocities for bulk, bilayer and monolayer PtS<sub>2</sub>. The calculated results are depicted in Figure 4.26(a-c). In the low frequency range, the in-plane group velocities are higher than out-of-plane, while at high frequency the in-plane and out-of-plane are small compared to the low frequency values. The anisotropy in group velocities have a great impact on the lattice thermal conductivity [129]. The group velocities distributions are almost identical for the three structures in the in-plane direction, but in the out-of-plane direction, the bulk has a value of 10 Å.THZ while the other remain at 0 Å.THz. The combined effect of the frequency dependence of the phonon lifetimes and group velocities are consistent with the anisotropy in the thermal conductivity as well as the large contribution to the total thermal conductivity form the low frequency phonons.



**Figure 4.26:** Average directional phonon group velocities against frequency. (a) Bulk, (b) bilayer and (c) monolayer.

#### 4.2.7 Transport properties of PtS<sub>2</sub>

The Seebeck coefficients were calculated and presented in Figure 4.27 for bulk, bilayer and monolayer  $PtS_2$ , at a range of temperature between 200 to 500 K. The results predict the highest values of Seebeck coefficient for holes carriers concentrations of  $10^{19}$  cm<sup>-3</sup>. At 500 K we obtained  $294\mu$ V/K for bulk,  $334 \mu$ V/K for bilayer and  $410\mu$ V/K for monolayer. From the plots, we can observe that the Seebeck coefficients are increasing with the increasing of the temperature.



Figure 4.27: Seebeck coefficients of bulk, bilayer and monolayer  $PtS_2$ .

The electrical conductivity for the bulk, bilayer and monolayer  $PtS_2$  are depicted in Figure 4.28. We found the maximum values for a single layer at 200 K, are  $1.75 \times 10^{-4}$ S/m for bulk,  $7.97 \times 10^{-4}$  S/m for bilayer and  $3.6 \times 10^{-4}$  S/m for monolayer, which are caused by electrons carriers whose concentration is  $10^{20}$  cm<sup>-3</sup>. For all concentration of charge carriers, the electrical conductivity decreases with an increase in temperature. This indicates that the electrical conductivity decreases when the temperature is increase due to their inverse relationship, which it is converse to what was noted in





Figure 4.28: Electrical conductivity for a single layer in bulk, bilayer and monolayer  $PtS_2$ .

In order to know the contribution to the total thermal conductivity arising from the electronic component, we examined the electronic contribution to the total thermal conductivity. Figure 4.29 depicts the maximum values, at a low temperature of 200 K for a single layer in bulk, bilayer and monolayer, achieve by the majority of electrons carriers concentration of  $10^{20}$  cm<sup>-3</sup>. The obtained results show the same behaviour occur, from bulk to bilayer and to monolayer structure, with different highest values. Generally, for semiconductors the lattice thermal contribution often dominates the total thermal conductivity, since  $\kappa_L \ge \kappa_e$ .



Figure 4.29: Electronic contribution to thermal conductivity coefficients for a single layer in bulk, bilayer and monolayer  $PtS_2$ .

Power factor is a parameter used to measure the ability of electric power generation of a material. The power factor was calculated over a temperature range of from 200 to 500 K for a single layer in bulk, bilayer and monolayer. The obtained results are plotted in Figure 4.30. Similarity on the power factor gradient can be observed among the structures. The highest and lowest values of power factor for all structures are obtained from



Figure 4.30: Power factor for a single layer in bulk, bilayer and monolayer  $PtS_2$ .

The ZT was obtained within the range of from 200 to 500 K. The high value of figure of merit for each of a single layer in bulk, bilayer and monolayer  $PtS_2$  were attained at 200 K, 500 K and 500 K, respectively. Their ZT values are 0.04 for bulk, 0.12 for bilayer and 0.18 for monolayer, as illustrated in Figure 4.31. The maximum values of figure of merit were dominated by electrons carriers concentration of  $10^{19} \text{ cm}^{-3}$ , while the lowest values are dominated by electrons carriers concentration of  $10^{20} \text{ cm}^{-3}$ , in all cases. The small values of the figure of merit are possibly due to the high values of lattice thermal as provided in the previous section. ZT values are increasing in opposite to increasing the number of layers.



Figure 4.31: Figure of merit for bulk, bilayer and monolayer  $PtS_2$ .
# 4.3 Platinum diselenide ( $PtSe_2$ )

#### 4.3.1 Structural Properties

The fully optimized equilibrium lattice parameters of bulk, bilayer and monolayer PtSe<sub>2</sub>, using optB86-vdW and PBE approximations and compared with available experimental and previous study data are listed in Table 4.9. We observed that the calculated results of the lattice parameters using optB86-vdW function agreed to the experimental for bulk and monolayer to the previous study. On the other hand, the obtained lattice parameters for the bilayer are close to the bulk and monolayer. On the other hand, we set c = 15Aas a vacuum layer for bilayer and monolayer which is make the vad der Waal's force between the layers to be weak. The investigation of the phase stability done using the cohesive and formation energies as defined in Chapter 3, using Equation (3.2.1) and (3.2.2), respectively. In Table 4.9, we listed the energy and formation energies per atom for bulk, bilayer and monolayer, and compared with available previous studies. The computed cohesive energy and formation energies are negative. Hence, the bulk, bilayer and monolayer  $PtSe_2$  are energetically stable. The *a* and *c* lattice parameters, the interlayer structural parameters, show the least variation across the different approximations. The inter-layer spacing, defined by the c lattice parameter, show the most variation. We note that optB86-vdW gives the best equilibrium structural parameters for bulk  $PtSe_2$  when compared to the experimental.

