APPENDIX A

2ND-ORDER CURRENT IMPULSE CIRCUIT

A lightning impulse combination generator available at the University of the Witwatersrand (Melaia, 1993), may be configured for <u>current mode</u> only (refer to Figure A1).



Figure A1: 2nd-order impulse circuit (combination generator in <u>current mode</u>)

In the charging loop a dc voltage source V_s charges the charging capacitor C_c via series resistor R_c . In the discharging loop, C_c is discharged via switch *S* into resistor R_m , inductor L_r and the device-under-test (DUT).

The waveform parameters (e.g. $8/20 \ \mu s$) are defined under <u>short-circuit</u> conditions i.e. DUT replaced by a shunt. Therefore the discharging loop comprises a 2nd-order RLC circuit described by:

$$\frac{d^2i}{dt^2} + 2\alpha \frac{di}{dt} + \omega_n^2 i = 0$$
(A1)

where

$$\alpha = \frac{R_m}{2L_r} \qquad \qquad \omega_n = \frac{1}{\sqrt{L_r C_c}}$$

For an <u>under-damped</u> circuit, $\alpha < \omega_n$ and:

$$\frac{i(t)}{I} = k \exp(-\alpha t) \sin(\omega_d t)$$
(A2)

where

$$k = \frac{\exp(\alpha t_{peak})}{\sin(\omega_d t_{peak})} \qquad \qquad \omega_d = \sqrt{\omega_n^2 - \alpha^2} \qquad \qquad t_{peak} = \frac{\tan^{-1}(\omega_d / \alpha)}{\omega_d}$$

For a <u>critically damped</u> circuit, $\alpha = \omega_n$ and:

$$\frac{i(t)}{I} = k t \exp(-\alpha t)$$
(A3)

where

$$k = \frac{\exp(\alpha t_{peak})}{t_{peak}} \qquad t_{peak} = \frac{1}{\alpha}$$

For an <u>over-damped</u> circuit, $\alpha > \omega_n$ and:

$$\frac{i(t)}{I} = k(\exp(s_1 t) - \exp(s_2 t))$$
(A4)

where

$$s_{1} = -\alpha - \sqrt{\alpha^{2} - \omega_{n}^{2}} \qquad k = \{ \exp(s_{1}t_{peak}) - \exp(s_{2}t_{peak}) \}^{-1} \qquad t_{peak} = \frac{\ln(s_{1}/s_{2})}{s_{2} - s_{1}}$$

By plotting the resulting equations (A2, A3 and A4) in Microsoft® Excel (or similar package), α and ω_n are adjusted through a number of iterations until the 0.1, 0.9 and 0.5 criteria are met satisfactorily by one of the equations.

APPENDIX B

DERIVING R_{sys} & L_{sys}

Consider the combination generator in current mode, as per Appendix A, but where R_m and L_r have been replaced by a shunt, and the device-under-test (DUT) has also been replaced by a shunt. The resulting circuit is shown in Figure B1, where R_{sys} and L_{sys} are the lumped system resistance and inductance respectively in the discharging loop.



Figure B1: Impulse generator (Figure A1) with R_m , L_r and DUT replaced by shunts

The discharging loop comprises an under-damped 2nd-order RLC circuit, producing a waveform shown in Figure B2 and described by:

$$\frac{i(t)}{I} = k \exp(-\alpha t) \sin(\omega_d t)$$
(B1)

where

$$k = \frac{\exp(\alpha t_{peak})}{\sin(\omega_d t_{peak})} \qquad \qquad \omega_d = \sqrt{\omega_n^2 - \alpha^2} \qquad \qquad t_{peak} = \frac{\tan^{-1}(\omega_d / \alpha)}{\omega_d}$$

and

$$\alpha = \frac{R_{sys}}{2L_{sys}} \qquad \qquad \omega_n = \frac{1}{\sqrt{L_{sys}C_c}}$$



Figure B2: Under-damped current waveform

Because C_c is known, R_{sys} and L_{sys} may be calculated once values for α and ω_d have been derived from the recorded waveform. Yet in practice the exact origin of the waveform on the oscilloscope trace is seldom known (also due to noise), hence the absolute values of t_1 , t_2 , t_3 and t_4 are unknown. But their relative positions e.g. $t_2 - t_1$ can easily be deduced from the recorded waveform, using the oscilloscope cursor function, provided the waveform is sufficiently underdamped such that the peaks and zeros are easily discernible. Similarly the ratio $i(t_1) : i(t_3)$ can easily be deduced and calculated using the oscilloscope cursor function.

Therefore, according to equation (B1), i(t) = 0 when $sin(\omega_d t) = 0$ i.e. when $\omega_d t = 0$, π , 2π , ... etc., and from Figure B2, $\omega_d t_2 = \pi$ and $\omega_d t_4 = 2\pi$. Therefore:

$$\omega_d = \frac{\pi}{t_4 - t_2} \tag{B2}$$

Also from Figure B2 and equation (B1):

$$\frac{i(t_1)}{I} = k \exp(-\alpha t_1) \sin(\omega_d t_1)$$
(B3)

and

$$\frac{i(t_3)}{I} = k \exp(-\alpha t_3) \sin(\omega_d t_3)$$
(B4)

Dividing equation (B3) by (B4), and solving for α yields:

$$\alpha = \frac{\ln\left(\frac{i(t_1)\sin(\omega_d t_3)}{i(t_3)\sin(\omega_d t_1)}\right)}{t_3 - t_1}$$
(B5)

But the peaks of the curve in Figure B2 occur when the derivative of equation (B1) is zero, as follows:

$$\frac{d}{dt}\left(\frac{i(t)}{I}\right) = k \exp(-\alpha t) \left[\omega_d \cos(\omega_d t) - \alpha \sin(\omega_d t)\right] = 0$$

This holds when $\tan(\omega_d t) = \omega_d / \alpha$ yielding $\omega_d t = \tan^{-1}(\omega_d / \alpha)$, $\pi + \tan^{-1}(\omega_d / \alpha)$, ... etc. Therefore from Figure B2, $\omega_d t_1 = \tan^{-1}(\omega_d / \alpha)$ and $\omega_d t_3 = \pi + \tan^{-1}(\omega_d / \alpha) = \pi + \omega_d t_1$. Hence:

$$\frac{\sin(\omega_d t_3)}{\sin(\omega_d t_1)} = \frac{\sin(\pi + \omega_d t_1)}{\sin(\omega_d t_1)} = -1$$

and equation (B5) reduces to:

$$\alpha = \frac{\ln\left(\frac{i(t_1)}{-i(t_3)}\right)}{t_3 - t_1} \tag{B6}$$

Therefore once ω_d and α have been calculated from the recorded waveform as per equations (B2) and (B6), ω_n , R_{sys} and L_{sys} may be calculated.

APPENDIX C

R_{stray} & L_{stray} DATA PER CAPACITOR CONFIGURATION

See overleaf.

