

IMPROVED INVENTORY CONTROL AT
BOART HARDMETALS (PTY) LTD

BY: M Jagoe

IMPROVED INVENTORY CONTROL AT BOART HARDMETALS (PTY) LIMITED

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ABSTRACT

This work covers the use of exponential smoothing in calculating order points. Various exponential models are tested and based on an inventory simulation, a model is chosen that will reduce the total inventory holding. Rules are developed for reordering inventory; A-B-C analysis of the inventory is used to highlight those items requiring tight control and a further analysis by customer is used to indicate demand vulnerability. Savings of at least 28% of the inventory costs are expected.

DECLARATION

I hereby declare that this is
my own, unaided work

A handwritten signature in cursive script, appearing to read "Jagoe", written over a horizontal line.

M Jagoe

For reasons of confidentiality, the following alterations have been made to this report:

- 1) All part numbers have been deleted. Reference numbers have been given to the six items specifically dealt with in the report.
- 2) All rand values for inventory and sales listings have been deleted.

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1. SUMMARY

1.1. Scope of the Report

This report covers the use of time series analysis techniques for forecasting demand.

An inventory simulation is carried out, using the forecasted demand, and it is shown that inventory can be reduced by 25%.

1.2. Findings

1.2.1 An A-B-C analysis of the sales data shows that 20% of the items for 2000 units is responsible for 75% of the total demand for these items. These items are the most important, and in this analysis, an A-B-C analysis is shown, and the A-B-C analysis is shown.

1.2.2 The forecasting system needs to be improved, making information.

1.2.3 The inventory simulation shows the distinct advantage of regular monitoring of demand. An inventory saving of R84 500 was possible in the period April 1980 to January 1981.

1.2.4 These savings can be obtained by using an exponential smoothing model, with the tracking signal used as a control parameter. The R84 500 saving can be increased to R114 000 by better matching of the forecasting model to individual demand data.

Conclusions

- 1.1.1 The current inventory ordering system is inadequate. The re-order point is not recalculated frequently enough nor does it have any statistical basis. The order point should be recalculated monthly as described in this report.
- 1.1.2 An A-B-C analysis should be carried out regularly (every three months) and cover at least the past six month's sales data. This analysis should be used for:
 - (a) Determining demand vulnerability by analysing the 'A' items by customer.
 - (b) Choosing the forecasting model. The exponential smoothing model (using the tracking signal as a control parameter) is suggested for 'A' items. Adaptive smoothing using the Trigg and Leach model, is suggested for 'B' items.
 - (c) Items should be made only on receipt of a customer order.
- 1.3.3 Inventory should be ordered on the basis of the ordering rule suggested in Section 7.7.6.
- 1.3.4 Exception reports must be produced monthly for all forecasts that are out of control. The products should be listed in their A-B-C rankings, so that the most important items receive attention first.
- 1.3.5 Further work should be carried out to determine the optimum distribution of inventory amongst the various branches. The inventory savings calculated in this report are based on the assumption that all demand is satisfied from one central point. The branches could possibly be more economically and efficiently served by special weekly deliveries from the central point. This is particularly attractive as 74% of the sales take place from three branch offices, excluding the central branch.

2. INTRODUCTION

The drill market in South Africa is primarily concentrated. A limited number of customers account for the bulk of the demand. As a result of this, the demand pattern for drill tools and equipment is sensitive to changes in customer requirements.

Amongst the factors influencing demand for drill tools are:

- a) The competitive scene;
- b) Fluctuation in stock levels and inventory contracts;
- c) Changes in government policy;
- d) Changes in drilling techniques;
- e) Laws of business because of responsibility of staff.

These factors amongst others, influence demand for drill tools which are usually done in the system by inventory.

The purpose of the report is to determine if there is any place for a mechanized forecasting system in forecasting inventory control, the current inventory system is based on the following factors -

"All the following factors are used
to forecast demand for drill tools
and equipment."

The basis of the report is to determine if the forecasted by using inventory (10) drill tools is done in forecasting system and inventory control system. The case study is a company which produces drill tools, mostly concerned with drill tools and equipment.

The body of the report discusses the importance of the forecast analysis using of drill tools and equipment, the forecast analysis, the inventory control and the forecast analysis. The forecast analysis is done in the following way -

FORECASTING

1.1 Forecasting

Many forecasts are made in the course of running a business, and they are used for a variety of purposes. Forecasts can be used for setting budgets, planning capital expenditures and for production and inventory control planning.

The need for forecasting is frequently arising because a production or inventory control system must be able to follow some rules. These rules specify demand and quantity for any particular time. They are based on a routine basis to every products.

De Salvia (6) points out that a business firm is operating in an environment of uncertainty, and ultimately the firm has to adjust or adapt to this environment. He notes that, in the manufacturing area, there are only three basic ways of adapting to uncertainty:

1. The firm may develop flexible means of production - flexible in its ability to alter rates of production and flexible with regard to product changes.
2. The firm may cushion itself from the effects of uncertainty through inventory policies, particularly in regard to safety stocks.
3. Finally, the firm may attempt to reduce uncertainty through improved methods, prediction or forecasting.

He notes that these three courses of action are not mutually exclusive. The actual course adopted may be some mixture of the three. Furthermore, each course of action has its own cost associated with it and ideally one should minimise costs.

Forecasting is therefore one way in which a firm can try to reduce the uncertainty of the future.

De Salvia (6) points out that a forecast is essential in developing a production schedule. This schedule is an essential document required by the production and inventory control departments in order to plan the factory work load and resources.

Mechanistic forecasting, using a computer model with a monitoring system provides for exception reporting.

A further reason for forecasting is the fact that lead times for raw material and capital equipment generally far exceed those for production. It is therefore necessary to order the raw material or equipment long before production orders are raised. Forecasting of the correct items and quantities will enable stock reductions to be carried out and customer service to be improved.

3.2 What To Forecast

Orlicky (9) first proposed the independent-dependent demand principle in 1971, in which he states that demand should only be forecast for independent demand items. These are items which he defines as finished goods, or service parts not used in current production, or items where the demand is unrelated to that of others. On the other hand, where demand is dependent, ie related to the demand for other finished goods, it must not be forecasted, but calculated through a bill of material explosion, based on the demand for the finished goods.

It is also necessary to sort the sales items into order of importance. An A-B-C (Pareto) analysis will rank the sales in descending order of sales value. Stratton (11) points out that the A-B-C analysis will prompt the marketing product managers to examine their product lines more closely in order to identify low sales and low profit items. It will also assist management in identifying those items which constitute the bulk of the sales value.

3.3 Forecasting Systems

There are three basic groups of forecasting systems:

- a) Qualitative
- b) Causal
- c) Time series

1.2.1 Qualitative Systems

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In this case, all information and judgments related to an item's demand are used to forecast the future demand. It is often used when little history is available. The forecasts could also be based on market research studies. It is most suited to the forecasting of demand for a product group rather than for individual items due to the judgmental nature of the forecasting process.

1.2.2 Causal Systems

In this instance, the forecaster attempts to find a relationship between some indication or index and the demand for an item or product group. A cause and effect relationship is sought. These techniques are also more suited to forecasting the demand of product groups, because of the cost and effort involved in finding a causal relationship.

1.2.3 Time Series Analysis

These techniques rely on a statistical analysis of historical demand to predict future demand. It assumes that underlying trends in the past will be continued into the future. Items which do not fall into this category should not be forecasted by this method. They are better served by the methods described in 1.2.1 and 1.2.2.

It is generally accepted that forecasting based on Time Series Analysis is a more powerful method, when the demand for a item or group of items does not have to be forecasted on a particular time. The method used is basically dependent on the nature of the demand of the item, and not on the demand for the method. The fact that it assumes that the demand for a item or group of items will continue to follow the same pattern.

1.2.1 Qualitative Systems
1.2.2 Causal Systems
1.2.3 Time Series Analysis

2.4 Demand Patterns

Demand patterns must be recognized in order to select the correct forecasting model.

2.4.1 Unilateral Demand Patterns

In this part it is assumed that random fluctuations in demand occur about a mean level which remains unchanged with the passage of time.

2.4.2 Level Demand Patterns

Only a single mean level of demand is shown during a certain period. Typical examples are the inventory of a warehouse or the production of a factory.

2.4.3 Seasonal Demand Patterns

Seasonal demand patterns are characterized by a regular and periodic variation in demand.

2.4.4 Trend Demand

Trend demand patterns are characterized by a steady increase or decrease in demand over time. Typical examples are the demand for new cars or the demand for new houses. The demand for new cars is increasing steadily over time, while the demand for new houses is decreasing steadily over time. The demand for new cars is increasing steadily over time, while the demand for new houses is decreasing steadily over time. The demand for new cars is increasing steadily over time, while the demand for new houses is decreasing steadily over time.

3.5 Demand Distribution

The following assumptions are made about the demand distribution in order that the time series analysis techniques can be applied:

- The demand distribution is symmetrical
- The demand distribution is unimodal
- The fluctuations about the mean are due to random influences.

4.1 REVIEW OF THE LITERATURE ON TIME SERIES ANALYSIS

4.1.1 Introduction

The literature on forecasting is so voluminous that I have drawn on previous surveys by Lewis (7) and Oduardo (8). The references [Brown (2)] point out that for cost effective competition it is essential that the forecasting model should:

- 1) Require the minimum of historical data.
- 2) Be able to introduce the latest demand information as it becomes available.
- 3) Be simple to calculate.

The models discussed below (except for moving averages) comply with the above requirements. In addition, interpretation of the models does not require an extensive mathematical background. This is an important point since, as Lewis (7) points out:

"One of the principle reasons why forecasting techniques have not gained an even more widespread acceptance than they have, has been the very natural antagonism toward the use of mathematics."