**Table 4.9:** Calculated, experimental and theoretical, optimized lattice constants of bulk, bilayer and monolayer  $PtSe_2$ , cohesive  $(E_{coh})$  and formation formation energies per atom, and inter-layer distance.

		a (Å)	c (Å)	$V_o$ (Å <sup>3</sup> )	$E_{coh}$ (eV)	$E_{form}$ (eV)
Bulk	PBE	3.81	4.87	61.24	-4.20	-0.38
	optB86b-vdW	3.76	4.97	61.11	-4.55	-0.43
	$Exp^{[45, 30]}$	3.72	5.08	61.15	-	_
	$\operatorname{Exp}^{[121]}$	3.74	5.14	62.54	-	_
Bilayer	PBE	3.76	15	-	-3.95	-0.39
	optB86b-vdW	3.76	15	-	-3.22	-0.31
Monolayer	PBE	3.81	15	-	-3.96	-0.38
	optB86-vdW	3.81	15	_	-3.03	-0.71
	Previous work <sup>[130]</sup>	3.75	-	-	-	0.11
	Previous work <sup>[123]</sup>	3.75	-	_	_	-0.36

#### 4.3.2 Mechanical stability

In this section, we examined the mechanical stability of the three PtSe<sub>2</sub> structures. The elastic constants listed in Table 4.10, fulfil the Born stability criteria [102] see section (3.3.1), which indicate that bulk, bilayer and monolayer PtSe<sub>2</sub> are mechanically stable. The Young's moduli and Poisson's ratio for PtSe<sub>2</sub> were obtained for bulk, bilayer and monolayer are represented in Table 4.11. We observed that Young's moduli increases with the increase of the number of layers, indicating the increase of the resistance to deformation under the application of opposing forces as the number of layers are increased. The results agree with previous study [41], for monolayer. We also present the calculated Young's moduli (Y) and Poisson's ratio ( $\nu$ ) for bulk, bilayer and monolayer PtSe<sub>2</sub>, and bulk moduli and shear moduli for bulk PtSe<sub>2</sub>, which consistent to an available previous study [41]. The values of the Young's moduli in Table 4.11 shows that the bulk is more resistant to deformation than monolayer and bilayer, also the bilayer more resist than monolayer.

**Table 4.10:** Elastic constants ( $C_{ij}$  (GPa)), for bulk, bilayer and monolayer PtSe<sub>2</sub>.

		$C_{11}$	$C_{12}$	$C_{13}$	$C_{33}$	$C_{66}$
Bulk	optB86b-vdW	197.7	67.89	41.32	40.73	64.91
Bilayer	PBE	76.52	18.19	_	_	—
Monolayer	PBE	65.38	19.37	_	—	—
Monolayer	Other work <sup>[41]</sup>	73.73.40	26.30	_	_	_

**Table 4.11:** The obtained Bulk moduli (B) Shear moduli (G), Young's moduli (Y) and Poisson's ratio ( $\nu$ ) in GPa, for bulk, bilayer and monolayer PtSe<sub>2</sub>, and the other theoretical study.

		B	Y	G	ν
Bulk	optB86b-vdW	66.75	102.97	41.42	0.24
Bilayer	PBE	_	72.19	_	0.24
Monolayer	PBE	_	59.64	_	0.29
Monolayer	Other work <sup>[41]</sup>	_	64.35	_	0.25

#### 4.3.3 Dynamical stability

The harmonic phonon dispersion relations were computed along with the high symmetry directions. The phonon band structure, total density of states and partial density of



**Figure 4.32:** The band structure of phonon dispersion for PtSe<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.



**Figure 4.33:** TDOS and atomic contributions to acoustic and optical modes of phonon dispersion for PtSe<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.

states, for bulk, bilayer and monolayer  $PtSe_2$  are presented in Figure 4.32(a-c) and Figure 4.33(a-c), respectively. The phonon partial density of states shows the atomic contribution to the total phonon density. The range of phonon frequencies is between 0 - 6.6 THz for bulk and monolayer, while for bilayer is 0 - 6.7 THz. All the phonon frequencies are positive, which indicates that the bulk, bilayer and monolayer of  $PtSe_2$ are dynamically stable. The similarity behavior of bilayer  $PtSe_2$ , was noted for  $PtO_2$  and  $PtS_2$  in the phonon band structure. The total and partial density of states respectively for bulk, bilayer and monolayer are presented in Figure 4.11(a-c). It is evident that the Pt atom controls in the low frequency acoustic region and the Se atom contributes more to the high frequency optical mode region.



**Figure 4.34:** Bulk, bilayer and monolayer PtSe<sub>2</sub> calculated electronic structure using optB86b-vdW for bulk and PBE for bilayer and monolayer. (a) Bulk, (b) Bilayer (c) Monolayer. Along high symmetry directions.

#### 4.3.4 Electronic structure properties

The electronic band structure, total and partial density of states of the bulk, bilayer and monolayer  $PtSe_2$  are shown in Figure 4.34(a-c) and Figure 4.35(a-c), respectively. The electronic structure calculations proved that the bulk phase of both compounds shows is a semi-metal, while the bilayer and monolayer are semiconductor with an indirect band gap. The minima of the conduction are located between  $\Gamma$  and M, while the maxima of the valance are at the A and L points, of the Brillouin zone. Furthermore, we calculated the density of states (total and partial), Figure 4.35(a-c) illustrated the contributions of atoms to the gap edge. The density of states in Figure 4.35(a) confirmed the band structure plot for bulk a semi-metal behaviour. But, the density of states for bilayer and monolayer show that the maximum valence band is mostly do to the Se(p) orbital while the minimum conduction band comes from the hybridisation between the Pt(d)and Se(p) states. Note, the bilayer band structure appears dense as it is in  $PtO_2$  and  $PtS_2$  bilayer. In Table 4.12, we summarised the band gap values for bulk, bilayer and monolayer for PtSe<sub>2</sub>. Our calculated results agree with the experimental and previous studies in Table 4.12. We find that the band gaps decrease with the increasing number of layers as it was previously reported by Xu M et al. [140]. The values of the band gap explain that the bilayer and monolayer suitable to photovoltaic applications.





**Figure 4.35:** Bulk, bilayer and monolayer PtSe<sub>2</sub> calculated TDOS and PDOS for each atom and orbital using optB86-vdW for bulk and PBE for bilayer and monolayer. (a) Bulk (b) Bilayer (c) Monolayer.

Table 4.12: The calculated band gaps values compared to the experimental and theoretical (in eV) of  $PtSe_2$ .

	optB86-vdW	PBE	$GW_0$	Exp.	Other calculations
Bulk	semimetal	semimetal	-	semimetal <sup>[29, 47]</sup>	-
Bilayer	0.76	0.93	1.24	$\sim 0.80^{[48]}$	$0.21^{[47]}, 0.99^{[50]}$
Monolayer	1.25	1.38	$3.90, 2.10^{[130]}, 2.67^{[123]}$	$1.6^{[48]}$	$1.20^{[47]}, 1.22^{[141]}, 1.41^{[130]}, 1.39^{[50]},$
					$1.29^{[123]}, 1.25^{[42]}, 1.40^{[135]}, 1.18^{[51]}$



**Figure 4.36:** GW<sub>0</sub> BSE results (a) imaginary part  $\varepsilon_2(\omega)$ , (b) real part  $\varepsilon_1(\omega)$  of dielectric function and (c) absorbance for bulk, bilayer and monolayer of PtSe<sub>2</sub>.