			Suray		suruy																
	Rshunt =	= 0.001	ohm																		
	Lobust -	0.16																			
	LSHUIT -	0.15	un																		
Cc =	8 47	υE																			
hander	14-		147	44	47-1-1-	0	1	Deterror	1				-								
impuise	vs	1	1/05	17wn	i/aipna	risys	LSYS	resulay	LSU ay												
No.	(k∨)	(kA)	(kA/kV)	(us)	(us)	(ohm)	(uH)	(ohm)	(uH)												
1	1.055	1 480	1.40	5.40	82.43	0.0835	3.44	0.0825	3 29												
	0.004	0.000		5.10	00.10	0.0005	0.11	0.00005	0.00		Lve Ve	γ = 1.5239	X		Detray ve 1			Le:	raw word		
2	2.004	2.820	1.41	5.40	82.42	0.0835	3.44	0.0825	3.29		1 00. 00	n ² - 0 000	2		v=	-0.01061 p(x) + 0.0918	3	La	1 ay vs. 1	0.0736Ln(v	+ 3 348
3	3.007	4.360	1.45	5.37	82.38	0.0826	3.40	0.0816	3.25			H ⁻ = 0.999	2		3 -	-0.010001(0) + 0.0010	^		y	0.07 JOLII(A	1 + 5.540.
	4.000	E 000	1.40	E 27	05 00	0.0702	2.40	0.0792	2.05	35			0.11	-		R ² = 0.7751	3.70 -			R ² = 0.77	'81
4	4.020	5.000	1.40	0.37	00.00	0.0793	3.40	0.0703	3.23				0.11	1			0.10				
5	5.040	7.480	1.48	5.27	88.98	0.0737	3.28	0.0727	3.13	30			0.10	1			3.60 +				
6	6.040	8 900	1.47	5.31	113.90	0.0584	3 33	0.0574	3.18	25				1			3.50				
7	7.000	40.500	1.40	5.04	00.00	0.0074	0.00	0.0004	0.10	-			0.09	1			0.00				
/	7.030	10.500	1.49	5.31	99.20	0.0671	3.33	0.0661	3.18	20	1		0.08	+ + +			3.40 -	1			
8	8.020	12.100	1.51	5.34	91.33	0.0737	3.37	0.0727	3.22	15			0.00		× .		3.30 -				
q	10.030	15 100	1.51	5.31	106.05	0.0628	3 33	0.0618	3.18	10			0.07				3 20 4				
3	10.030	10.100	1.01	0.01	100.00	0.0020	3.33	0.0010	3.10	10			0.00				3.20 T			-	
10	12.080	18.300	1.51	5.28	107.02	0.0615	3.29	0.0605	3.14	5			0.06		¥		3.10				
11	14 030	21.400	1.53	5.28	116.24	0.0566	3.29	0.0556	3.14	0			1 0.05			1	3 00 4				
40	40.040	24,000	4.54	6.20	444.04	0.0007	0.20	0.0007	0.14					0 0 4 6	0 40 40 44 46 40	20 22 24 26 28 20	0.001				
12	16.010	24.600	1.54	5.25	114.81	0.0567	3.25	0.0557	3.10	0 2 4	6 8 10 1	2 14 16 18 20	II.	0 2 4 0	0 10 12 14 10 10	20 22 24 26 26 30		1 2 4 6 8 10 1.	14 16 18	20 22 24 2	6 28 30
13	17.980	27.800	1.55	5.21	105.57	0.0607	3.20	0.0597	3.05												
AVERAGE			1.49	5 32	98.16	0.0692	3 33	0.0692	3.18												
OTD DEL			0.05	0.02	40.10	0.0002	0.00	0.0002	0.07				_								
STUDEV			0.05	0.06	13.15	0.0106	0.07	0.0106	U.U/												
Co-	33.02	υE			1			1					-				-		-	-	
UC =	33.95	ur															_			1	
Impulse	Vs	1 1	I/Vs	1/wn	1/alpha	Rsys	Lsys	Rstray	Lstray		-		1			0.0F0F -0.908	1				
No.	(k\/)	(kA)	(kA/kV)	(us)	(us)	(ohm)	(uH)	(ohm)	(nH)		Ivs. Vs	y = 4.1648	× []		Rstray vs. I	y = 0.0565x ^{10.000}	· 🛛	Ls	ray vs. I		
1	0.525	2,000	2.01	7.07	70.00	0.0525	1.07	0.0530	1.70			R ² = 0 999	7 fl			$R^2 = 0.9431$	Н		- y = -	U.U428Ln(x	+ 1.742
1	0.525	2.000	3.81	1.9/	70.65	0.0530	1.87	0.0520	1.72				· (I			11 0.0401	н		-	$P^2 = 0.68$	276
2	1.003	4.000	3.99	7.81	100.93	0.0356	1.80	0.0346	1.65	100			0.06	1.			1.75 т			A = 0.00	
2	2,022	9,000	2.00	7 00	100.04	0.0000	1.02	0.0070	1 60				0.05	1				•			
J	2.022	0.000	3.50	7.00	120.04	0.0205	1.00	0.0275	1.00	80			1 0.05				1.70 -	1			
4	3.036	12.400	4.08	7.82	137.59	0.0262	1.80	0.0252	1.65									N.A.			
5	4 011	16.400	4 119	7.76	152.95	0.0232	1.77	0.0222	1.62				0.04	1			1.65				
0	5.000	20,000	4.40	7.70	450.00	0.0202	4.70	0.0245	4.04	60		/	0.04	- k			1.00 T		*		
6	5.000	20.800	4.16	1.13	156.66	0.0225	1.76	0.0215	1.61			-	0.03				1 4 00		Λ		
7	6.030	25.000	4.15	7.69	154.36	0.0226	1.74	0.0216	1.59	40			0.03				1.60 1		<u> </u>		
0	7.040	20.400	4 10	7 60	100.04	0.0200	1.74	0.0100	1.60		and the second s		0.00		-			1			
0	7.040	25.400	4.10	7.05	100.04	0.0205	1.74	0.0155	1.05	20			1 0.02				1.55				_
9	8.010	33.400	4.17	7.57	169.90	0.0199	1.69	0.0189	1.54				0.02					· · · · · · · · · · · · · · · · · · ·			
10	9 040	37,600	4 16	7 79	160.68	0.0223	1 79	0.0213	1.64	a second			0.01				1.50 -				
44	40.050	40.000	4.20	7.00	477.40	0.0405	4.70	0.0405	4.50	0				0 10 2	0 20 40 60	60 70 90		10 20 20	40 60	60 70	90
11	10.050	42.200	4.20	7.00	177.19	0.0195	1.73	0.0105	1.50	0 2 4	6 8 10 1	2 14 16 18 20		0 10 2	0 30 40 30	00 70 00	, °	10 20 30	40 50	00 70	00
AVERAGE			4.09	7.76	143.14	0.0268	1.78	0.0258	1.63												
STD DEV			0.12	0.11	32.38	0.0000	0.06	0.0000	0.05				_								
OID DEV			0.12	0.11	52.50	0.0000	0.00	0.0000	0.00											-	
Cc =	136.00	uF																			
Impulso	16		10.6	1 6	1/alaha	Down	Lan	Botrou	Lotrou												
mpuise	45		1/05	17 4411	naipira	nsys	LSYS	nsuay	LSUAY												
No.	(k∨)	(kA)	(kA/kV)	(us)	(us)	(ohm)	(uH)	(ohm)	(uH)							0.49					
1	0.407	3,300	8 11	14 77	154.55	0.0208	1.60	0.0198	1.45		Vs. Vs	y = 8.9531	х		Rstray vs. 1	γ = 0.0325× ^{-0.400}		le	raw ws I	y = 1.5	157 x 0.046
	0.000	£ 000	0.40	14.50	105.51	0.0107	1.55	0.0177	1.40			$P^2 = 0.99$	a li			p ² - 0.02		20	ay ion	n2	0.0100
4	0.605	5.000	0.42	14.52	105.51	0.0107	1.55	0.0177	1.40			11 0.000				R = 0.55				- M	0.9109
3	0.803	6.840	8.52	14.28	186.98	0.0160	1.50	0.0150	1.35	100 1			0.02	25 -			1.50 т				
4	1.007	8 700	8.64	14 35	187 23	0.0162	1.51	0.0152	1 36			_					1 1				
-	4,000	40,000	0.74	44.07	202.00	0.0400	4.50	0.0140	4.00	80			0.02	20			1.45 -	•			
5	1.202	10.500	0.74	14.27	233.90	0.0126	1.50	0.0110	1.35					· · · · ·				N			
6	1.602	14.100	8.80	14.08	259.38	0.0112	1.46	0.0102	1.31	60		/	0.04	6			1.40 +	1			
7	2.003	17 700	8.84	14.11	253.19	0.0116	1.46	0.0106	1.31		-	/	0.01				1 4 05	Ne.			
	2.000	21,400	0.00	14.05	210.02	0.0000	1.45	0.0000	1.00	40				o 🔊 🛰			1.35				
8	2.410	21.4UU	8.88	14.05	310.92	0.0093	1.45	0.0083	1.30	40			0.01	·			1 1 30				
9	2.803	25.000	8.92	14.12	280.41	0.0105	1.47	0.0095	1.32						· · · · · · · · · · · · · · · · · · ·		1 ···· T	and the second se			
10	3 206	28.600	8.92	13.99	325.58	0.0088	1.44	0.0078	1.29	20			0.00	15 1			1.25				
44	0.200	20.000	0.02	40.00	323.30	0.0000	4.40	0.0070	1.2.9				H				1				
11	3.605	32.200	8.93	13.96	327.19	0.0088	1.43	0.0078	1.28	0			0.00	1 00			1.20 +				
12	3.970	36.400	9.17	13.86	282.84	0.0100	1.41	0.0090	1.26	0 1 2	3 4 5	678910		0 10 3	20 30 40 50	60 70 80 90	0	10 20 30	40 50	50 70	80 90
AVEDACE			0.74	14.20	247 21	0.0129	1 49	0.0110	1 22	1		10	H				11	0 20 30	10 00		
AVERAGE			0.74	14.20	247.31	0.0129	1.40	0.0119	1.35												
STD DEV			0.28	0.26	61.65	0.0041	0.05	0.0041	0.05												
				1				I													
Ce -	100.20				-												-		-	-	
00=	102.30	ur .															-i			1	1
Impulse	Vs	1 1	I/Vs	1/wn	1/alpha	Rsys	Lsys	Rstray	Lstray			v = 7.877×	1				28				
No.	(k\/)	(kA)	(kA/k\)	(us)	(us)	(ohm)	(uH)	(ohm)	(uH)	1	I vs. Vs	y = 7.077X	1		Rstray vs. I	y = 0.03x ^{-0.00}		Ls	ray vs. I	0.04401	
1	0.511	2,700	7.22	10.05	101.01	0.0004	1.54	0.000	1.20	1		R ² = 0.9995	H			R ² = 0 8625	H		y = -	u.u418Ln(x)	+ 1.4349
1	0.514	3.760	1.52	12.55	131.61	0.0234	1.54	0.0224	1.39				11			1.0020	H			$R^2 = 0.87$	48
2	0.726	5.440	7.49	12.44	154.08	0.0196	1.51	0.0186	1.36	~			1 U.03	50]			1 30 1	1			
3	1.002	7.680	7.62	12.32	175.92	0.0162	1.48	0.0159	1.33	70			0.03	00 1			1.39	1			
J	1.000	7.000	7.02	12.32	175.55	0.0103	1.40	0.0108	1.33	60			1	60 N			1.37	1			
4	1.540	11.800	7.66	12.33	233.21	0.0127	1.49	0.0117	1.34	50			1 0.02	50 T			1.35	<u> </u>			
5	2 002	15,600	7 79	12 27	229.87	0.0128	1.47	0.0118	1.32		/		0.02	00			1 1 32	and a			
	2.002	40.000	7.00	40.07	240.07	0.0120	4.47	0.0110	1.32	40			1 0.00	50			1.05				
6	2.504	19.600	7.83	12.27	213.19	0.0138	1.47	0.0128	1.32	30	1				the second secon		1.31 +		<hr/>		
7	3.006	23.600	7.85	12.14	228.38	0.0126	1.44	0.0116	1.29	20	•		0.01	00		_	1.29	× 4	*		
8	3.506	27,602	7.87	12.09	216.51	0.0132	1.43	0.0122	1.28	1 10			0.00	50			1 1 27	¥			
0	3.000	27.000	7.00	12.00	210.01	0.0132	1.40	0.0122	1.20				1				1 1.4/			_	
9	4.003	31.600	7.89	12.21	252.10	0.0116	1.46	0.0106	1.31				1 0.00	00			1.25 +				
10	4.520	36.000	7.96	12.14	242.30	0.0119	1.44	0.0109	1.29	0 1 2	3456	7 8 9 10	1	0 10	20 30 40 5	0 60 70 80	0	0 10 20 30	40 50	60 7	0 80
AVEDACE			7.73	12.29	207.72	0.0140	1.47	0.0130	1.32	1			1				l I				
AVERAGE			1.73	12.20	201.12	0.0149	1.47	0.0139	1.32												
OTD DEL			• • • • • • • • •		11117	1.111139		a criticizio	11112												
STD DEV			0.20	0.14	40.17	0.0000	0.00	0.0005	0.03												