4.2 Types Of Models

4.2.1 Stationary Models

These are models to be used where the demand pattern is essentially horizontal, eg

- 1) Moving averages
- 2) Exponential smoothing

4.2.2 Growth Models

Where the demand pattern is rising or falling, the models mentioned in 4.2.1 tend to lag behind the demand. When the demand is growing, it is being under-forecasted and when it is falling it is being over-forecasted. In

$$x(n)_6 = \sum_{c=n-5}^n (x(c)_6)/6$$

10

and in the next period

$$x(n+1)_6 = \sum_{c=n-4}^{n+1} (x(c)_6)/6$$

This method places an equal weight (or smoothing) on all the past data. If there is a gradual rising or falling trend reflected in the latest data, the forecast will be very slow to respond to it. From a computational point of view, the amount of data that has to be stored in order to compute the moving average is a definite disadvantage.

4.3.2. Exponential Smoothing

4.3.2.1 The Exponential Smoothing Equation

Exponential smoothing was first developed by Brown (2) (3) and this method has the advantage that the minimum amount of information has to be stored for each item.

The equation is

$$NF = \alpha ND + (1 - \alpha)OF \quad \text{--- (1)}$$

Where NF = new forecast

ND = new demand information

OF = previous forecast

α = smoothing coefficient = alpha

Alpha (also known as the smoothing factor) is set between the values zero to plus one.

Since alpha is set to 0.2 (20%) one can

interpret this as ...

"Add 20% of the latest demand
to 80% of the old forecast
to generate the forecast for the
next period."

Thus in each period, only 20% of the latest demand information is fed into the forecast. This has the effect of considerably dampening fluctuations in demand level from month to month.

Brown (2) has shown that equation 1 is equivalent to a linear combination of all past demands, where the weight given to each past demand decreases geometrically with age. The exponential smoothing system is quite flexible:

When alpha is very small, the forecast function behaves like an average with a great deal of past data (its response to change is very slow). When alpha is large, the forecast function responds rapidly to change.

4.3.2.2 Selecting A Smoothing Factor

The smoothing factor used, produces an average in which the weight for past observations decreases geometrically, whereas the moving average weights the N most recent observations each with 1/N. Table 1 from Brown (2) shows the relationship between the smoothing factor and the equivalent number of observations in a moving average.

The relationship is given by:

$$\alpha = \frac{2}{N + 1}$$

TABLE I
RELATIONSHIP BETWEEN NUMBER OF OBSERVATIONS IN A MOVING
AVERAGE AND THE SMOOTHING PARAMETER

N	$\Delta t p h_s$
3.0	0.5
4.0	0.6
5.0	0.33
5.78	0.3
6.0	0.285
8.0	0.2
12.0	0.154
16.0	0.105
19.0	0.1
25.0	0.08

From (27) points out that if a trial run on actual data indicates that alpha should exceed 0.1, then the data should be treated as if they were a significant trend or seasonal pattern. In this instance, $\Delta t p h_s$ is 0.10 and $\Delta t p h_s$ is 0.10 and $\Delta t p h_s$ is 0.10.

4.2.1. Forecast Terms and Terms

In order to model the time series, the following terms are necessary in the model. The forecast terms are given by the following:

$$F_t = Y_t - O_t$$

Where F_t = Forecast error at period t

O_t = Actual observed Air for test t

F_t = Forecast error at period t
made at period t-1

By making use of equation 1, the average error can be efficiently calculated in each period, using the minimum of data. In this case a smoothing factor - gamma - is used ($0 < \gamma < 1$). Note that gamma could be equal to alpha but this is not necessary.

$$\bar{E}_t = \gamma(E_t) + (1 - \gamma)\bar{E}_{t-1} \quad \text{--- (3)}$$

Where $\bar{E}_t$ = smoothed average error in period t

$\bar{E}_{t-1}$ = smoothed average error in period t-1

Similarly, the smoothed mean absolute error can be calculated:

$$\bar{MAD}_t = \gamma(|E_t|) + (1 - \gamma)\bar{MAD}_{t-1} \quad \text{--- (4)}$$

Where $\bar{MAD}_t$ = smoothed mean absolute error in period t

$|E_t|$ = absolute error in period t

$\bar{MAD}_{t-1}$ = smoothed mean absolute error in period t-1

The trend in the forecast is defined as:

$$T_t = F_t - F_{t-1}$$

The smoothed average trend can be calculated in a similar manner:

$$\bar{T}_t = \gamma(T_t) + (1 - \gamma)\bar{T}_{t-1} \quad \text{--- (5)}$$

Where T_t = current trend in period t

$\bar{T}_t$ = smoothed average trend in period t

$\bar{T}_{t-1}$ = smoothed average trend in period t-1

Tracking signals were developed to monitor the performance of the forecasting models. They are used to show when the forecasting model is out of control. A number of formulas have been proposed, but the one first proposed by Irig (13) has received widespread acceptance.

$$TS = \frac{\sum_{t=1}^n (F_t - A_t)}{\sum_{t=1}^n |F_t - A_t|} \quad (5)$$

This tracking signal TS fluctuates between plus and minus unity. When the forecasting system is under control, TS will fluctuate about zero. It will move towards plus or minus unity, according to the direction of the bias in the forecasting errors.

4.3.3 Adaptive Forecasting - Irig and Lanch Method

One of the disadvantages of the models discussed above is the fact that their performance has to be monitored, and multiple forecasts produced, when the forecasts go out of control. In a situation where the demand for thousands of items is being forecasted, the number of exception messages, and amount of manual intervention required to keep the system going, could be enormous. Some authors, therefore, started developing models whereby the smoothing factor α , is varied automatically to allow the model to respond to change.

The Irig and Lanch (14) model proposed that α be varied in proportion to the amount of bias being obtained in the forecasts. This results in the model having the following characteristics:

- 16
- a) Forecast bias low — then alpha small
 - model stable with slow response to changes in demand
 - b) Forecast bias high — then alpha large
 - model has rapid response to changes in demand

This model makes use of the tracking model defined in equation 6 in 4.3.2.4.

Since the absolute value of the tracking signal fluctuates between zero and unity, and it approaches unity when the forecast errors are large, Tripp and Leach proposed a model where

$$\alpha = 1/TS$$

Tripp and Leach (14) point out that the rate at which the system will respond to changes is affected by the value of gamma, where gamma is used for smoothing the average error and mean absolute deviation. A value of gamma between 0.05 and 0.1 is recommended; higher values leading to instability.

4.4.2.4. Dennis' (5) Run Length Control Model

Dennis (5) proposed a model using the exponential smoothing equation, but controlling it on the basis of "Runs" of errors. The model counts the number of consecutive times a positive or negative forecasting error is obtained, and compares this against a preset parameter. If the length of the run exceeds the value of the preset parameter, alpha is adjusted upwards. An error of either zero or opposite sign is used to indicate the end of a run and the value of alpha is then immediately reset to its base value.

Dennis (5) reports on a test comparing this model to one proposed by Whybark (15) (a model where the forecast error is compared with the standard deviation of the forecast error, and alpha is adjusted on the basis of

this comparison). He shows that the run based model performed better than the Whybark model. He points out that the model is computationally efficient and easy to understand.

4.2.2. A Forecasting Model

4.2.2.1. A Simple Forecasting Model

The use of a forecasting model is necessary in order to detect real changes in demand. When a real change happens, the signal must indicate this change to the person in charge of forecasting. A model might be required, or alpha might have to be reset to a higher value for a few periods to allow the model to adjust rapidly to the new situation.

Trigg's (13) tracking signal is widely used to indicate when a real change occurs and Batty (1) produced a table of cumulative probabilities for use with the tracking signal. An observer may then determine the statistical confidence in his hypothesis that a significant change has taken place in the mean level of demand.

TABLE 2¹
SINGLE EXPONENTIAL SMOOTHING
CUMULATIVE PROBABILITY TABLE FOR VARIOUS VALUES OF ALPHA

CUMULATIVE PROBABILITY	TRACKING SIGNAL			
	$\alpha = 0,1$	$\alpha = 0,2$	$\alpha = 0,3$	$\alpha = 0,4$
0,7	0,24	0,33	0,44	0,53
0,8	0,29	0,40	0,52	0,62
0,85	0,32	0,45	0,57	0,67
0,9	0,35	0,50	0,63	0,72
0,95	0,42	0,58	0,71	0,8
0,96	0,43	0,60	0,73	0,82
0,97	0,45	0,62	0,76	0,84
0,98	0,48	0,66	0,79	0,87
0,99	0,53	0,71	0,82	0,92

¹ Source : Batty (1)