#### 4.3.5 Optical properties

Figure 4.36(a-c) presents the calculated imaginary and real parts of the dielectric functions, and the absorbance of bulk, a single layer of the bilayer and a monolayer PtSe<sub>2</sub>. As we mentioned it in the case of other compounds, these properties are obtained by solving the BSE. The maximum absorbance in in-plane polarization for monolayer is  $\approx$ 31.05% at 2.06 eV and for bilayer is  $\approx 26.89\%$  at 1.51 eV and 25.04% at 1.95 eV for bulk. The absorbance of a monolayer is considerably greater than the absorbance for a bilayer and bulk. This is higher than that of  $MoS_2$ ,  $MoSe_2$  and  $WS_2$  (5–10%) [115, 116], where the single layer absorbance is high in monolayer than bilayer and bulk. Moreover, in the out-of-plane polarisation, the maximum absorbance is  $\approx 0.09\%$  at 2.60 eV for monolayer and  $\approx 0.96\%$  at 1.58 eV for bilayer and 16.00% at 0.80 eV for bulk. We used the Tauc plot [117] to calculate the optical band gap. For the bulk PtSe<sub>2</sub>, the in-plane and out-of-plane optical band gap polarizations are 0.1 and 0.3 eV, respectively. The value for in-plane polarisation gap is higher than a predicted experimental gap. For the monolayer, the optical band gap of 1.43 and 1.64 eV was predicted for the in-plane polarisation and out-of-plane, respectively. The calculated optical band gaps of the inplane and out-of-plane polarization, for the bilayer are 1.10 and 1.25 eV, respectively. Therefore, the obtained values of the bilayer could also be used for photovoltaic solar cells applications, [142, 143, 144].

#### 4.3.6 Lattice thermal conductivity

The lattice thermal conductivity against temperature and frequency were shown in Figure 4.37(a) and (b) respectively, for a single layer of bulk, bilayer and monolayer PtSe<sub>2</sub> structure. The average lattice thermal conductivity at300 K for a single layer in bulk, bilayer and monolayer is  $0.47 \times 10^{-8}$ ,  $0.24 \times 10^{-8}$  and  $0.11 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> in-plane direction for a single layer in bulk, bilayer and monolayer respectively, and  $0.10 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> out-of-plane for bulk while the out-of-plane for bilayer and monolayer are zero. The lattice thermal conductivity value for a single layer in bulk decreases by about ~49% of the bilayer and ~77% of the monolayer, in the in-plane. Further, the high in-plane value of lattice thermal conductivity per single layer was found to be in the low-temperature range is  $7.27 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 20 K for bulk, and  $2.39 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 20 K for bilayer and  $2.27 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 30 K for monolayer. The high out-of-plane is  $1.28 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 10 K for single layer bulk.

 $10^{-8} \text{ Wm}^{-1} \text{K}^{-1}$ 

Lattice thermal conductivity  $\kappa_{\! L}$  per layer

Δ

2

In-plane



0° 0  $^{0}_{0}$ 100 400 500 600 2 200 300 3 4 Frequency (THz) 5 6 Temperature (K) **Figure 4.37:** Lattice thermal conductivity per layer for  $PtSe_2$ , (a) lattice thermal

conductivity vs temperature, (b) cumulative lattice thermal conductivity vs frequency.

0.1

thermal conductivity against frequency at 300 K is plotted in Figure 4.7(b), and its cumulative lattice thermal conductivity as a function of the frequency of single layer for bulk, bilayer and monolayer. We observed that the lattice thermal conductivity is highly anisotropic, with the thermal conductivity in-plane of the layers being much higher than in the out-of-plane direction for two cases bulk, bilayer and monolayer. The all lattice thermal conductivity values for a single layer in bulk, bilayer and monolayer PtSe<sub>2</sub>, are suits for thermoelectric application

Furthermore, we calculated the directional projected density of states for each atom as a function of frequency. Figure 4.38 shows the in-plane and out-of-plane contributions, left and right, respectively, which are along [100] and [001]. The results of directional projected density of states look like phonon density of states, but here we have directional contributions. The Pt and Se atoms contribution to the directional projected density of states look like PtO<sub>2</sub> and PtS<sub>2</sub> compounds. While in out-of-plane just we only have the contribution for bulk. To understand the contribution ratio of phonon to lattice thermal conductivity for bulk, bilayer and monolayer PtSe<sub>2</sub>, we compute the contribution of acoustic and optical phonons branches mode. The contribution estimated to the thermal conductivity from the acoustic modes at 300 K. We obtained that the inplane acoustic mode total contribution is 95.12%, 95.39% and 96.58% for bulk, bilayer and monolayer  $PtSe_2$  respectively. While the out-of-plane 86.02% for bulk, and 0% for bilayer and monolayer. The contributions of phonon to lattice thermal conductivity per



Figure 4.38: Directional projected density of states, left is in-plane and right is outof-plane for bulk, bilayer and monolayer PtSe<sub>2</sub> as function of frequency.



Figure 4.39: Contribution ratio of phonon to lattice thermal conductivity, left is inplane and right is out-of-plane for bulk and monolayer  $PtSe_2$  as function of frequency. (Recall there is no contribution in out-of-plane for monolayer).

atoms are illustrated in Figure 4.39 (left and right), for bulk, bilayer and monolayer. Through Figure 4.39, we can note that the ratio of contribution is almost the same in in-plane, for bulk, bilayer and monolayer. Also in the right, we have out-of-plane, which is for bulk. This is in clear contrast to the conventional understanding, especially in the out-of-plane direction, that the acoustic modes control thermal conductivity [127].

#### Phonon lifetime

Figure 4.40(a-c) shows how the bulk, bilayer and monolayer  $PtSe_2$  phonon lifetime depends on frequency, at 300 K. The highest peak for phonon lifetime is located in acoustic mode, and while the lowest peak for phonon lifetime is located in optical mode for all structures. This is in accordance with a somewhat potent scattering in the high



**Figure 4.40:** Phonon lifetime against frequency at 300 K for PtSe<sub>2</sub>. (a) Bulk, (b) bilayer and (c) monolayer.

frequency optical phonon modes. To differentiate the phonon lifetime contributions to the total lattice thermal conductivity, one can use the phonon lifetime distribution of acoustic and optical phonon mode [128].