Table C1: R_{stray} & L_{stray} data per capacitor configuration

APPENDIX D

LOW RESISTANCE SHUNTS – MORE CONSIDERATIONS

Low resistance shunts may be constructed to achieve very low inductance, using an alternative conductor to Nichrome e.g. Copper, Aluminium or Iron; these shunts would typically be thin but broad to keep the inductance as low as possible – refer to Figure D1.



Figure D1: Low resistance shunt geometry

However Copper, Aluminium and Iron are wholly unsuitable conductors for the purposes of the very low inductance shunts i.e. l_{shunt} is excessive in all cases to achieve the associated resistance values required in this work. This is due to resistivity ρ that is too low, and a higher component mass *m* that is required to compensate for relatively high temperature coefficient α_T . Whilst Nichrome is superior in this regard i.e. l_{shunt} is much smaller in all cases, it is also unsuitable for the purposes of very low inductance shunts.

Graphite

A more appropriate material would allow a small component mass *m* such that its dimensions, particularly length l_{shunt} , are small. This would require high resistivity ρ , as well as low temperature coefficient α_T and/or high heat capacity *c*. An example of such material is graphite with the following properties:

 α_T = -0.0005 °C⁻¹ (Giancoli, 1984); *c* = 709 J/kg.°C (Counterman, 1997a); ρ = 3e-5 to 60e-5 Ω .m (Giancoli, 1984); *P* = 2260 kg/m³ (Counterman, 1997b).

Assuming a maximum permissible $\Delta R/R_0$ of 5%, Table D1 shows the resultant ΔT_{max} and hence the required graphite component mass per C_c . Table D2 shows the shunt lengths for each of the very low inductance components required.