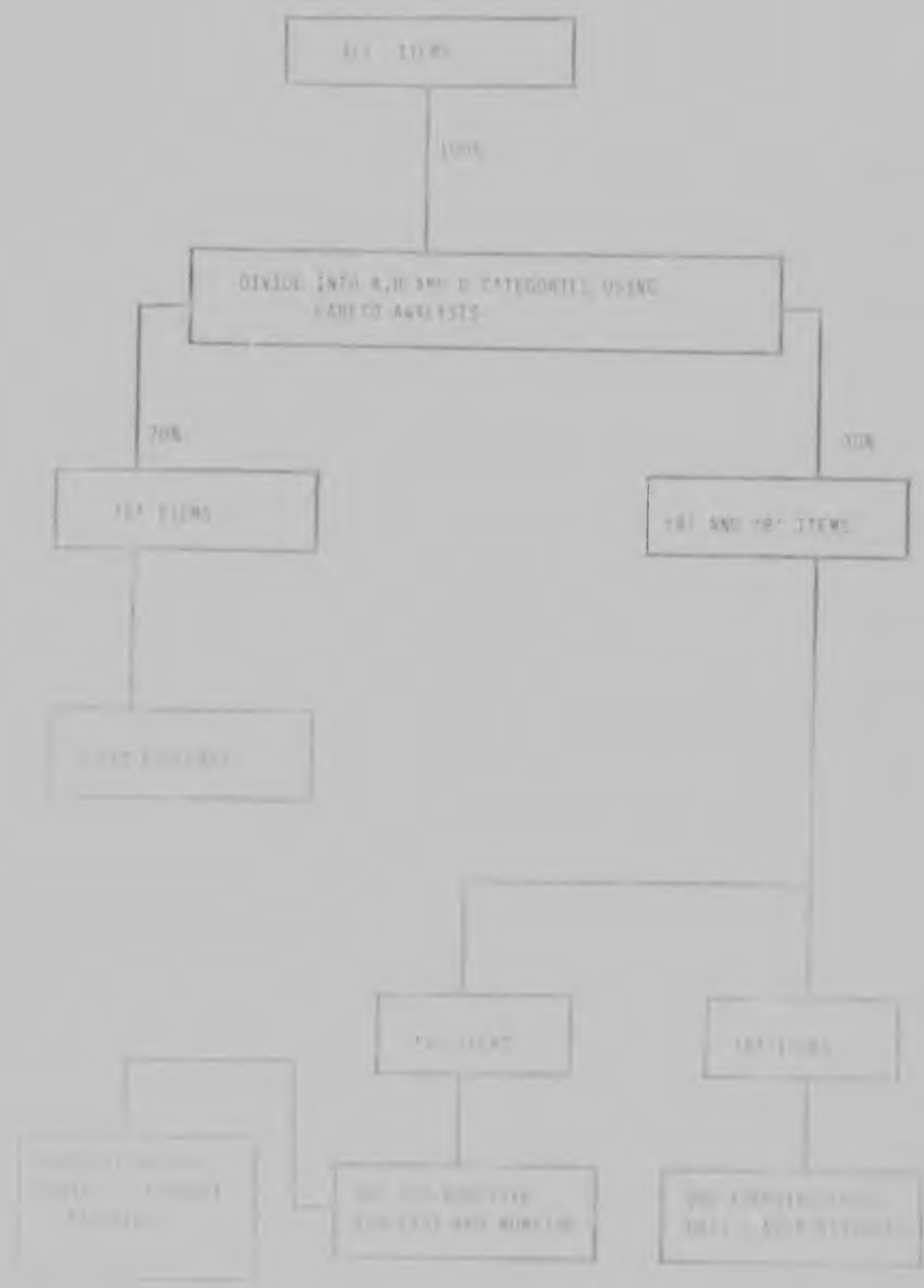


FIGURE 1
MOVIE ITEM FORECASTING PROCEDURE

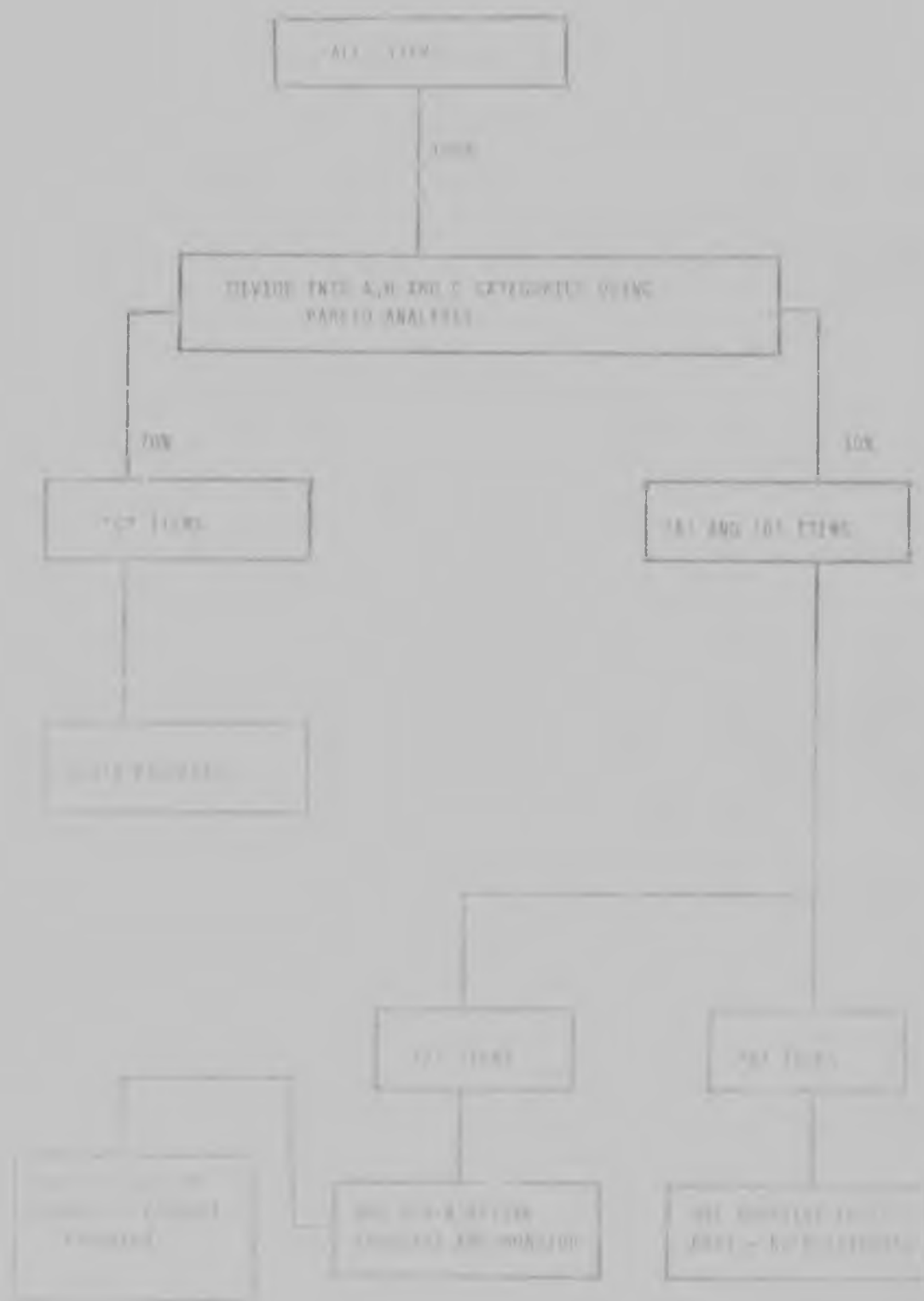


FIGURE 1
 A. LOW AND HIGH TIME FORECASTING PROCEDURE

Brown calculates

$$K = \frac{D_t - F_t}{S.D.}$$

Where D_t = demand in period t

F_t = forecast of demand for period t

S.D. = standard deviation of forecast error

Brown shows that when $K > 3.5$ (for tight control) the value D_t can be treated as an outlier. In this case D_t can be filtered and reset as follows:

$$\text{Filtered } D_t = F_t + 3 (S.D.)$$

The sign in the above equation will depend on whether

$$D_t > F_t \text{ or } D_t < F_t$$

4.6 Order Point And Order Quantities

Classical inventory control is based on using an order point/ order quantity system for ordering independent demand items (see section 3.2 for the definition of independent demand). This theory has been well developed and is summarised below.

$$OP = DDLT + SS$$

Where OP = order point

DDLT = demand during lead time

SS = safety stock

The order point can be recalculated as frequently as required and the advantages of frequent recalculation will be shown in section 7.

Every time the stock-on-hand plus stock-on-order drops below the order point, one order quantity is ordered from the factory.

The safety stock is calculated from the mean absolute deviation of the demand. The details are given in section 4.7.

This system is based on a set of rules to define the workings of the model. These rules must define:

- a) How to calculate DDLT
- b) What quantity to order

Proposed rules are developed in section 7.

Service Level and Safety Stock

A number of definitions of service level exist and only used by BOART is:

$$S.L. = \frac{N^{\circ} \text{ of orders delivered from stock}}{N^{\circ} \text{ of orders received}}$$

The target service level is set at 95%.
Safety stock is held as a buffer against variation in

- a) Lead time from the factory
- b) Demand from the customer

The amount of safety stock held is dependent on:

- a) Demand variability as measured by mean absolute deviation;
- b) Service level;
- c) Ratio of lead time period to demand interval period

Extract of the tables of safety stock factors and a sample calculation are shown in Appendix 5.

Table 3 overleaf indicates the safety stock required for the six top 'A' items (note that the safety stock forms only part of the actual stock holding). These results are strictly only true for demand distributions that are symmetrical and therefore the safety stocks calculated for the first two products (where demand is changing rapidly) are not applicable. A management decision must be made on the stocking policy to be followed. This could be based on a contract with the customer, in the case of the first product, where one customer accounts for 86% of the demand. In the case of the second product, account must be taken of the variation of customer demand and stock holding determined accordingly.

TABLE 3
SAFETY STOCK REQUIREMENTS

Days	% A.B.	Lead Time Adjustment Factor	Safety Stock Factor	Safety Stock	24 Month Average Sales
11	100	1.63	1.60	1215	643
12	97.5	1.63	1.60	958	498
15	90	1.63	1.60	287	150
18	80	1.63	1.60	376	216
21	65	1.63	1.60	190	102
24	50	1.63	1.60	52	28
24 Month Average	100	1.63	1.60	1495	803

Days = Lead Time A = 4955 units

Percent A.B. = 100 - Days x 100

A. B. Lead Time Factor (Table 3)

The following method of computation will be used to determine safety stock:

- The mean is the arithmetic mean of daily demand for 24 months of the year. The standard deviation is the square root of the variance. This gives the amount of safety stock that has to be kept.
- The mean monthly demand over the period is determined as above. Only 18 days are used for horizontal demand.
- Standard deviation is a graphical representation of the dispersion of the data. A '5-month' forecast is given by a linear forecast, as it gives stability to forecasting and thus forecasting is needed.
- A forecast of the leading index is desired as this indicates the direction of the forecast. Following the actual data very closely.