#### Group velocity

The calculated results are plotted in Figure 4.41(a-c). The in-plane group velocity is higher than out-of-plane in the low frequency range, while at high frequency the inplane and out-of-plane are small compared to the low frequency values. The anisotropy in group velocity has a big impact on the lattice thermal conductivity [129]. The similarity of the distribution for in-plane group velocities of bulk and monolayer. In contrast, the out-of-plane group velocities is 11 Å.THz for bulk and zero for others. The combined effect of the frequency dependence of the phonon lifetimes and group velocities are consistent with the anisotropy in the thermal conductivity as well as the large contribution to the total thermal conductivity form the low frequency phonons.

#### 4.3.7 Transport properties of PtSe<sub>2</sub>

In Figure 4.42, we present the calculated Seebeck coefficients for bulk, bilayer and monolayer  $PtSe_2$  at range of temperature between 200 K to 600 K. The highest values of Seebeck coefficient were obtained when majority carriers are holes with concentrations of  $10^{19}$  cm<sup>-3</sup> to be  $1013\mu$ V/K at 200 K for bulk, and  $343\mu$ V/K at 600 K for bilayer, while for monolayer it was 376  $\mu$ V/K at 600 K.

In Figure 4.43, the highest values of the electrical conductivity are found at 200 K for



**Figure 4.41:** Average directional phonon group velocities against frequency for PtSe<sub>2</sub>. (a) Bulk, (b) bilayer and (c) monolayer.



Figure 4.42: Seebeck coefficients of bulk, bilayer and monolayer PtSe<sub>2</sub>.

all structures. For the bulk, it is  $0.53 \times 10^{-4}$ ,  $18.07 \times 10^{-4}$  and  $3.42 \times 10^{-4}$  S/m for the bilayer and monolayer, respectively. These values are achieved when the electrons carriers concentration is  $10^{20}$  cm<sup>-3</sup>. For all concentration of carriers, the electrical conductivity decreases with an increase in temperature. This explains that the electrical conductivity, whereby an increase in temperature results in a decrease in electrical conductivity due to their inverse relationship, and it is converse to what was noted in Figure 4.42 for the case of Seebeck coefficient.

Figure 4.44 illustrate the computed electronic contribution to thermal conductivity for a single layer in the bulk, bilayer and monolayer PtSe<sub>2</sub>. The highest  $\kappa_e$  values are achieved at a high temperature of 600 K for bulk, while it is at low temperature (200 K) for both bilayer and monolayer. At 200 K for bulk, bilayer and monolayer are dominated by the majority of electrons carriers concentration of  $10^{20}$  cm<sup>-3</sup>, while minimum temperature values, were dominated by the majority hole carriers whose concentration is  $10^{19}$  cm<sup>-3</sup>. The calculated results show the same behaviour of electrical contribution Figure 4.43 for bilayer and monolayer structures. Oftenly, in reality, the lattice thermal



**Figure 4.43:** Electrical conductivity for a single layer in bulk, bilayer and monolayer PtSe<sub>2</sub>.



contributions dominate the total thermal conductivity since  $\kappa_L \ge \kappa_e$ .

**Figure 4.44:** Electronic contribution to thermal conductivity for a single layer in bulk, bilayer and monolayer PtSe<sub>2</sub>.

The power factor was calculated over a temperature range of temperature, from 200 K to 600 K for a single layer bulk, bilayer and monolayer  $PtSe_2$ , the obtained results plotted in Figure 4.45. The similarity between the bulk and the bilayer and a monolayer is visible in the plot. The highest and lowest values of power factor for the bulk structure is detected at 600 K which 06 obtained by the electrons carriers concentration of  $10^{20}$  cm<sup>-3</sup>, and for bilayer and monolayer are at 200 K which detected by the electrons carriers concentration of  $10^{20}$  cm<sup>-3</sup>, respectively, close to 200 K. The charge carriers concentration decreases gradually when the temperature increase, which is reverse to the lowest charge carriers concentration.

The dimensionless figure of merit (ZT) was determined within 500K and 600 K for PtSe<sub>2</sub>. The figure of merit magnitudes of 0.16 at 500 K for bulk, and 0.35 at 600 K for bilayer, and 0.46 at 300 K for monolayer were extracted, as illustrated in Figure 4.46. The high values of the figure of merit were achieved by holes carriers in bulk case, and



Figure 4.45: Power factor for a single layer in bulk, bilayer and monolayer PtSe<sub>2</sub>.

by electrons carriers in bilayer and monolayer cases. The monolayer structure possess a higher value than bulk and bilayer.



Figure 4.46: Figure of merit for bulk, bilayer and monolayer PtSe<sub>2</sub>.

## 4.4 Platinum ditelluride (PtTe<sub>2</sub>)

#### 4.4.1 Structural Properties

The fully optimized equilibrium lattice constants of PtTe<sub>2</sub> for two approximations compared with experimental data are listed in Table 4.13. We observe that the calculated results by optB86-vdW are  $a_0 = 4.05$  Å,  $c_0 = 5.11$  Å and  $V_0 = 72.04$  Å<sup>3</sup>, which are agree with the experimental  $a_0 = 4.01$  Å,  $c_0 = 5.20$  Å and  $V_0 = 72.43$  Å<sup>3</sup> [145]. Also the calculated lattice parameters for a bilayer are same to the results by previous study. On the other hand, we set  $c = 15 \text{\AA}$  as a vacuum layer for bilayer and monolayer which is make the vad der Waal's force between the layers to be weak. The investigation of the phase stabilities for bulk, bilayer and monolayer, were done using the cohesive and formation energies as defined in Chapter 3, using Equation (3.2.1) and (3.2.2) respectively. Our calculated cohesive and formation energies are listed in Table 4.13 per atom for bulk, bilayer and monolayer, and compared with the available previous study. Formation and cohesive energies are negative, indicating these structures are energetically stable. the PtTe<sub>2</sub> structures are exothermic, suggesting that structures can be formed from their constituent atoms [146]. The a and c lattice parameters, the in-layer structural parameters, show the least variation across the different approximations. The inter-layer spacing, defined by the c lattice parameter, show the most variation. We note that optB86-vdW gives the best equilibrium structural parameters for PtTe<sub>2</sub> when compared to experiment.