	Table DT. Required (minimum) in for graphic										
Cc	V _{s,max}	ΔT_{max}	m								
(μF)	(kV)	(°C)	(kg)								
8.47	20		0.024								
33.93	20	100.0	0.096								
136.0	10		0.096								

Table D1: Required (minimum) *m* for graphite

Table D2: Required l_{shunt} and A_{shunt} for graphite

R (Ω)	l _{shunt} (m)	A _{shunt} (mm²)
0.035	0.05 – 0.22	853.3 – 190.8
0.335	0.15 – 0.69	275.8 – 61.7
0.487	0.19 – 0.83	228.8 – 51.2
0.650	0.21 – 0.96	198.0 – 44.3

Certainly these l_{shunt} values are workable, particularly the lower ones per range, although the performance of the graphite under high impulse current would need to be explored.

Immersion in high heat capacity fluid

An alternative solution is to reduce the length of the shunt, without reducing its (thermal) mass, by immersing it in a non-conducting tube¹ of distilled water or any other very low (electrical) conductivity fluid with high heat capacity – refer to Figure D2.

As before, closure of spark gap *S* will result in the energy stored in capacitor C_c dissipating as heat energy in R_m under short-circuit conditions. The worst case occurs for $V_{s,max}$:

¹ Square tubing would be more applicable but cylindrical tubing is more commonly available.

$$\frac{1}{2}C_c V_{s,\max}^2 = m c \Delta T_{\max} + m_f c_f \Delta T_{\max}$$
(D1)

where *m* is the mass (kg) and *c* is the heat capacity (J/kg.°C) of the shunt, m_f is the mass (kg) and c_f is the heat capacity (J/kg.°C) of the fluid, and ΔT_{max} is the maximum temperature change (°C) of the component.



Figure D2: Shunt in very low (electrical) conductivity / high heat capacity fluid

Equation (D1) does not account for dynamic heat flow – the fluid temperature will not rise quickly due to its low thermal conductivity compared to the metallic shunt.

This may be improved by increasing the shunt vs. fluid contact area i.e. by using a number of uniformly-spaced parallel strands of wire e.g. Nichrome resistance wire – refer to Figure D3. Each strand is enclosed by an imaginary cylinder of sufficient fluid volume (diameter d_j) to limit the increase in temperature of the strand and imaginary cylinder to ΔT_{max} .

It is assumed that any fluid beyond the imaginary cylinder has no influence in limiting ΔT_{max} due to the relatively low thermal conductivity of the fluid. This yields a minimum strand spacing a_s and hence inner diameter D_t of the tube.



Therefore rearranging equation (D1) and substituting for mass yields:

$$D_{t} = s(a_{s} + d_{s}) = s d_{f} = s \sqrt{\frac{2C_{c} V_{s,\max}^{2}}{\pi P_{f} c_{f} s l_{s} \Delta T_{\max}}} + d_{s}^{2} \left(1 - \frac{Pc}{P_{f} c_{f}}\right)$$
(D2)

where P_f is the fluid density (kg/m³), *P* is the conductor density (kg/m³), l_s is the strand length (m), d_s is the strand diameter (m), and *s* is the number of strands.

Unless the resistance of the shunt is required to be very low i.e. $R < 0.01 \Omega$, the available Nichrome wire is best used. The first step is to define the maximum allowable l_s such that the shunt can fit comfortably between the terminals. Then for each reel, assume maximum l_s and calculate the number of strands *s* to yield the required *R*. Round *s* down to the nearest integer and calculate the actual (reduced) l_s per reel. Choose the reel yielding l_s closest to the maximum allowable value, whilst ensuring that *s* is suitably high i.e. $s \ge 4$ to ensure effective

heat transfer and low inductance. Then choose a suitable fluid, and substitute for the various variables in equation (D2) to yield D_t .

<u>Example 1</u>: Require $R = 0.035 \Omega$. Terminal spacing is approximately 0.1 m; this defines the maximum allowable l_s . Choosing distilled water², and bearing in mind that the water must not be allowed to boil, conservatively choose $\Delta T_{max} = 75 \text{ °C}$. Table D3 shows the results per Nichrome wire reel, including D_t as per equation (D2).

REEL	d _s (mm)	R' (Ω/m)	s	l _s (m)	D _t (mm)	
1	1.1	0.51	1	0.069	20.1	
2	0.914	0.714	2	0.098	23.7	
3	0.9	0.79	2	0.089	25.0	
4	1.219	0.924	2	0.076	27.0	
5	0.813	0.947	2	0.074	27.3	
6	1.219	0.98	2	0.071	27.8	
7	0.71	1.292	3	0.081	31.9	
8	0.914	1.68	4	0.083	36.4	
9	0.56	2.004	5	0.087	39.8	
10	0.45	3.187	9	0.099	50.2	
11	0.4	3.95	11	0.097	55.9	
12	0.315	14.1	40	0.099	105.6	
13	0.213	14.39	41	0.100	106.6	
14	0.193	36.5	104	0.100	169.9	

Table D3: Example 1: Results per Nichrome wire reel

 $R = 0.035 \Omega$ is achieved for all reels. Typically reels 8 to 11 would be suitable i.e. $s \ge 4$, with reel 10 the optimum choice because l_s is maximised; thereafter *s* becomes too large to be practicable.

<u>Example 2</u>: Require $R = 0.650 \Omega$. Again terminal spacing is approximately 0.1 m; this defines the maximum allowable l_s . Choosing distilled water, and bearing in mind that the water must not be allowed to boil, conservatively choose

² <u>Water</u>: $P_f = 1000 \text{ kg/m}^3$ (Giancoli, 1984); $c_f = 4180 \text{ J/kg.}^\circ\text{C}$ (Counterman, 1997a).

<u>Nichrome</u>: $P = 7800 \text{ kg/m}^3$ i.e. assumed same as Iron (Giancoli, 1984); $c \approx 447 \text{ J/kg.°C}$ i.e. assumed average of Iron (450), Nickel (444) and Chrome (449) (Counterman, 1997a).

 ΔT_{max} = 75 °C. Table D4 shows the results per Nichrome wire reel, including D_t as per equation (D2).

REEL	d _s (mm)	R' (Ω/m)	s	l _s (m)	D _t (mm)					
10	0.45	3.187	0	-	-					
11	0.4	3.95	0	-	-					
12	0.315	14.1	2	0.092	24.5					
13	0.213	14.39	2	0.090	24.7					
14	0.193	36.5	5	0.089	39.4					

 Table D4:
 Example 2:
 Results per Nichrome wire reel

 $R = 0.650 \ \Omega$ cannot be achieved for reels 1 to 11. Only reel 14 is suitable because $s \ge 4$.

The above considerations would need to be explored further.

APPENDIX E

s & *l*_s CALCULATIONS FOR SIX COMPONENTS

<u>Component 1: 8/20 \mus</u> ($C_c = 8.47 \ \mu$ F, R = 0.607, $L = 4.2 \ \mu$ H)

Choose lowest *s*, then lowest l_s ; refer to Table E1 where optimum selection is shown in bold. Experimentation led to doubling up of *s* and l_s to effect a loosely packed solenoid to increase inductance.