5. REVIEW OF THE TEST DATA

5.1 Extraction of the Data

For the purpose of this study, the sales data for one product group was chosen. The product group represents approximately 10,000,000 sales per month. Production planning and inventory control staff experienced numerous problems with this group of data and are in the process of determining future needs.

The monthly sales data was extracted from a Microsoft Access 2.00 database and converted to a flat file. All the data was then used in the development of the program.

Figure 2 gives an overview of the system used.

The following program is used:

- The program "P1" takes as an input a file containing the required product group and outputs the data to a file. The data is then used for the production planning and inventory control.
- The program "P2" takes as an input the data, and outputs the data to a file. The data is then used for the production planning and inventory control.
- The program "P3" takes as an input the data, and outputs the data to a file. The data is then used for the production planning and inventory control.
- The program "P4" takes as an input the data, and outputs the data to a file. The data is then used for the production planning and inventory control.
- The program "P5" takes as an input the data, and outputs the data to a file. The data is then used for the production planning and inventory control.



FIGURE 2
DATA EXTRACTION AND ANALYSIS SYSTEM FLOW CHART

TABLE 4
A-B-C RANKING COMPARISON

PRODUCT	Aug '80 To Jan '81	May '80 To Oct '80	Feb '80 To Jul '80	Nov '80 To Apr '80	Aug '79 To Jan '80	May '79 To Oct '79
P2	A1	A1	A4	B2	A12	A10
P3	A2	A2	A1	A2	A4	A3
P4	A3	A5	A3	A3	A2	A2
	A4	A6	A9	A13	B5	B2
	A5	A7	A6	A8	A13	B5
	A6	A9	A11	A12	A10	A12
P1	A7	A3	A2	A1	A1	A1
	A8	A10	A10	A9	A7	A6
P6	A9	A8	A7	A7	A6	A7
	A10	A11	A13	A16	B1	B3
	A11	A4	A5	-	B6	A15
	A12	A14	A12	A4	A5	A5
	A13	A13	A16	A5	A3	A4
	A14	B6	-	-	-	-
P5	A15	A15	A8	A6	B4	B1
	B1	A12	A15	A11	A9	A13
	B2	B7	B1	A10	A8	A8
	B3	B4	A17	A14	A11	A14
	B4	A16	B7	B14	-	-
	B5	B12	B9	B10	-	B12
	B6	-	-	-	B7	-
	B7	B9	B8	B1	B9	B8
	B8	B10	B4	B6	-	-
	B9	B5	B6	B13	B14	-
	B10	-	-	-	-	-
	B11	B14	B17	B8	B13	B6
	B12	B3	B5	B20	-	-
	B13	B15	B14	B19	B15	-
	B14	-	-	-	-	-

TABLE 5
DEMAND CHARACTERISTICS

	(1)	(2)	P1	P4	P5	P6	GRAND TOTAL SALES
DEMAND VARIABILITY ¹			X	X		X	X
NUMBER OF CUSTOMERS ACCOUNTING >75% OF DEMAND ²	7	X					
LUMPY DEMAND ³	X	X					
DEMAND HIGH	X	X				X	
DEMAND MEDIUM			X	X	X		X
DEMAND LOW							

Extracted from Appendix 2.

Extracted from Appendix 3.

ments can be made to meet the demand.

28

The rankings shown in Appendix 3, Table 1, of the items are fairly stable over time. This table provides an indication of the relative importance of items from B to A category of items. Changes in stock holding policies might be made to meet the demand.

5.4.2 Demand Vulnerability

Appendix 3 Table 1 shows the relative importance of items. 75% of items are in the B category. This means that:

- a) Stockholding policies need to be revised to meet the demand.
- b) Demand forecasting need to be revised to meet the demand.

Generally, items are in the B category. This means that items are in the B category. They are equally likely to be in the B category as in the A category.

Bulk is generally vulnerable to the demand change. Its very strength is in fact a major weakness.

5.4.3 Major Demand Changes

Any major change in demand must be predicted manually. It is impossible for a forecasting system based on past history to do this. When major changes occur, the manual forecast, or a combination of manual and exponential smoothed forecast should be used. This is clearly evident in Figures 3 and 4 in Appendix 1.

TABLE 6
RESULTS FROM THE SELECTED FORECASTING MODELS

PRODUCT	Model	Alpha	P*	% Forecast Error	Tracking Signal	Demand Variability %
P1	2	0,1	N/A	7,1	0,05	86
P2	6	0,2	2	-17,0	-0,48	94
P3	6	0,2	2	-0,14	0,27	36
P4	2	0,2	N/A	0,1	-0,02	44
P5	5		N/A	0,19	0,5	59
P6	2	0,2	N/A	1,3	0,01	47

*P is the number of allowable periods of consecutively signed forecast errors.

6.2 Demand Spike.

- a) Manually filter the demand figures to reduce their effect on the model, and
- b) Place factory orders for the spike based on marketing information.

7. INVENTORY SIMULATION

7.1. Introduction

In order to test the effectiveness of the foregoing techniques, a simulation was carried out on the data of the actual stock on hand at the end of January 1981, starting with the stock figures for April 1980, and the sales figures for May 1980 to January 1981.

This theoretical stock was compared to the actual stock to measure the improvement.

7.1.1 Existing Ordering Procedure

The existing ordering procedure is as follows:

- a) An order point is determined periodically (every three to six months) and is set equal to three times the past six month's average sales).

- b) Factory orders are determined by:

$$\text{Factory orders} = \text{order point} + (\text{stock on hand} + \text{stock on order})$$

The factory order is rounded to the nearest fifty or one hundred units depending on the item.

- c) In addition, the carrier's order card is used based on the following:

Copy of the actual inventory of the store and one of the warehouse person.

7.1.2 Proposed Ordering Policy

The proposed policy and procedure, described as a statistical calculation of order point. To do this, a statistical measure of the order point, statistically significant, is based on time series analysis.

From the information presented in sections 4.6 and 4.7, the order point will be calculated as follows:

$$OP = DDLT + SS$$

Where OP = Order point
 DDLT = Demand during lead time
 SS = Safety stock

7.2.1 Assumptions

- Lead time is eight weeks.
- A service level of 90% is required.
- The review interval is four weeks.
- The factory order quantity will always be a multiple of one month's forecasted demand rounded to the nearest 100 units.

Appendix 2.1 Review Interval

- One order quantity will be raised whenever the stock-on-hand plus stock-on-order drops below the order point.
- The order point will be recalculated every three months and be based on the past six months' data. Appendix 2.2 contains the monthly average sales, average mean absolute deviation, calculated at three month intervals.
- The average sales will be used as a forecast.
- The mean absolute deviation will be used to calculate the safety stock.
- The initial order point in April 1980 is based on the past twelve months' data (Appendix 2.3).

Appendix 9.12, Tables 95.4 to 95.6 give the results of this exercise. Table 95.4 compares the results of this simulation with the actual stock in January 1981.

- The total value of the 'X' items listed in Table 7.2 approximately equals the inventory in January 1981.
- A parallel picture of the 'X' items.
- In the case of the 'X' items, the simulated stock levels for the 'X' items are in line with the inventory levels. However, in the real life situation, inventory levels are not in the factory - some of it is held at a customer's premises.

Table 7.2

Table 7.2: Comparison of the 'X' items in the inventory in January 1981 with the results of the simulation.

Item	Actual Value Jan 1981	Simulated Value Jan 1981	Actual Value Jan 1981	Simulated Value Jan 1981	Relative Difference %
01	1071	1100	1071	1100	2.7%
02	707	711	707	711	0.6%
03	891	1000	891	1000	12.2%
04	1001	1000	1001	1000	-0.1%
05	447	441	447	441	-1.3%
06	97	117	97	117	20.8%
TOTAL 'X' ITEMS			4184	4179	-0.1%

7.3 Continuous Review of the Order Policy

In this case, the selected inventory numbers from section 6 will be used to continuously approximate some parts.

7.3.1 Assumptions

- Lead time is eight weeks.
- A service level of 90% is required.
- The demand interval is four weeks.

Appendix 7.1, Tables 25.1 to 25.6 give the results of this exercise. Table 7 below compares the results of this simulation with the actual stock in January 1981.

- The total value of the 10 items listed in Table 7 represents 9% of the inventory in January 1981.
- A possible saving of £,000 a year.
- In the last 10 days of the year the simulated stock levels are in the region of 10% of the value of the actual stock. This is due to the fact that the demand is increasing steadily. Currently, in the region of 10% of the actual stock, the demand is increasing steadily. This is due to the fact that the demand is increasing steadily.

Table 7
Comparison of the results of the simulation with the actual stock in January 1981

Item	Stock Jan 1981	Value Jan 1981	Simulated stock Jan 1981	Value Jan 1981	Simulated stock Jan 1981	Value Jan 1981
1	1000	1000	1000	1000	1000	1000
2	200	200	200	200	200	200
3	300	300	300	300	300	300
4	400	400	400	400	400	400
5	500	500	500	500	500	500
6	600	600	600	600	600	600
7	700	700	700	700	700	700
8	800	800	800	800	800	800
9	900	900	900	900	900	900
10	1000	1000	1000	1000	1000	1000
Total 10 items						

7.3 Conclusions, Review of the order policy

In this case, the selected inventory model from section 6 will be used to continuously review the stock position.

7.3.1 Assumptions

- Lead time is eight weeks.
- A service level of 90% is required.
- The demand interval is four weeks.

- d) The factory order quantity will always be a multiple of one month's forecasted demand rounded to the nearest fifty units.

7.3.2 Ordering Rules

- a) One order quantity will be raised whenever the stock-on-hand plus stock-on-order drops below the order point.
- b) The order point will be recalculated every month and be based on the forecasted demand. Appendix 8.1, Table 17.2 shows a sample of the monthly forecast and mean absolute deviations used to recalculate the order points in Table 26.1.
- c) The mean absolute deviation will be used to calculate the safety stock.