Table 4.13:	Calculated, e	experimer	ntal and	theoretical	optimized	lattice cons	stants of
bulk bilayer	and monolaye	r PtTe <sub>2</sub> ,	cohesive	$(E_{coh})$ and	d formation	formation	energies
per atom, and	d inter-layer d	istance.					

		a (Å)	c (Å)	$V_o$ (Å <sup>3</sup> )	$E_{coh}$ (eV)	$E_{form}$ (eV)
Bulk	PBE	4.00	4.89	66.9	-4.43	-0.40
	optB86b-vdW	4.05	5.11	72.04	-3.24	-0.37
	$\mathrm{Exp}^{[45, \ 38, \ 39]}$	4.02	5.22	73.29	_	_
	$\operatorname{Exp.}[145]$	4.01	5.20	72.43	_	_
Bilayer	PBE	4.08	15	-	-3.80	-0.37
	optB86b-vdW	4.09	15	-	-2.93	-0.84
Monolayer	PBE	4.05	15	—	-3.80	-0.36
	optB86-vdW	4.04	15	-	-2.74	-0.66
	Previous work <sup>[123]</sup>	4.02	_	_	_	-0.32

#### 4.4.2 Mechanical stability

The calculations mechanical properties are exam for the elastic stability of materials. The obtained elastic constants are listed in Table 4.14, accordance with the Born stability criteria [102] see section (3.3.1), which confirm that the bulk, bilayer and a monolayer PtTe<sub>2</sub> are mechanically stable. Further, we investigated Young's moduli (Y) and Poisson's ratio ( $\nu$ ) to test the stiffness and bonding nature of the materials. In Table 4.15, we present the computed Young's moduli (Y) and Poisson's ratio ( $\nu$ ) for bulk, bilayer and monolayer PtTe<sub>2</sub> compared to an available previous study [41], and bulk moduli and shear moduli for bulk PtTe<sub>2</sub>. As we mentioned previously of Young's moduli decreasing with when the number of layer decrease, indicative of increased resistance to deformation under the application of opposing forces as the number of layers is increased. While, the Poisson's ratio values looks the same for all bulk, bilayer and monolayer. The values of the Young's moduli in Table 4.7 shows that the bulk is more resist to deformation than monolayer and bilayer, also the bilayer more resist than monolayer.

**Table 4.14:** Elastic constants  $(C_{ij}$  (GPa)), for bulk, bilayer and monolayer PtTe<sub>2</sub>.

		$C_{11}$	$C_{12}$	$C_{13}$	$C_{33}$	$C_{66}$
Bulk	optB86b-vdW	169.33	52.83	42.16	69.22	58.25
Bilayer	PBE	85.36	21.74	—	_	—
Monolayer	PBE	64.61	22.89	—	_	—
Monolayer	Other work <sup>[41]</sup>	58.62	32.90	_	_	_

**Table 4.15:** The obtained Bulk moduli (B) Shear moduli (G), Young's moduli (Y) and Poisson's ratio ( $\nu$ ) in GPa, for bulk, bilayer and monolayer, and the other theoretical study.

		B	Y	G	ν
Bulk	optB86b-vdW	68.69	103.84	41.60	0.25
Bilayer	PBE	_	79.82	_	0.25
Monolayer	PBE	_	59.64	_	0.29
Monolayer	Other work <sup>[41]</sup>	_	40.15	_	0.35

#### 4.4.3 Dynamical stability

The phonon dispersion relations were calculated along with the high symmetry directions. Figure 4.47(a-c) depicted the phonon band structure, for bulk, bilayer and



**Figure 4.47:** The band structure of phonon dispersion for PtTe<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.



**Figure 4.48:** TDOS and atomic contributions to acoustic and optical modes of phonon dispersion for PtTe<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.

monolayer PtTe<sub>2</sub>. The phonon frequencies range is 0-5.4 THz, 0-5.0 THz and 0-5.2 THz for bulk, bilayer and monolayer, respectively. Figure 4.48(a-c) show the total and partial density of states, and explain the atomic contribution to the total phonon density, to the acoustic and optical mode for bulk, bilayer and monolayer. All the phonon frequencies are positive, which is suggest that the bulk, bilayer and monolayer of PtTe<sub>2</sub> are dynamically stable. Also, we observed the same phonon band structure dense of the bilayer PtTe<sub>2</sub> as in bilayer for PtO<sub>2</sub>, PtS<sub>2</sub> and PtSe<sub>2</sub>. From the plots, we can confirm that the most contribution of (Pt) atoms are in acoustic mode and (Te) atoms are in optical mode.



Figure 4.49: Calculated band structure of PtTe<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.

#### 4.4.4 Electronic structure properties

In Figure 4.49(a-c) and Figure 4.50(a-c), we show the electronic band structure, total and partial density of states of the bulk, bilayer and monolayer PtTe<sub>2</sub>, respectively. The electronic structure investigations proved that the bulk phase of both compounds have a semi-metal behavior, hence the bilayer and monolayer are semiconducting with an indirect band gap in both compounds. The minima of the conduction are located at  $\Gamma$ , while the maxima of the valance band between A and L points, almost the same of  $PtO_2$ , of the Brillouin zone. The obtained density of states (total and partial) was done to know the orbital contributions to the gap edge. We found that a semi-metal behaviour for bulk through the density of states plot, but the bilayer and monolayer are semiconductors with gap edge determine by Te(p) in top of the valence band and hybridization of Pt(d) and Te(p) in the minimum conduction band. The bilayer band structure exhibits the same behavior of a bilayer for other compounds. In Table 4.16, we listed the band gap values for bulk, bilayer and monolayer for PtTe<sub>2</sub>. Our calculated results agreed with some of the previous studies [26, 50, 48]. We find that the band gaps decrease with the increasing number of layers as it was previously reported by Xu M et al. [140]. The obtained results of band gap for bilayer and monolayer were consistent to photovoltaic solar cell applications.



**Figure 4.50:** Calculated total and partial DOS of PtTe<sub>2</sub>. (a) Bulk (b) Bilayer (c) Monolayer.

Table 4.16: The calculated band gaps values compared to the experimental and the-oretical (in eV) of  $PtTe_2$ .

	optB86-vdW	PBE	$GW_0$	Exp.	Other calculations
Bulk	semimetal	semimetal	—	semimetal <sup>[29]</sup>	_
Bilayer	0.33	0.43			
Monolayer	0.63	0.80	$3.90, 2.03^{[123]}$	—	$0.75^{[123]}, 0.61^{[42]}, 0.38^{[52]},$
					$0.70^{[f135]}, \! 0.79^{[f130]}$



**Figure 4.51:** GW<sub>0</sub> BSE results (a) imaginary part  $\varepsilon_2(\omega)$ , (b) real part  $\varepsilon_1(\omega)$  of dielectric function and (c) absorbance for bulk, bilayer and monolayer of PtTe<sub>2</sub>.