REEL	d _s (mm)	R' (Ω/m)	S	l _s (mm)	
1	1.1	0.51	2	2.380	
2	0.914	0.714	3	2.550	
3	0.9	0.79	3	2.305	
4	1.219	0.924	3	1.971	
5	1.219	0.98	3	1.858	
6	0.813	0.947	4	2.564	
7	0.71	1.292	5	2.349	
8	0.914	1.68	5	1.807	
9	0.56	2.004	8	2.423	
10	0.45	3.187	12	2.286	
11	0.4	3.95	15	2.305	
12	0.315	14.1	34	1.464	
13	0.213	14.39	51	2.151	
14	0.193	36.5	89	1.480	

Table E1: Component 1: Nichrome reel data sorted by s then l_s

<u>Component 2: 8/20 μs</u> (*C_c* = 33.93 μF, *R* = 0.149, *L* = 0.3 μH)

Choose lowest l_s for even-numbered s; refer to Table E2 where optimum selection is shown in bold. Effect anti-parallel strand loops to minimise inductance.

Table L2. Component 2. Nichrome reel data softed by t_s									
REEL	d _s (mm)	R' (Ω/m)	l _s (mm)	S					
12	0.315	14.1	1.458	138					
14	0.193	36.5	1.474	361					
8	0.914	1.68	1.508	17					
6	1.219	0.98	1.520	10					
4	1.219	0.924	1.613	10					
13	0.213	14.39	2.133	206					
10	0.45	3.187	2.151	46					
11	0.4	3.95	2.188	58					
7	0.71	1.292	2.191	19					
5	0.813	0.947	2.203	14					
9	0.56	2.004	2.231	30					
3	0.9	0.79	2.263	12					
2	0.914	0.714	2.296	11					
1	1.1	0.51	2.337	8					

 Table E2:
 Component 2: Nichrome reel data sorted by *l_s*

<u>Component 3: 8/20 μs</u> (*C*_c = 136.0 μF, *R* = 0.035, *L* = 0 μH)

Choose lowest l_s for even-numbered s, but avoid high s because numerous thin strands of wire are not workable; refer to Table E3 where optimum selection is shown in bold. Note that odd s is not viewed as critical because it is quite high. Effect anti-parallel strand loops to minimise inductance.

				j - 3
REEL	d _s (mm)	R' (Ω/m)	l _s (mm)	S
6	1.219	0.98	0.643	21
12	0.315	14.1	0.651	306
8	0.914	1.68	0.661	37
14	0.193	36.5	0.661	804
4	1.219	0.924	0.682	21
13	0.213	14.39	0.953	457
10	0.45	3.187	0.960	102
11	0.4	3.95	0.972	128
9	0.56	2.004	0.973	65
7	0.71	1.292	0.975	42
5	0.813	0.947	0.982	31
3	0.9	0.79	0.987	26
1	1.1	0.51	1.000	17
2	0.914	0.714	1.008	24

Table E3: Component 3: Nichrome reel data sorted by l_s

Component 4: 4/70 μs (*C_c* = 8.47 μF, *R* = 10.479, *L* = 15.3 μH)

Choose lowest s, then lowest l_s ; refer to Table E4 where optimum selection is shown in bold. Effect loosely packed solenoid to increase inductance.

REEL	d _s (mm)	R' (Ω/m)	S	l _s (mm)
8	0.914	1.68	1	6.238
6	1.219	0.98	1	10.693
5	0.813	0.947	1	11.065
4	1.219	0.924	1	11.341
3	0.9	0.79	1	13.265
2	0.914	0.714	1	14.676
1	1.1	0.51	1	20.547
9	0.56	2.004	2	10.458
7	0.71	1.292	2	16.221
10	0.45	3.187	3	9.864
11	0.4	3.95	4	10.612
12	0.315	14.1	9	6.689
13	0.213	14.39	13	9.467
14	0.193	36.5	22	6.316

Table E4: Component 4: Nichrome reel data sorted by s then l_s

<u>Component 5: 4/70 μ s</u> (C_c = 33.93 μ F, R = 2.613, L = 3.0 μ H)

Choose lowest l_s but avoid high *s*; refer to Table E5 where optimum selection is shown in bold. Effect bifilar winding to reduce inductance.

REEL	d _s (mm)	R' (Ω/m)	l _s (mm)	s
12	0.315	14.1	6.116	33
8	0.914	1.68	6.221	4
14	0.193	36.5	6.228	87
6	1.219	0.98	7.999	3
4	1.219	0.924	8.484	3
13	0.213	14.39	8.898	49
10	0.45	3.187	9.019	11
9	0.56	2.004	9.127	7
11	0.4	3.95	9.261	14
3	0.9	0.79	9.923	3
7	0.71	1.292	10.112	5
1	1.1	0.51	10.247	2
2	0.914	0.714	10.979	3
5	0.813	0.947	11.037	4

Table E5: Component 5: Nichrome reel data sorted by l_s

<u>Component 6: 4/70 μs</u> (*C_c* = 102.3 μF, *R* = 0.863, *L* = 0.2 μH)

Choose lowest l_s for even-numbered s, but avoid high s because numerous thin strands of wire are not workable; refer to Table E6 where optimum selection is shown in bold. Effect anti-parallel strand loops to minimise inductance.

REEL	d _s (mm)	R' (Ω/m)	l _s (mm)	S
12	0.315	14.1	3.060	50
14	0.193	36.5	3.074	130
8	0.914	1.68	3.082	6
6	1.219	0.98	3.522	4
4	1.219	0.924	3.736	4
13	0.213	14.39	4.438	74
5	0.813	0.947	4.556	5
11	0.4	3.95	4.588	21
10	0.45	3.187	4.603	17
7	0.71	1.292	4.676	7
9	0.56	2.004	4.737	11
2	0.914	0.714	4.835	4
1	1.1	0.51	5.076	3
3	0.9	0.79	5.462	5

Table E6: Component 6: Nichrome reel data sorted by l_s

APPENDIX F

QUANTIFICATION OF *I* vs. *V_s* PER COMPONENT

See overleaf.



Table F1: Quantification of I vs. V_s for components 1, 2, 4, 5 & 6 COMPONENT 1: 8/20 us

APPENDIX G

BENCHMARK SAMPLE TEST SHEET

See overleaf.