TABLE 8
STOCK STATUS AT END OF SIMULATION RUN

PRODUCT	Forecast	Safety Stock	Simulated Stock	Simulated Stock On Order	Months Stock On Hand	Months Stock On Hand and On Order
P1	260	743	1360	-	5,3	5,3
P2	982	805	(430)	3600	-	3,2
P3	291	234	634	350	2,2	3,4
P4	256	254	437	550	1,7	3,85
P5	53	151	301	100	5,6	7,5
P6	41	57	75	100	1,8	3,4

7.3.3 Results

The detailed results are shown in Appendix 9.2; Tables 26.1 to 26.6 and are summarised in Table 9 (overleaf). The results from Table 7 have been included for comparison purposes. There is a substantial reduction in inventory usage, the maximum receipt of the order point. Inventory has dropped by 38,7%. Table 8 shows the stock status at the end of the simulated run. Despite the 38,7% drop in inventory, the stock status is acceptable.

7.4 Selection Of One Forecasting Model

Table 8 shows that best results selected from the various forecasting runs using different models (Refer to Appendix 8). In the real life situation, it would be preferable to have one model in use, rather than the three used, to derive the results in Table 8. The principle advantage will be simplicity and ease of understanding, by all concerned, of how the forecasting model operates. Overall, the best results in Table 9 were obtained with models two and six. The principle difference between the two models is in the method of control.

7.4.1 Model Two

Level control is controlled by monitoring the tracking signal. An order is issued, the tracking signal is allowed to exceed the pre-set limit value (for a 95% confidence level - Table 9) for consecutive periods. In the first period, z is reset to 0,8, and held at that level until the tracking signal dropped below the alarm level. This method can therefore be made more, or less sensitive by increasing, or decreasing the number of periods allowed before z is reset.

TABLE 1
Summary of the Results of the Review of the 1981-82
Annual Budgetary Results

Product	Actual Exp. (Jan. 1981)	Stock Value (Jan. 1981)	FUTURE REVIEW			CONTINUOUS REVIEW		
			Estimated Costs (Jan. 1981)	Actual Expenditure (Increase)	Value of Reduction (Decrease)	Estimated Costs (Jan. 1981)	Actual Expenditure (Increase)	Value of Reduction (Increase)
P1	1785	14225	2375	(1579)	(70029)	2380	(254)	(7712)
P2	12	205	(3420)	-	-	(522)	-	-
P3	1705	51045	584	722	11911	584	1072	25782
P4	808	15745	589	412	2587	432	121	2022
P5	411	12115	110	220	7719	121	775	1611
P6	207	270	100	181	15000	100	27	1001
TOTAL					8715			

Model Six

Model six (which uses the same forecasting equation as model two, equation 1, section 4.3.2.1), is controlled only on the basis of the number of consecutively signed forecast errors. Thus, two consecutive forecast errors of the same sign can be used to indicate that the forecast is out of control. In the various results used in this work, tests using two, three and four periods of consecutive, similarly signed forecast errors were tried. In general, as the number of periods increase, this model becomes less and less responsive to change.

Model Selected

Table 10 shows a comparison between the optimum results detailed in Table 9 and the results obtained using model six for all items.

Table 10 shows that there is a small loss of optimization, particularly for P3 where the simulated stock has increased by two hundred units (a cost increase of R4 812). The results for P5 are exactly the same. The stock of P1 has increased by three hundred and fifty units (R4 640) although, in the real life situation it would be hoped that the end of the demand spike would be foreseen and the model adjusted (by manually resetting alpha to say 0.05 for a few periods or by overriding the order point calculation). Note that in fact this fall off in optimization as the actual stock was only 1 096 in January 1981.

A similar situation occurs for P2 where the simulated stock is negative (ie understocked). In the real life situation, this would indicate that sufficient factory capacity is not provided to cover customer demand.

TABLE 10
COMPARISON OF THE BEST SIMULATED STOCK RESULTS
WITH ONE COMMON MODEL

Product	Model	Alpha	Control Period	Simulated Stock	Simulated Stock for Order
P1	2	0.1	-	1380	-
P1	2	0.2	-	1735	-
P2	6	0.2	2	(430)	3600
P2	2	0.2	-	(1030)	4060
P3	6	0.2	2	634	350
P3	2	0.2	-	834	350
P4	2	0.2	-	437	550
P5	5	-	-	301	200
P5	2	0.2	-	301	100
P6	2	0.2	-	175	100

This work only have been done on either customer orders received or information from marketing. In either case they would signal to the forecaster that the model will require adjustment to reflect the new level of demand. The fact that the simulated stock goes negative is important in that it indicates clearly that a forecasting system cannot operate in isolation. Marketing information is an essential part of the total forecasting system.

The tracking signal model for alpha = 0.2 appears to be a good tracking model for the data tested. It would also produce a 28.7% reduction in inventory level for the 28 January 1971.

Table 11. Summary of Tracking Model Two

- the tracking factor = 20 units
- the quantity factor = alpha
- the allowable limits for the tracking signal (from Table 2)

- c) The number of consecutive periods in which the tracking signal is allowed to exceed the limits. (Determined from Table 2).
- d) The value of the smoothing factor used when the tracking signal has exceeded the allowed limits for the specified number of periods.
- e) The smoothing factor for the forecast errors (generally set at 0,1).

The following test data was used:

- a) Alpha = 0,1; 0,2 or 0,3.
- b) 95% confidence limits for the factor alpha from Table 2.
- c) The tracking signal was allowed to go out of control for two consecutive periods before alpha was reset.
- d) Alpha was reset to 0,8 in all cases.
- e) Gamma was set at 0,1.

The following points should be noted:

- a) The principle method of monitoring the performance of the model should be by means of the tracking signal. The closer the tracking signal is to zero, the better the model is following actual sales data.
- b) Where demand spikes occur, judgement must be used in determining if the smoothing factor must be increased or if it should be held low and special orders placed to cover the spike only. This can only be determined from marketing information.
- c) A graph of both the forecast versus actual demand and the tracking signal should be maintained for all 'A' items. This will enable the forecaster to fit his model to what is actually happening.
- d) Exception reports must be produced every time the tracking signal indicates that the forecast errors are unacceptable. These reports should be referred to the product managers/ marketing for investigation.

The reasons should be clearly determined so that the outliers in the demand data can be discarded.

- e) The exception reports should show the items ranked in their A-B-C rankings to that the most important items are investigated first.

7.6 Forecasting Of 'B' and 'C' Items

A sample 'B' item was chosen and the forecasting results are shown in Appendix 9.4; Tables 28.1 and 28.2. There is very little difference between the models. The inventory simulations show that in all cases the same ending inventory is produced. This is mainly due to the large order quantity of fifty units, which is accepted as being the minimum factory order quantity desirable. [Altering the order quantity to the forecast quantity, rounded to the nearest ten units, reduces the final inventory (using model five) to seventy five units. This results in a reduction in inventory of ten units - refer to Table 28.2].

For 'B' items, the adaptive forecasting model of Trigg and Leach (model five) has distinct advantages. For these less important items, the use of an adaptive model allows more freedom for the forecaster to spend time on 'A' items. As suggested by Lewis (7), 'B' items can be forecasted in this manner and the only monitoring that is done is to set an arbitrary limit on the value of the tracking signal. Exception reports are then prepared for 'B' items whose tracking signals exceed this value.

The demand for 'C' items is highly erratic and it is suggested that these are handled strictly on a 'make to order' basis. No stock of 'C' items should ever be held.

7.7 Summary

- 7.7.1 A saving of between 24 and 38% of the inventory value at the end of January 1987 could have been achieved by the introduction of a forecasting system and the use of classification and reorder quantity techniques in April 1986.
- 7.7.2 The percentage of additional sales of the order point is 38.7% in 1986. The saving drops from 38.7% to 8.2% if the order points are revised every three months.
- 7.7.3 It is noted that the per cent saving for the best data results is less than of systemised. It is thought that this is due to the at the inventory status of each item and it will be easier to understand.
- 7.7.4 The system of monitoring the performance of the model for each item is suggested. The model for each item is suggested and model show the items ranked by their 3-5 classification.
- 7.7.5 It is proposed that all 'B' items be forecast using model five - the adaptive forecasting model, with monitoring done by limiting the value of the tracking signal. Exception reports should be generated on all items whose tracking signal exceeds the pre-set limit.
- 7.7.6 The inventory reorder rules are listed below:
- 7.7.6.1 'A' Items
- Calculate a new order point each month based on the latest forecast and smoothed mean absolute deviation.

- b) When stock-on-hand plus stock-on-order drops below the order point, order one order quantity.
- c) The order quantity is defined as the largest forecast rounded to the nearest fifty units.
- d) If one order quantity is insufficient to raise stock-on-hand plus stock-on-order to the order point level, place an order for another order quantity. (even if stock-on-hand plus stock-on-order is only just below the order point.)

7.7.6.2 'B' Items

Use the same system, except that the order quantity is rounded to the nearest ten units.

7.7.6.3 'C' Items

Make for firm orders only.

8. CONCLUSIONS

It is shown in this work that it is possible to improve the inventory situation by using a more sophisticated and more sophisticated inventory ordering system than the one presently in use.

8.1 It is suggested that an exponential smoothing model, controlled by a tracking signal as described in Appendix 7.1.2 be used to forecast demand and recalculate the order point every month for each 'A' item.

8.2 It is suggested that all 'B' items be forecasted by an adaptive smoothing model as described in Appendix 7.1.3. A limit should be set on the value of the tracking signal and exception reports must be produced if the tracking signal exceeds this value.

8.3 It is suggested that at least a 28.7% saving of the January 1981 inventory levels is possible, ie RBA 518. These savings are based on a customer service level of 90%.