#### 4.4.5 Optical properties

The imaginary and real parts of the dielectric functions, and the absorbance of bulk, a single layer of the bilayer and a monolayer  $PtTe_2$ , were calculated and plotted in Figure 4.51(a-c). The maximum absorbance in in-plane polarization for monolayer is  $\approx 35.27\%$  at 1.33 eV and for bilayer is  $\approx 26.75\%$  at 1.45 eV and 6.32% at 1.65 eV for bulk. The absorbance of a monolayer is considerably greater than the absorbance for a bilayer and bulk. This agrees with MoS<sub>2</sub>, MoSe<sub>2</sub> and WS<sub>2</sub> results (5–10%) [115, 116], where the single layer absorbance is high in monolayer than bilayer and bulk. Moreover, the out-of-plane polarisation, the maximum absorbance is  $\approx 0.15\%$  at 2.30 eV for monolayer and  $\approx 6.04\%$  at 2.36 eV for bilayer and 5.20% at 1.88 eV for bulk. The Tauc plot [117], was used to obtain the optical band gap. For the bulk PtTe<sub>2</sub>, the in-plane and out-of-plane optical band gap polarizations are 0.03 and 0.00 eV, respectively, which is confirmed the experimental measurements. The calculated optical band gaps of the in-plane and out-of-plane polarization, for the monolayer, are 1.00 and 1.50 eV, and for bilayer are 0.37 and 0.92 eV, respectively. Therefore, the obtained values of the monolayer and bilayer can be use for photovoltaic solar cells applications [142, 143, 144].

#### 4.4.6 Lattice thermal conductivity

In Figure 4.52(a) and (b), we illustrate the lattice thermal conductivity vs temperature and frequency, respectively, for a single layer of bulk, bilayer and monolayer PtTe<sub>2</sub> structure. The average lattice thermal conductivity at 300 K for single layer in bulk, bilayer and monolayer is  $0.33 \times 10^{-8}$ ,  $0.12 \times 10^{-8}$  and  $0.07 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> in-plane direction for a single layer in bulk, bilayer and monolayer respectively, and  $0.08 \times 10^{-8}$ Wm<sup>-1</sup>K<sup>-1</sup> out-of-plane for bulk while the out-of-plane for bilayer and monolayer are zero. The lattice thermal conductivity value for bulk decreases by about ~64% of the bilayer and ~79% of the monolayer, in the in-plane. Further, the high in-plane value of lattice thermal conductivity per single layer was found to be in the low-temperature range is  $2.58 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 20 K for bulk, and  $0.95 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 20 K for bilayer and  $0.52 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 30 K for monolayer. The high out-of-plane is  $0.60 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> at 20 K for single layer bulk. The lattice thermal conductivity against frequency at 300 K is presented in Figure 4.52(b), and its cumulative lattice thermal conductivity as a function of the frequency of single layer for bulk, bilayer and monolayer. We observed that the lattice thermal conductivity is highly anisotropic,



Figure 4.52: Lattice thermal conductivity per layer for  $PtTe_2$ , (a) lattice thermal conductivity against temperature, (b) cumulative lattice thermal conductivity against frequency.

with the thermal conductivity in-plane of the layers being much higher than in the out-of-plane direction for two cases bulk, bilayer and monolayer. The all lattice thermal conductivity values for a single layer in bulk, bilayer and monolayer PtTe<sub>2</sub>, are suits for thermoelectric application

Furthermore, we computed the directional projected density of states for each atom as a function of frequency. The in-plane and out-of-plane contributions are shown in Figure 4.53 left and right, respectively, which are along [100] and [001]. The results appears the similarity of directional projected density of states for other compounds. To perceive the contribution ratio of phonon to lattice thermal conductivity for bulk, bilayer and monolayer  $PtTe_2$ , we compute the contribution of acoustic and optical phonons modes. The contribution estimated to the thermal conductivity from the acoustic modes at 300 K. We obtained that the in-plane acoustic mode total contribution is 86.22%, 83.33% and 92.30% for bulk, bilayer and monolayer  $PtTe_2$  respectively. While the out-of-plane 64.29% for bulk, and 0% for bilayer and monolayer. The contributions of phonon to lattice thermal conductivity per atoms are illustrated in Figure 4.54 (left and right), for bulk, bilayer and monolayer. Through Figure 4.54, we can note that the ratio of contribution is almost the same in in-plane, for bulk, bilayer and monolayer. Also in the right, we have out-of-plane, which is for bulk. This is in clear contrast to the conventional understanding, especially in the out-of-plane direction, that the acoustic



Figure 4.53: Directional projected density of states, left is in-plane and right is outof-plane for bulk, bilayer and monolayer  $PtTe_2$  as function of frequency.



Figure 4.54: Contribution ratio of phonon to lattice thermal conductivity, left is inplane and right is out-of-plane for bulk and monolayer  $PtTe_2$  as function of frequency. (Recall there is no contribution in out-of-plane for monolayer).

modes control thermal conductivity [127].

#### Phonon lifetime

The third-order force constants [90, 95], were used to obtain the phonon lifetime. The phonon lifetime at 300 K for bulk, bilayer and monolayer  $PtTe_2$ , as a function of frequency, as depicted in Figure 4.55(a-c). The highest peak for phonon lifetime is located in acoustic mode, and while the lowest peak for phonon lifetime is located in optical mode for all structures. This is in accordance with a slightly strong scattering in the high frequency optical phonon modes. The phonon lifetime distribution of acoustic and optical phonon mode can be used to differentiate the phonon lifetime contributions to the total lattice thermal conductivity [128].



**Figure 4.55:** Phonon lifetime against frequency at 300 K for PtTe<sub>2</sub>. (a) Bulk, (b) bilayer and (c) monolayer.



Figure 4.56: Average directional phonon group velocities against frequency for PtTe<sub>2</sub>. (a) Bulk, (b) bilayer and (c) monolayer.