	IDEAL										PRACTICAL					
Samplo	Wave-	I	Cc	l/Vs	Twg	Vs	Qg	Gap	Vs	I	l/Vs	File	Comments			
Sample	form	(kA)	(uF)	(kA/kV)	(us)	(kV)	(mC)	groups	(kV)	(kA)	(kA/kV)					
1	8/20 us	2	8.47	0.6862	12.35	2.9	25	1+1+1+1	3.0	2.0	0.6569	TEK1a,b,c,d	None, clipped, overshot, clipped			
2	8/20 us	5	8.47	0.6862	12.35	7.3	62	2+2	7.0	4.7	0.6743	TEK2a,b				
3	8/20 us	8	8.47	0.6862	12.35	11.7	99	4	11.0	7.4	0.6764	TEK3	Clipped			
4	8/20 us	11	8.47	0.6862	12.35	16.0	136	4	15.1	10.2	0.6781	TEK4				
5	8/20 us	13	8.47	0.6862	12.35	18.9	161	4	19.1	13.0	0.6806	TEK5				
6	8/20 us	14	33.93	2.6993	12.57	5.2	176	2+2	5.2	13.4	2.5769	TEK6a,b				
7	8/20 us	24	33.93	2.6993	12.57	8.9	302	2+2	8.8	23.2	2.6364	TEK7a,b				
8	8/20 us	34	33.93	2.6993	12.57	12.6	427	4	12.5	32.8	2.6240	TEK8				
9	8/20 us	44	33.93	2.6993	12.57	16.3	553	4	16.1	42.6	2.6460	TEK9				
10	8/20 us	53	33.93	2.6993	12.57	19.6	666	4	19.7	52.6	2.6701	TEK10				
46	4/70 us	0.4	8.47	0.0880	96.30	4.5	39	1+1+1+1	4.5	0.4	0.0889	TEK46a,b,c,d	Clipped, overshot, overshot, clipped			
47	4/70 us	0.7	8.47	0.0880	96.30	8.0	67	2+2	8.0	0.7	0.0875	TEK47a,b	Clipped, clipped			
48	4/70 us	1.0	8.47	0.0880	96.30	11.4	96	4	11.4	1.0	0.0877	TEK48	Clipped			
49	4/70 us	1.3	8.47	0.0880	96.30	14.8	125	4	14.8	1.3	0.0878	-	Clipped			
50	4/70 us	1.7	8.47	0.0880	96.30	19.3	164	4	19.3	1.7	0.0881	TEK50	Clipped			
51	4/70 us	2	33.93	0.3525	96.26	5.7	193	2+2	5.7	2.0	0.3509	TEK51a,b	None, overshot			
52	4/70 us	3	33.93	0.3525	96.26	8.5	289	2+2	8.5	3.0	0.3529	TEK52a,b	None, clipped			
53	4/70 us	4	33.93	0.3525	96.26	11.3	385	4	11.3	4.0	0.3540	TEK53	?			
54	4/70 us	5	33.93	0.3525	96.26	14.2	481	4	14.2	5.0	0.3521	TEK54	None			
55	4/70 us	6	33.93	0.3525	96.26	17.0	578	4	17.0	6.0	0.3529	TEK55	Overshot			
56	5/72 us	7	102.30	1.0305	99.27	6.9	705	2+2	6.9	7.0	1.0145	TEK56a,b				
57	5/72 us	8	102.30	1.0305	99.27	7.8	794	2+2	7.8	8.0	1.0256	TEK57a,b				
58	5/72 us	9	102.30	1.0305	99.27	8.7	893	2+2	8.7	8.9	1.0230	TEK58a,b				
59	5/72 us	10	102.30	1.0305	99.27	9.7	993	2+2	9.7	9.9	1.0206	TEK59a,b				
60	5/72 us	10.3	102.30	1.0305	99.27	10.0	1023	4	10.0	10.2	1.0200	TEK60				

 Table G1: Test sheet for reduced benchmark sample

APPENDIX H

GAP ETCHING MEASUREMENT DATA

See overleaf.

2.0	kA	1		1	2		3	4	1
	Dx								
<u>р</u>	Dy			1.613	1.664	0.854			
hid.	dx			1.306	1.432	0.849			
윎	dy								
	D/d	#DIV/0!	#DIV/0!	1.24	1.16	1.01	#DIV/0!	#DIV/0!	#DIV/0!
	Dx								
0	Dy					1.200			
iii iii	dx					1.134			
1 H	dy								
_	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	1.06	#DIV/0!	#DIV/0!	#DIV/0!
Etching	Area per			4.05	4.07	4.04			
gap plat	te (mm2)			1.05	1.07	1.64			
Amean (mm2) 1.72									
Std. dev	/. (mm2)	0.11							

Table H1: Gap etching data (8/20 μ s, 2.0 to 13.0 kA)

4.7	kA		1		2		3		4	
	Dx				0.425	0.577	1.260	1.616		
6	Dy	2.290	2.295	2.265	2.447	2.186	1.825	0.437		
i i i i i i i i i i i i i i i i i i i	dx	2.249	2.195	2.017	1.841	1.852	1.559	0.452		
윎	dy				0.342	0.530	1.195	1.434		
	D/d	1.02	1.05	1.12	1.33	1.17	1.13	1.11	#DIV/0!	
	Dx					0.377		1.018		
0	Dy					0.269	0.333	1.461		
ir ir	dx					0.225	0.247	1.074		
a constant and a constant a cons	dy					0.265		0.697		
	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	1.33	1.35	1.39	#DIV/0!	
Etching	Area per	4.04	2.00	2.50	2.05	2.55	2.40	2.77		
gap pla	te (mm2)	4.04	3.96	3.59	3.65	3.55	3.49	3.11		
Amear	i (mm2)				3.	72				
Std dev (mm2)										

7.4	kA	1	1		2		3		4
	Dx	0.382	0.291						
6	Dy	3.136	2.922	3.056	2.942	3.360	3.088	3.098	3.216
臣	dx	2.753	2.681	2.722	2.850	2.491	2.640	2.707	2.657
윎	dy	0.329	0.197						
	D/d	1.14	1.09	1.12	1.03	1.35	1.17	1.14	1.21
	Dx								
6	Dy								
in the second se	dx								
태	dy								
_	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching	Area per	C 00	C 20	6.52	0.50	6.57	C 40	0.00	0.74
gap pla	te (mm2)	0.00	0.20	0.53	53 6.59 6.57 6.40 6.59 6.7			0./1	
Amear	Amean (mm2) 6.56								
Std. de	/. (mm2)				0.	19			

10.2	kA	1	1		2		3		4
	Dx								
5	Dy	3.680	3.670	3.565	3.629	3.435	3.488	3.451	3.514
i	dx	3.190	3.146	3.247	3.200	2.272	2.257	3.261	3.213
l ដំ	dy								
	D/d	1.15	1.17	1.10	1.13	1.51	1.55	1.06	1.09
	Dx								
0	Dy					2.310	2.220		
Ë	dx					1.374	1.584		
읪	dy								
	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	1.68	1.40	#DIV/0!	#DIV/0!
Etching	Area per	0.00	0.07	0.00	0.10	0.00	0.04	0.04	0.07
gap plate (mm2) 9.22 9.07			5.09	3.1Z	0.02	0.94	0.04	0.07	
Amean (mm2) 8.97									
Std. dev	/. (mm2)	0.18							

13.0	kA	1	1		2		3		4
	Dx								
6	Dy	4.167	4.244	3.836	3.935	4.097	4.204	4.116	3.870
in the second se	dx	3.403	3.333	3.651	3.790	3.598	3.568	3.373	3.401
ポ	dy								
_	D/d	1.22	1.27	1.05	1.04	1.14	1.18	1.22	1.14
	Dx								
6	Dy								
Ë	dx								
읪	dy								
	D/d	#DIV/0!							
Etching gap plat	Area per te (mm2)	11.14	11.11	11.00	11.71	11.58	11.78	10.90	10.34
Amear	Amean (mm2) 11.19								
Std. dev	/. (mm2)				0.	45			

13.4	kA	1	1	1	2		3	4	1
	Dx								
<u>р</u>	Dy	3.914	4.079	4.125	3.966	3.991	3.877	3.842	3.885
hin	dx	3.686	3.690	3.532	3.531	3.660	3.851	3.757	3.788
1 fil	dy								
_	D/d	1.06	1.11	1.17	1.12	1.09	1.01	1.02	1.03
	Dx								
6	Dy								
iii iii	dx								
1 H	dy								
_	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching gap plat	Area per te (mm2)	11.33	11.33 11.82 11.44 11.00 11.47 11.73 11.34 11.						
Amean	i (mm2)) 11.46							
Std. dev	/. (mm2)	0.24							

Table H2: Gap etching data (8/20 μ s, 13.4 to 52.6 kA)