8.4 Exception reports must be generated of all forecasts that are out of control. It is clearly demonstrated that the forecasting system cannot operate in isolation. Marketing information must be combined with the calculated forecast. This is necessary to:

- 8.4.1 Avoid stockouts when demand suddenly rises beyond previous forecasts.
- 8.4.2 Avoid stock increases when demand falls below previous forecasts.

8.5 Based on a number of B&W products it may be concluded that these products are heavily customer dependent. The type of demand must be closely monitored to avoid excessive stock. A further analysis of the 'A' items is needed to Appendix 2, providing complete indication of this demand.

- 8.6 Changes in customer demand from one item to another cause large spikes in the demand pattern. These spikes are not conducive to good stock control. Every effort should be made to track down the reasons for the spikes and, through customer liaison, to try to minimise them. The amount of safety stock carried is directly dependent of the variability in the sales data.
- 8.7 Regular A-B-C analysis should be carried out to determine when the forecasting policy should change.
- 8.8 The definition of a 'standard' product should be based on some cut off point in the A-B-C classification. Certainly all 'A' items should be considered as standard products. 'B' items up to 90% of the sales revenue could also be considered as standard.
- 8.9 'C' items should be handled on a 'make to order' basis only.

LIST OF REFERENCES

1. Betty, H. "Smoothing an Exponential Smoothing Forecasting System", Quantitative Research Quarterly, Vol 16, No 4, 1974.
2. Brown, R.C. "Forecasting, Control and Production of Discrete Time Systems", Warwick Hall, Englewood Cliffs, New Jersey.
3. Brown, R.C. "Forecasting, Control and Production", John Wiley and Sons.
4. Gray, W.D. "Effective Control of an Exponential Smoothing Forecasting System", Journal of Management Science, Vol 10, No 1, 1964.
5. Brown, J.B. "Development of a Fast and Effective Exponential Forecasting System", Production and Inventory Management, Vol 19, No 2, pp 23 - 40, 1978.
6. De Boer, D.A. "Exponential Smoothing - A Diagnostic Approach to Production Planning", Production and Inventory Management, Vol 19, No 1, 1978.
7. Lewis, C.D. "The Variability of the Exponential Smoothing Portfolio of Skills", Production and Inventory Management, Vol 19, No 2, pp 53 - 66, 1978.
8. O'Garra, F. "How Forecasting Affects the M.R.P. System", Production and Inventory Management, Vol 19, No 2, pp 21 - 42, 1978.

9. Orlicky, J. A. "Materials Requirements Planning Systems", International Business Machines Corporation, May 1971, Publication 9320-1170-0.
10. Plossl, G. M. "Manufacturing Control - The Last Frontier of Profit", Boston Publishing Co.
11. Strickon, D. B. "How to Design a Valid Forecasting System", Production and Inventory Management, Vol. 20, No. 1, pp. 17 - 26, 1980.
12. Thompson, R. L. "Applied Forecasting Methods", Prentice-Hall, Englewood Cliffs, NJ, 1980.
13. Wilson, G. M. "Monitoring & Forecasting System", Business and Research Quarterly, Vol. 17, No. 3, 1965.
14. Wilson, G. M. and Wilson, J. H. "Managerial Decision Making in Adaptive Distributed Control", IEEE Transactions on Systems, Man, and Cybernetics, Vol. 13, No. 3, 1983.
15. Wilson, G. M. "A Comparison of Methods for Forecasting Uncertainty", The Joint Data and Forecasting Office Bulletin, Vol. 10, No. 3, 1983.
16. Wilson, G. M. "Forecasting and Inventory Management in the Computer Age", IEEE Transactions, 10 - 1983.
17. Wilson, G. M. "Forecasting with the Uncertainty Adapted Moving Average", Forecasting Science, Vol. 6, 1980.

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GRA IED ES IATA I
TWENTY FIFTH MONTHLY 1981

APPENDIX 1.1

GRAPHED SALES DATA

APPENDIX 1.1

GRAPHED SALES DATA

The sales history for the top six 'A' items, and one 'B' item have been graphed. The selection of these items comes from the A-B-C analysis in Appendix 2.1.

1.1 Demand For P1

This product exhibits an exceptionally high peak in one period (five times the twenty four month average demand) and 86% of the demand comes from one customer. The distribution is highly skewed with more than 50% of the periods experiencing a demand of less than two hundred and fifty units. Clearly, from the graphed sales figures in this appendix, history provides no indication of the sudden rise in demand and time series analysis cannot forecast this increase. Forecasting models can be chosen that will try to follow the trend rapidly but some outside decision making is required to:

- a) Forecast the rise in demand subjectively.
- b) Decide if it is a real change of demand level, or purely a 'spike'.
- c) Decide if the forecasting model must be changed.

Demand vulnerability is extremely high because of:

- a) High demand variability and skew distribution, (ie very few periods with high demand).
- b) Customer dependency.

Stock policies must therefore be determined taking these facts into account.

1.2 Demand For P2

This product shows a rapidly rising demand towards the end of the twenty four month period under review. Time series forecasting cannot be used to predict the rise in demand, it can only try to follow the trend. Demand vulnerability is fairly

high because of the low number of customers and high variability in demand.

1.3 Demand For P3

This product is a good candidate for forecasting by time series analysis. Demand is essentially horizontal with fluctuations about a mean level. There is a slight shift in the mean during the second twelve month period. Demand variability is low and variability is lower than for the previous items as four customers account for most of the demand.

1.4 Demand For P4

Generally exhibits the same characteristics as those discussed in 1.3 above, although demand is more variable.

1.5 Demand For P5

Demand for this product is falling continuously through the twenty four month period. Further investigation might reveal that one customer's consumption was changing or being phased out, causing the drop in sales. Time series analysis cannot predict the start or end of the drop, but can attempt to follow it.

1.6 Demand For P6

A horizontal demand pattern is apparent for this product. Forecasting of demand should be possible using time series analysis. Demand vulnerability is extremely high as one customer accounts for 94% of the demand for this item. Stock holding policies must take this into account.