#### Group velocity

The investigations of group velocity was described according to Equation (2.5.10). In Figure 4.56(a-c) we plot the average of group velocity. The in-plane group velocity is higher than out-of-plane in the low frequency range, while at high frequency the in-plane and out-of-plane are small compared to the low frequency values. The anisotropy in group velocity has a big impact on the lattice thermal conductivity [129]. The similarity of the distribution for in-plane group velocities of bulk and monolayer. In contrast, the out-of-plane group velocities is 13 Å.THz for bulk, while it is 0 Å.THz for bilayer and monolayer. The combined effect of the frequency dependence of the phonon lifetimes and group velocities are consistent with the anisotropy in the thermal conductivity as well as the large contribution to the total thermal conductivity form the low frequency phonons.

#### 4.4.7 Transport properties of PtTe<sub>2</sub>

Figure 4.57 shows the calculated Seebeck coefficients for a single layer in bulk, bilayer and monolayer  $PtTe_2$ , between 200 K and 800 K temperature range. The Seebeck coefficient for the bulk have negative values for all charge carriers concentration, which explain that the bulk can be a good n-type material. Possibly because the bulk have metallic behaviour so the majority of carriers should be electrons. From the plot, we can observe that the Seebeck coefficients are increases according to increase of the temperature.



Figure 4.57: Seebeck coefficients of bulk, bilayer and monolayer PtTe<sub>2</sub>.

Figure 4.58, presents the electrical conductivity for a single layer in bulk, bilayer and monolayer PtTe<sub>2</sub> in the temperature range of 200 K to 800 K. The highest values were found to be at 200 K for all structures, which are  $7.9 \times 10^{-4}$  S/m for bulk,  $4.4 \times 10^{-4}$  S/m for bilayer and  $1.5 \times 10^{-4}$  S/m for monolayer, which are associated with by electron carriers whose concentration is  $10^{20}$  cm<sup>-3</sup> for a single layer in bulk, bilayer and monolayer. For all concentration of carriers, the electrical conductivity decreases with an increase in temperature. This indicates that an increase in temperature results in a decrease in electrical conductivity, due to their inverse relationship, and it is converse to what was noted in Figure 4.57 for the case of Seebeck coefficient. This is also observed in the preceding binary compounds.

The obtained electronic contribution to thermal conductivity for a single layer in bulk, bilayer and monolayer  $PtTe_2$  in the temperature range of 200 K to 800 K is provided in Figure 4.58. To understand how the total thermal conductivity is affected by electronic contribution. Figure 4.59 shows the maximum values, at a low temperature of 200 K for bulk, bilayer and monolayer, while, the lowest values are found to be at high temperature range. Also, the behavior of bilayer and monolayer kook the same, since



**Figure 4.58:** Electrical conductivity for a single layer in bulk, bilayer and monolayer PtTe<sub>2</sub>.

the high concentration for each of electrons and holes has a high value of the electronic contribution, reverse to the low concentration. However, the highest values are determined when the majority are electrons whose carrier concentrations is  $10^{20}$  cm<sup>-3</sup>. The obtained results show the lowest electronic contribution is provided by the monolayer structure, whereas the highest is by bulk structure.



Figure 4.59: Electronic contribution to thermal conductivity for a single layer in bulk, bilayer and monolayer  $PtTe_2$ .

The calculated power factor for a single layer in bulk, bilayer, and monolayer  $PtTe_2$  in the temperature range of 200 K to 800 K, were plotted in Figure 4.60. The highest and lowest values of power factor was found at low temperature of 200 K. The behavior of power factor curvature for bilayer and monolayer looks the same since the charge carriers concentration of  $10^{19}$  cm<sup>-3</sup> for each of electrons and holes have given high values at low temperature, while the low values were reported for charge carrier concentration of  $10^{20}$  cm<sup>-3</sup> for each of them. Contrarily, the behavior of the bulk system seemed different.

The dimensionless figure of merit (ZT) was calculated from 200 K to 800 K, and the greatest values for a single layer in the bulk, bilayer and monolayer  $PtTe_2$  are attained



Figure 4.60: Power factor for a single layer in bulk, bilayer and monolayer PtTe<sub>2</sub>.

at 800 K. The obtained ZT values are, 0.08 at 600 K for bulk, 0.37 at 700 K for bilayer and 0.51 at 600 K for monolayer, as depicted in Figure 4.61. The high values of ZT were dominated by holes carrier of  $10^{20}$  cm<sup>-3</sup> for bulk and by electrons carriers of  $10^{19}$  cm<sup>-3</sup> for bilayer and monolayer. The results indicates that a monolayer have higher ZT than bilayer and bulk. Also, the figure of merit values for all the structures increases with increasing temperature, since, the lowest values are at low temperature.



Figure 4.61: Figure of merit for bulk, bilayer and monolayer PtTe<sub>2</sub>.

# $\left[5\right]$

# **Summary and Conclusion**

# 5.1 Summary

In this section we summarize the results of our calculations for the PtX<sub>2</sub> ( $\alpha$ -PtO<sub>2</sub>, PtS<sub>2</sub>, PtSe<sub>2</sub> and PtTe<sub>2</sub>) compounds examined in this thesis. All compounds were structurally relaxed to configurations that are mechanically and dynamically stable. Table 5.1, presents the calculated DFT and BSE-optical (in-plane and out-of-plane) band gap values for the PtX<sub>2</sub> compounds. We note that  $\alpha$ -PtO<sub>2</sub> has the widest band gap (DFT and optical) compared to other compounds. Also, the band gap values increases from bulk to bilayer to monolayer, which suggests that a degree of band gap engineering is possible for these compounds. The obtained optical band gap values in the 0.3 - 2.75 eV range for PtX<sub>2</sub> structures, so the values between 1.0 to 1.7 eV are suitable for photovoltaics cell applications, while the values less than 1.0 and high than 1.7 are suitable for lower and top layers of the tandem solar cell, respectively [142, 143, 144].

**Table 5.1:** Our calculated, DFT and BSE-optical gap (in-plane (in) and out-of-plane (out) ) band gaps (in eV) for the bulk, bilayer and monolayer of  $PtX_2$ .