23.2	kA	1	1		2	1	3	4	1
	Dx								
6	Dy	5.032	4.887	5.119	4.925	5.039	4.893	5.077	4.932
h	dx	4.944	4.701	5.071	4.816	4.989	4.823	5.076	4.911
윎	dy								
-	D/d	1.02	1.04	1.01	1.02	1.01	1.01	1.00	1.00
	Dx								
6	Dy								
Ē	dx								
윎	dy								
-	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching gap plat	Area per te (mm2)	rea per (mm2) 19.54 18.04 20.39 18.63 19.74 18.53 20.24						19.02	
Amean	Amean (mm2) 19.27								
Std. dev	/. (mm2)				0.	79			

32.8	kA	1	1	:	2	:	3	4	1
	Dx								
<u>р</u>	Dy	5.780	5.633	6.002	5.546	5.596	5.794	5.582	5.588
hid	dx	5.489	5.522	5.705	5.372	5.558	5.774	5.413	5.424
ti i	dy								
	D/d	1.05	1.02	1.05	1.03	1.01	1.00	1.03	1.03
	Dx								
0	Dy								
iq	dx								
t di la constante di la consta	dy								
	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching gap plat	Area per te (mm2)	24.92 24.43 26.89 23.40 24.43 26.28 23.73					23.80		
Amean	1 (mm2)	im2) 24.73							
Std. dev	/. (mm2)				1.	17			

42.6	kA		1		2		3		4
	Dx								
<u>0</u>	Dy	6.164	5.704	6.447	6.064	5.936	5.964	6.207	5.973
i i i i i i i i i i i i i i i i i i i	dx	5.915	5.604	6.334	6.006	5.929	5.740	6.196	5.838
l ដ	dy								
	D/d	1.04	1.02	1.02	1.01	1.00	1.04	1.00	1.02
~	Dx								
D D	Dy								
i i i	dx								
ш	dy								
	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching gap plat	Area per te (mm2)	page page <th< th=""><th>30.21</th><th>27.39</th></th<>					30.21	27.39	
Amear	nean (mm2) 28.32				1				
Std. dev. (mm2) 1.99									

52.6	kA	1	1		2		3		4	
	Dx									
6	Dy	5.848	6.033	5.961	6.173	6.258	6.166	6.036	5.929	
i i i i i i i i i i i i i i i i i i i	dx	5.840	5.986	5.836	6.171	6.206	6.112	5.870	5.870	
l 能	dy									
_	D/d	1.00	1.01	1.02	1.00	1.01	1.01	1.03	1.01	
	Dx									
0	Dy									
臣	dx									
읪	dy									
	D/d	#DIV/0!								
Etching	Area per	26.92	20.20	07.20	20.02	20.50	20.60	27.92	07.22	
gap plat	te (mm2)	20.02	20.30	21.32	23.92	30.50	23.00	21.03	21.33	
Amear	n (mm2)				28	.46				
Std. dev	/. (mm2)				1.	29				

0.4	۲A	1	1	1	2		3	4	ļ
0.4	KA	-	+	-	+	-	+	-	+
	Dx								
5	Dy		0.792		0.948		0.792		0.855
hin	dx		0.712		0.678		0.719		0.675
l fi	dy								
_	D/d	#DIV/0!	1.11	#DIV/0!	1.40	#DIV/0!	1.10	#DIV/0!	1.27
	Dx								
0	Dy								
Lid.	dx								
l fi	dy								
	D/d	#DIV/0!							
Etching	Area per		0.44		0.00		0.45		0.45
gap plat	te (mm2)		0.44		0.00		0.45		0.45
Amean (mm2) 0.46									
Std. dev	/. (mm2)				0.	02			

Table H3: Gap etching data (4/70 $\mu s,\,0.4$ to 1.7 kA)

0.7	μA	1		1	2		3	4	ļ.	
0.7	ка	-	+	-	+	-	+	-	+	
	Dx									
<u>0</u>	Dy				1.241		1.117		1.190	
hin	dx				0.999		1.009		1.170	
ц Ц	dy									
_	D/d	#DIV/0!	#DIV/0!	#DIV/0!	1.24	#DIV/0!	1.11	#DIV/0!	1.02	
	Dx									
0	Dy									
hin	dx									
ц Ш	dy									
	D/d	#DIV/0!	#DIV/0!							
Etching /	Area per				0.07		0.00		1.00	
gap plat	e (mm2)				0.97		0.09	0.89 1.09		
Amean	(mm2)			0.98						
Std. dev	/. (mm2)				0.	09				

1.0	ĿА	1	1	1	2		3	4	
1.0	KA	-	+	-	+	-	+	-	+
	Dx								
D	Dy		1.455		1.166		1.325		1.620
Etchin	dx		1.410		0.988		1.110		1.278
	dy								
	D/d	#DIV/0!	1.03	#DIV/0!	1.18	#DIV/0!	1.19	#DIV/0!	1.27
	Dx								
0	Dy				0.523				
hid	dx				0.500				
l H	dy								
_	D/d	#DIV/0!	#DIV/0!	#DIV/0!	1.05	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching	Area per		1.61		1 11		1 16		1.63
gap plate (mm2)			1.01		1.11		1.10		1.05
Amean	(mm2)				1.	38			
Std. dev	r. (mm2)				0.	24			

12 64		1		2		3		4	
1.5	KA .	-	+	-	+	-	+	-	+
	Dx								
Etching 1	Dy		1.497		1.463		1.508		1.771
	dx		1.301		1.066		1.499		1.197
	dy								
	D/d	#DIV/0!	1.15	#DIV/0!	1.37	#DIV/0!	1.01	#DIV/0!	1.48
	Dx								
0	Dy				0.694				
Ę	dx				0.684				
윎	dy								
_	D/d	#DIV/0!	#DIV/0!	#DIV/0!	1.01	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching	Area per		1.53		1.60		1 78		1.66
gap plate (mm2)			1.00		1.00		1.10		1.00
Amean	(mm2)				1.	64			
Std. dev	/. (mm2)				0.	09			

17 44		1		2	2	3		4	
1.7	KA	-	+	-	+	-	+	-	+
	Dx								
Etching 1	Dy		1.269		1.814		1.934		2.255
	dx		1.165		1.757		1.723		1.523
	dy								
	D/d	#DIV/0!	1.09	#DIV/0!	1.03	#DIV/0!	1.12	#DIV/0!	1.48
	Dx								
0	Dy		1.474		0.403				
iii.	dx		1.423		0.178				
ti i	dy								
_	D/d	#DIV/0!	1.04	#DIV/0!	2.26	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!
Etching	Area per		0.04		2.55		2.02		0.70
gap plat	e (mm2)		2.01		2.50		2.02		2.70
Amean	(mm2)				2.	67			
Std. dev	/. (mm2)				0.	09			