APPENDIX I

UNITED STATES SALES DATA

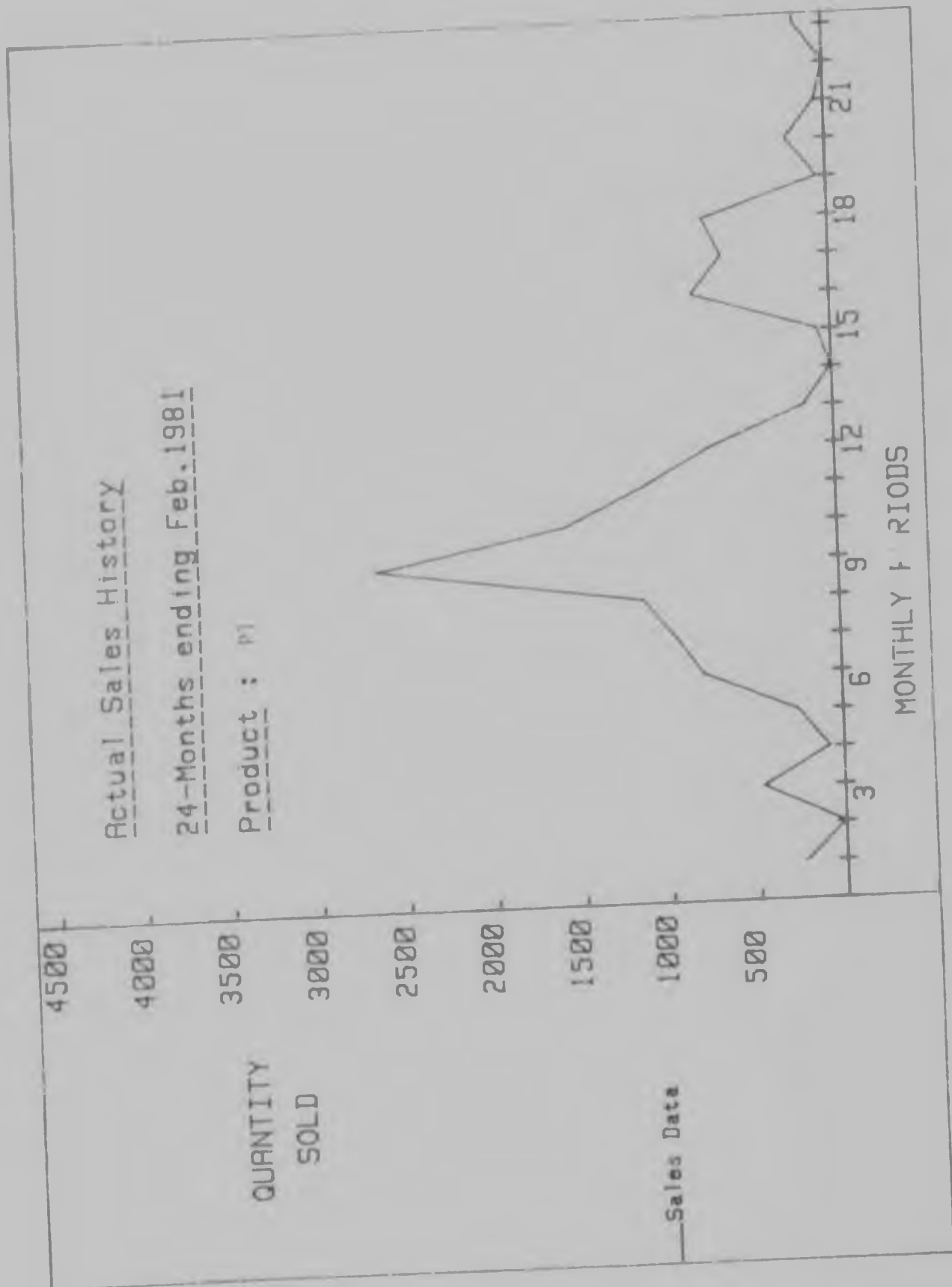


FIGURE 3

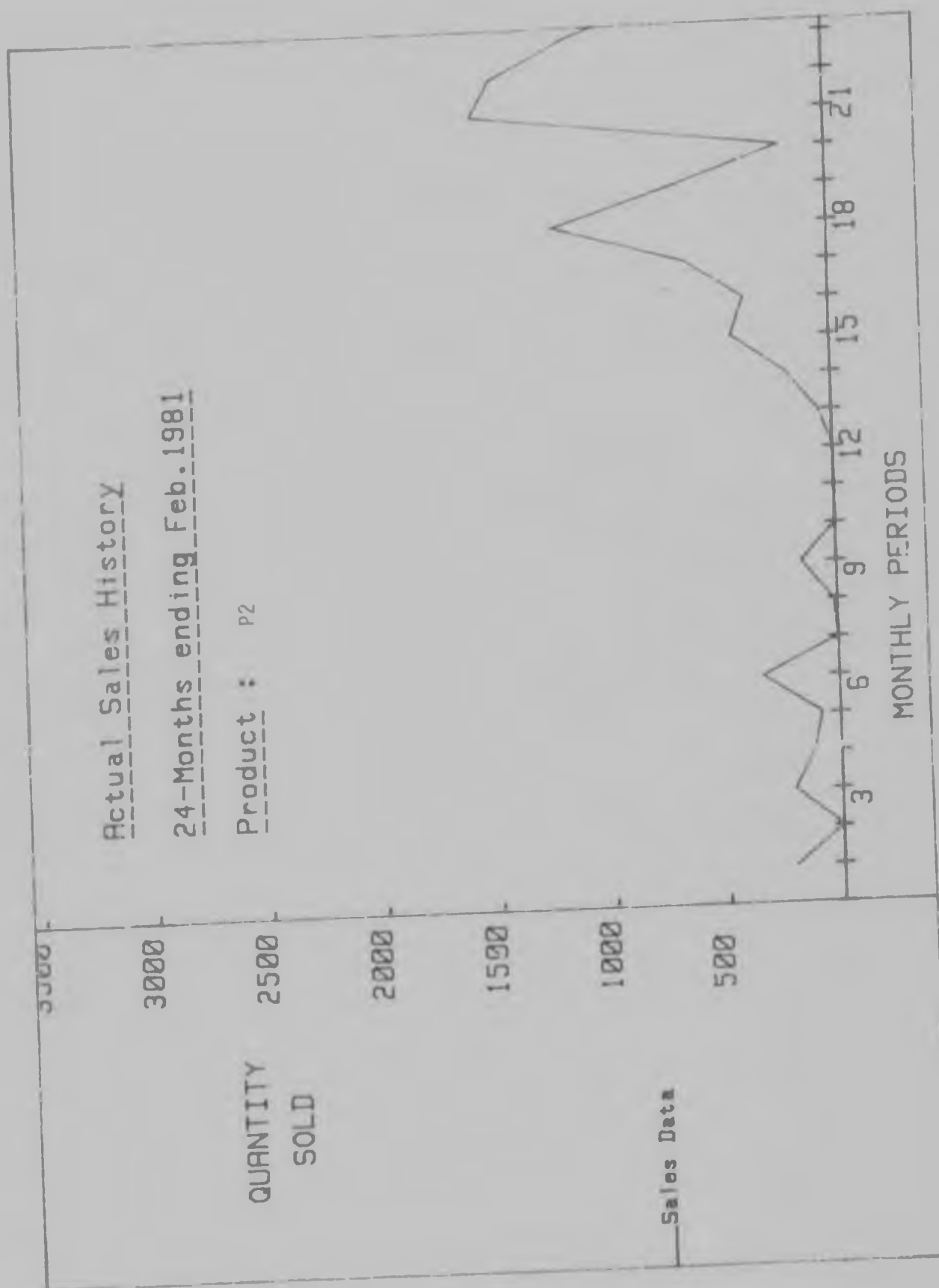


FIGURE 4

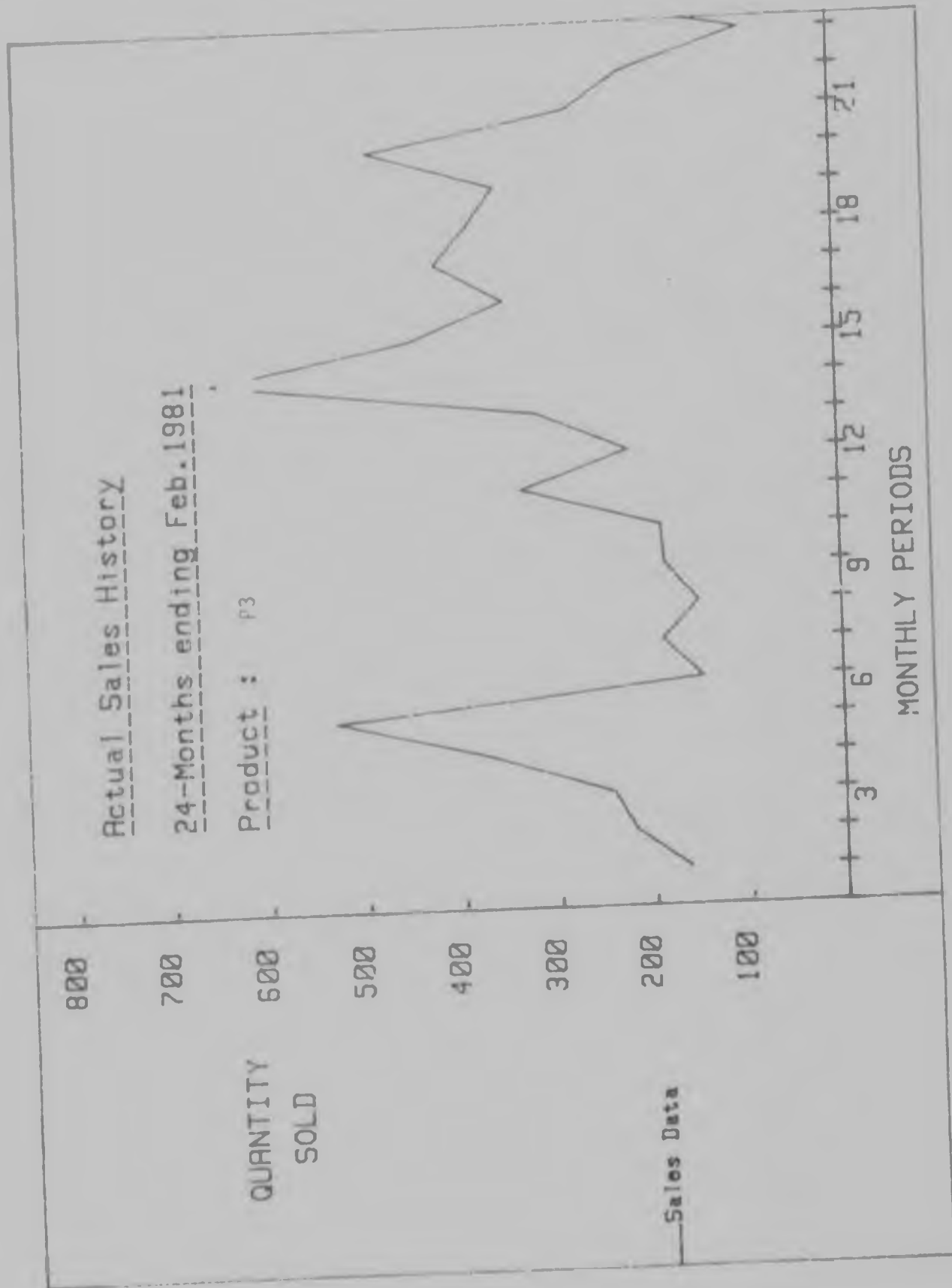


FIGURE 5