	Bulk			Bilayer			Monolayer					
Compound	ind ont P PPF BSE ont P PPF		PBF BSE		ontB	optB PBF		SE				
	орты	TDL	in	out	optb	FDE -	in	out	optD		in	out
α-PtO <sub>2</sub>	1.61	1.63	1.66	1.77	1.63	1.74	1.89	2.34	1.72	1.86	2.32	2.75
$PtS_2$	0.81	1.06	1.09	1.36	1.13	1.26	1.61	1.73	1.67	1.80	1.95	2.30
$PtSe_2$	semimetal	semimetal	0.10	0.3	0.93	0.93	1.10	1.25	1.38	1.38	1.43	1.64
PtTe <sub>2</sub>	semimetal	semimetal	0.03	0.00	0.33	0.43	0.37	0.92	0.63	0.80	1.00	1.50

In Table 5.2, we listed the results for the maximum absorbance in the range from 1-3 eV. The PtX<sub>2</sub> structures exhibited values ranging from 0.9 for bulk  $\alpha$ -PtO<sub>2</sub> up to 35 for monolayer PtTe<sub>2</sub>. Hence, the monolayers absorbance has the highest values among the others, also it increases from  $\alpha$ -PtO<sub>2</sub> to PtTe<sub>2</sub> compound. Moreover, the absorbance is dependent on the thickness of the material, which is the reason for the high values for monolayer, since it is thickness is a single layer thick. The monolayer PtTe<sub>2</sub> show the highest absorbance compared to others.

**Table 5.2:** The calculated maximum absorbance of in-plane, in the visible photon energy range for bulk, and a single layer of bilayer and monolayer  $PtX_2$ .

Compound	Bu	lk	Bila	yer	Monolayer		
Compound	absorbance % Energy (e		absorbance $\%$	Energy $(eV)$	absorbance $\%$	Energy $(eV)$	
α-PtO <sub>2</sub>	0.91	2.12	5.64	2.51	8.06	2.92	
$PtS_2$	2.00	2.90	7.64	1.83	13.15	2.51	
$PtSe_2$	25.04	1.95	26.89	1.51	31.05	2.06	
PtTe <sub>2</sub>	6.32	1.65	26.75	1.45	35.27	1.33	

The in-plane average lattice thermal conductivity per layer for PtX<sub>2</sub> compounds are shown in Table 5.3. Hence, our calculated values of the in-plane average lattice thermal conductivity for PtX<sub>2</sub> compounds per layer are in range from  $0.07 \times 10^{-8}$  for monolayer PtTe<sub>2</sub> to  $8.47 \times 10^{-8}$  Wm<sup>-1</sup>K<sup>-1</sup> for bulk  $\alpha$ -PtO<sub>2</sub> at room temperature. The results are given per layer for ease of comparison, see Section (3.6) for details. The low values of the lattice thermal conductivity is considered to be promising for the thermoelectric figures of merit. In our results, the lowest lattice thermal were found for the monolayers, PtTe<sub>2</sub> monolayer has lowest value of all the compounds investigated.

Compound	$\kappa_L \times 10^{-8}$ (Bulk)	$\kappa_L \times 10^{-8}$ (Bilayer)	$\kappa_L \times 10^{-8}$ (Monolayer)
$\alpha$ -PtO <sub>2</sub>	8.47	4.59	1.06
$PtS_2$	2.30	1.16	0.15
$PtSe_2$	0.47	0.24	0.11
PtTe <sub>2</sub>	0.33	0.12	0.07

Table 5.3: Lattice thermal conductivity (in  $Wm^{-1}K^{-1}$ ) for a single  $PtX_2$  layer.

Thermoelectric figures of merit (ZT) for the PtX<sub>2</sub> compounds are shown in Table 5.4. For comparison, we stated the highest values of ZT at a certain temperature, besides that, we observed how the ZT appears in various temperature. Our obtained ZT is between 0.04 at 200 K for bulk PtS<sub>2</sub> to 0.74 at 300 K for monolayer  $\alpha$ -PtO<sub>2</sub>, which it looks small ZT values for the bulk system. It is clear, that the monolayer for each compound possesses a high ZT value. Besides that, also the highest monolayer ZT value at 300 K, was found to be that of monolayer  $\alpha$ -PtO<sub>2</sub>, which is close to unity. Even though the thermal conductivity has a low value, unfortunately, the power factor was small for all PtX<sub>2</sub> compounds. Since the ZT of monolayer  $\alpha$ -PtO<sub>2</sub> has a value that is close to unity. Hence, it can be suitable for thermoelectric applications as n-type since it is due to the electrons charge carrier, as compared to the bulk system. The ZT of others system are low, for thermoelectric applications as it is unless strategies to improve ZT via reduction of lattice component i.e through straining or nanostructuring are implemented.

**Table 5.4:** The in-plane highest figure of merit (ZT) at a various temperature regimes of bulk, bilayer and monolayer  $PtX_2$ .

Compound	Bulk		Bilayer		Monolayer	
	ZT	Temperature (K)	ZT	Temperature (K)	ZT	Temperature(K)
$\alpha$ -PtO <sub>2</sub>	0.11	700	0.62	400	0.74	300
$PtS_2$	0.04	200	0.12	500	0.18	500
$PtSe_2$	0.16	500	0.35	600	0.46	500
PtTe <sub>2</sub>	0.08	600	0.37	700	0.51	600

### 5.2 Conclusion

First-principles calculations were used to investigate the structural, mechanical, dynamical stabilities, optical and thermoelectric properties of the trigonal PtX<sub>2</sub> (X=O, S, Se and Te), to get some insights about their applications as a thermoelectric or photovoltaic materials. This was carried out using density functional theory and many-body perturbation theory. All calculations were performed using the Vienna *ab-initio* Simulation Package (VASP) in conjunction with the PHONOPY, PHONO3PY and BoltzTraP2 packages. Mostly, the results are in agreement with available experimental and theoretical data. Since these  $PtX_2$  compounds have potential device applications, we opted to summarise our results and discuss potential applications separately as provided below. We hope that our predicted results will provide a better theoretical understanding of the rich properties of these materials, as extensively captured in this work.

The study of structural properties shows that the compounds, at their minimum energy configurations, are mechanically and dynamically stable. While, through the DFT and optical band gap, the monolayer of  $PtX_2$  compounds show that the values of band gap are good for photovoltaic and tandem solar cell application [142, 143, 144]. However,

the absorbance results depict that the monolayer  $PtTe_2$  possesses a high percentage of radiation absorption. Furthermore, we investigated the in-plane average lattice thermal conductivity for  $PtX_2$  compounds per layer, in order to calculate the transport coefficients, which was encourage by the low values average lattice thermal conductivity. Unfortunately, the calculation of the in-plane transport show low values for the power factor for all  $PtX_2$  structures. That was the main reason for the low values of the obtained thermoelectric figure of merit ZT.

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