			1	2	(p.c., _:	3	4	, 1		
2.0	kA	-	+		+	-	+	-	+		
	Dx		0.050		4.000		4.000		4.040		
jug	dx		2.050		1.983		1.960		1.813		
E	dy										
	D/d	#DIV/0!	1.22	#DIV/0!	1.04	#DIV/0!	1.17	#DIV/0!	1.24		
2	Dx Dv		0.673						0.676		
ių	dx		0.512						0.411		
ш	dy D/d	#DIV//01	4 24	#DIV//01	#DIV//01	#DIV/01	#DIV//01	#DIV//01	1.64		
Etching	Area per	#DIV/0!	1.01	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	1.04		
gap plat	te (mm2)		2.97		2.97		2.58		2.31		
Amear	n (mm2)				2.	71					
Std. dev	/. (mm2)	0.28									
3.0	k۸	1	1	2	2	3	3	4	1		
5.0		-	+	-	+	-	+	-	+		
-	Dx Dv		2.985		2.940		2.829		2.473		
ių	dx		2.091		1.900		2.380		2.081		
ŭ	dy D/d	#DIV/01	1 42	#DIV//01	1 55	#DIV/01	1 10	#DIV//01	1 10		
	D/d Dx	#DIV/0!	1.45	#DIV/0!	1.00	#DIV/0!	1.19	#DIV/0!	1.19		
1g 2	Dy								1.437		
tchir	dx								1.156		
Ű	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	1.24		
Etching	Area per		4 90		4.39		5.29		5.35		
gap plat	te (mm2)		4.50		7.00	0.0	5.25		0.00		
Std. dev	r (mm2) 7. (mm2)				4.	98 38					
		I									
4.0	kA	1	4	1	2		}	4			
	Dx	-	-		•	-	-	-	-		
5	Dy		3.008		2.612		3.153		3.372		
Etchir	dx dv		2.995		2.151		3.003		2.757		
	D/d	#DIV/0!	1.00	#DIV/0!	1.21	#DIV/0!	1.05	#DIV/0!	1.22		
Etching 2	Dx										
	Dy dv				1.305						
	dy dy				0.771						
	D/d	#DIV/0!	#DIV/0!	#DIV/0!	1.69	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!		
m	Dx Dv				1 220						
hing	dx				0.955						
Ê	dy										
Etching	D/d	#DIV/0!	#DIV/0!	#DIV/0!	1.30	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!		
gap plat	te (mm2)		7.08		6.13		7.44		7.30		
Amear	n (mm2)	6.99									
Std. dev	/. (mm2)	0.51									
5.0	LA.	1	1	2	2		3	4	1		
5.0	ка –	-	+	-	+	-	+	-	+		
-	Dx Dv		3 / 37		3 754		3 335		3 510		
hing	dx		3.084		2.911		3.033		3.122		
ш	dy	#DIN (/0)	4.44	4DI (/01	4.00	#DI1 (/0)	4.40	4DB (/0)	1.60		
	D/d Dx	#DIV/0!	1.11	#DIV/0!	1.29	#DIV/0!	1.10	#DIV/0!	1.12		
1g 2	Dy		1.032								
tchir	dx dv		0.909								
ü	D/d	#DIV/0!	1.14	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!		
Etching	Area per		9.06		8 58		7 94		8 61		
gap plat	te (mm2)		0.00		0.00	55			0.01		
Std. dev	/. (mm2)				8.5 0.4	40					
6.0	kA	-	+		<u>'</u>) +	- 4	+		
_	Dx	_	-	-		_		-			
ing 1	Dy	3.801	3.949		3.726	3.798	3.919	3.732	3.748		
itchi	dx dv	2.954	2.967		3.0/6	3.132	3.303	3.1/1	3.199		
	D/d	1.29	1.33	#DIV/0!	1.01	1.21	1.19	1.18	1.17		
N	Dx										
hing	dx										
Eter	dy										
Etching	D/d	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!	#DIV/0!		
gap plat	te (mm2)	8.82	9.20		10.76	9.34	10.17	9.29	9.42		
Amear	n (mm2)				9.	57					
Ctd do	((mm2)				0.0	61			I		

Table H4: Gap etching data (4/70 µs, 2.0 to 6.0 kA)

7 0 kA		1		2		3		4	
7.0	R.H.	-	+	-	+	-	+	-	+
hing 1	Dx								
	Dy	4.181	4.061	3.929	4.131	4.228	4.237	4.009	4.080
	dx	3.956	3.997	3.876	3.859	3.479	3.731	3.847	3.928
l fi	dy								
	D/d	1.06	1.02	1.01	1.07	1.22	1.14	1.04	1.04
	Dx								
0	Dy								
Ē	dx								
1 H	dy								
	D/d	#DIV/0!							
Etching Area per gap plate (mm2)		12.99	12.75	11.96	12.52	11.55	12.42	12.11	12.59
Amean	i (mm2)				12	.36			
Std. dev	/. (mm2)				0.4	43			

Table H5: Gap etching data (5/72 μ s, 7.0 to 10.2 kA)

8.0 kA		1		2		3		4	
		-	+	-	+	-	+	-	+
	Dx								
Etching 1	Dy	4.479	4.306	4.201	4.175	4.307	4.201	4.223	4.082
	dx	3.994	3.871	4.009	3.937	3.898	3.957	4.067	4.073
	dy								
	D/d	1.12	1.11	1.05	1.06	1.10	1.06	1.04	1.00
	Dx								
0	Dy								
hid	dx								
l H	dy								
	D/d	#DIV/0!							
Etching Area per gap plate (mm2)		14.05	13.09	13.23	12.91	13.19	13.06	13.49	13.06
Amean	(mm2)				13	.26			
Std. dev	/. (mm2)				0.	34			

80 44		1			2		3		4	
0.9	ка	-	+	-	+	-	+	-	+	
Etching 1	Dx									
	Dy	4.706	4.411	4.438	4.403	4.556	4.340	4.486	4.257	
	dx	4.571	4.163	4.440	4.226	4.259	4.173	4.450	4.223	
	dy									
	D/d	1.03	1.06	1.00	1.04	1.07	1.04	1.01	1.01	
	Dx									
0	Dy									
iii ii	dx									
ti i	dy									
	D/d	#DIV/0!								
Etching Area per gap plate (mm2)		16.89	14.42	15.48	14.61	15.24	14.22	15.68	14.12	
Amean	i (mm2)				15	.08				
Std. dev	/. (mm2)				0.	88				

0.0 44		1	1	2	2	3		4	
5.5	KA	-	+	-	+	-	+	-	+
	Dx								
ō,	Dy	4.705	4.563	4.816	4.661	4.935	4.844	4.996	4.756
iq	dx	4.633	4.449	4.735	4.553	4.875	4.586	4.840	4.712
1 1 1	dy								
	D/d	1.02	1.03	1.02	1.02	1.01	1.06	1.03	1.01
	Dx								
0	Dy								
i i i i i i i i i i i i i i i i i i i	dx								
l fi	dy								
	D/d	#DIV/0!							
Etching Area per gap plate (mm2)		17.12	15.94	17.91	16.67	18.90	17.45	18.99	17.60
Amean	(mm2)				17	.57			
Std. dev	r. (mm2)				0.	97			

10.2 %		1		1	2		3	4	
10.2	ка	-	+	-	+	-	+	-	+
	Dx								
g 1	Dy	5.079	4.896	4.961	4.688	5.113	4.655	5.309	4.715
ių	dx	4.846	4.680	4.823	4.462	4.966	4.431	5.197	4.638
븮	dy								
	D/d	1.05	1.05	1.03	1.05	1.03	1.05	1.02	1.02
	Dx								
B	Dy								
hin	dx								
Ĕ	dy								
	D/d	#DIV/0!							
Etching Area per gap plate (mm2)		19.33	18.00	18.79	16.43	19.94	16.20	21.67	17.18
Amean	(mm2)				18	.44			
Std. dev	r. (mm2)				1.	75			

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