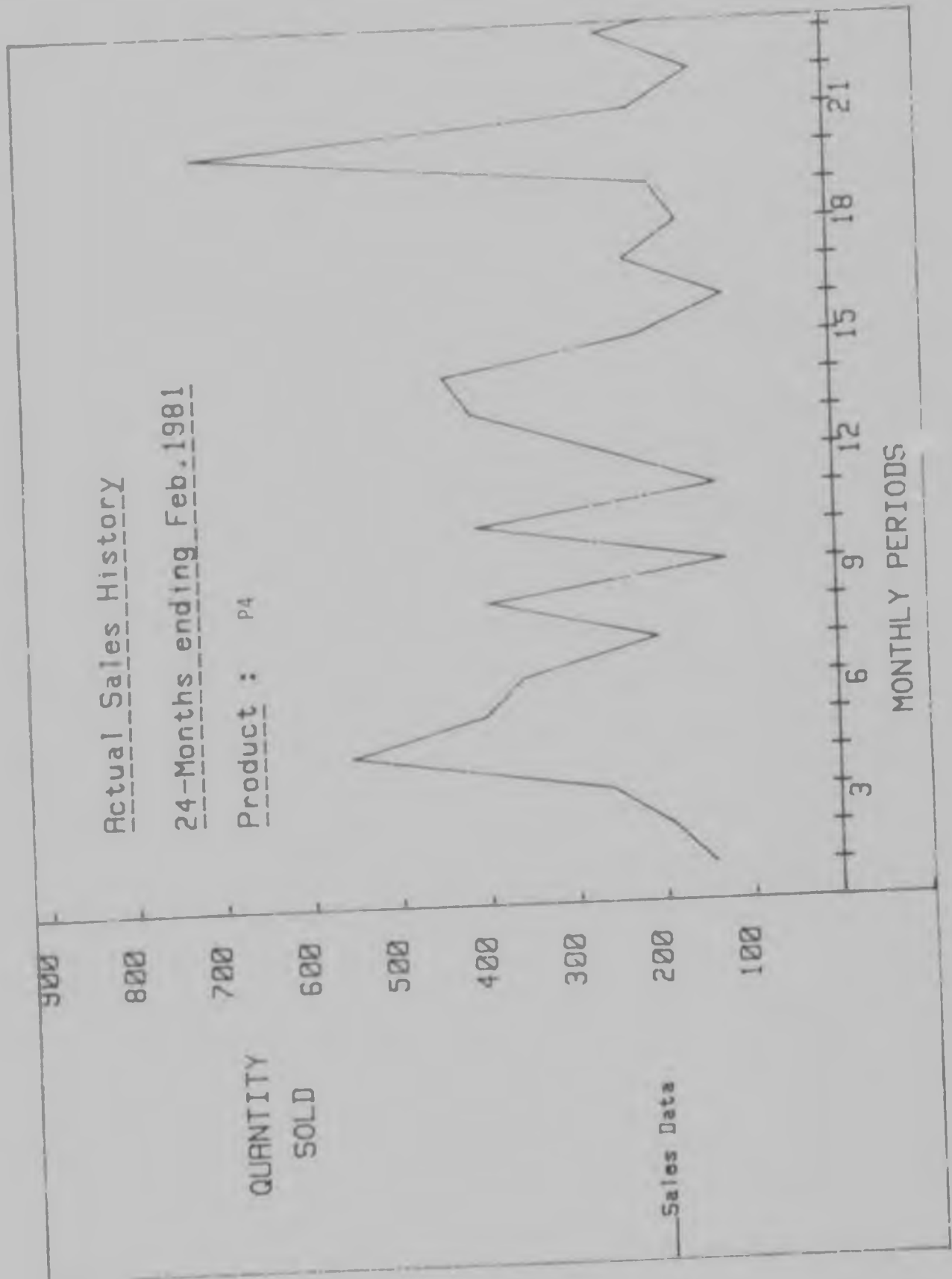


FIGURE 5

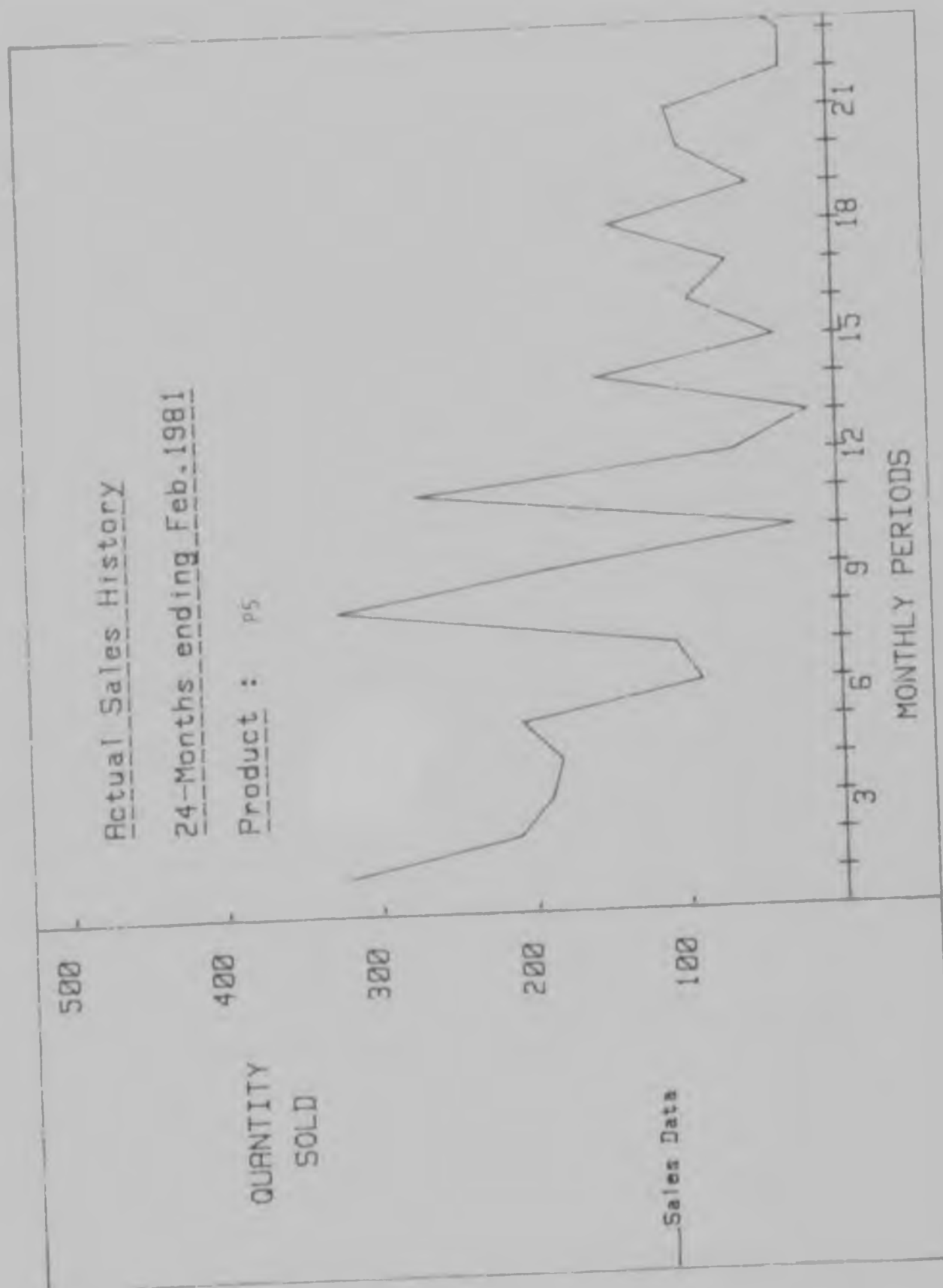


FIGURE 7

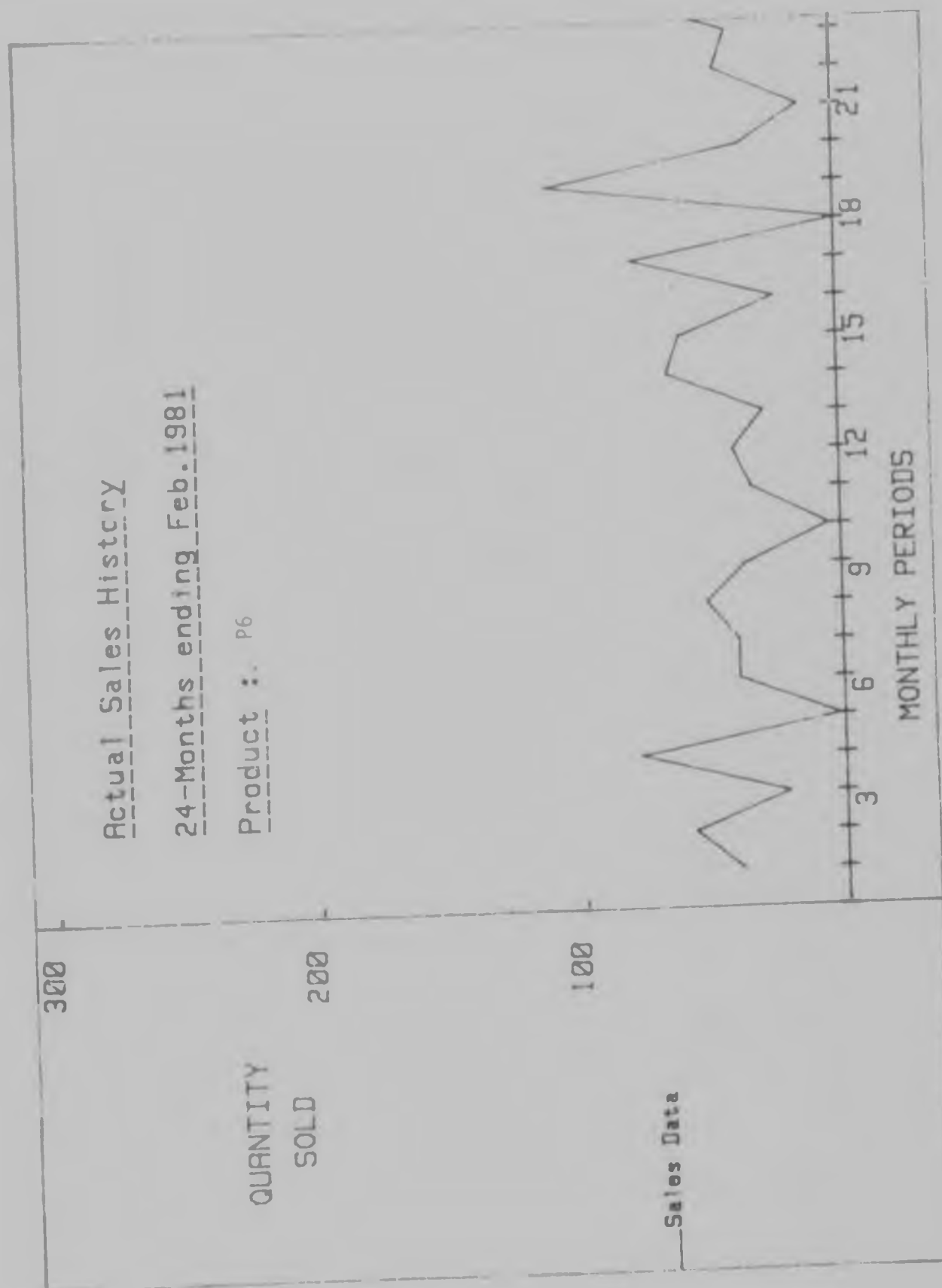


FIGURE 8

END V 1.2

TABLE 1.1. 1974 SALES DATA

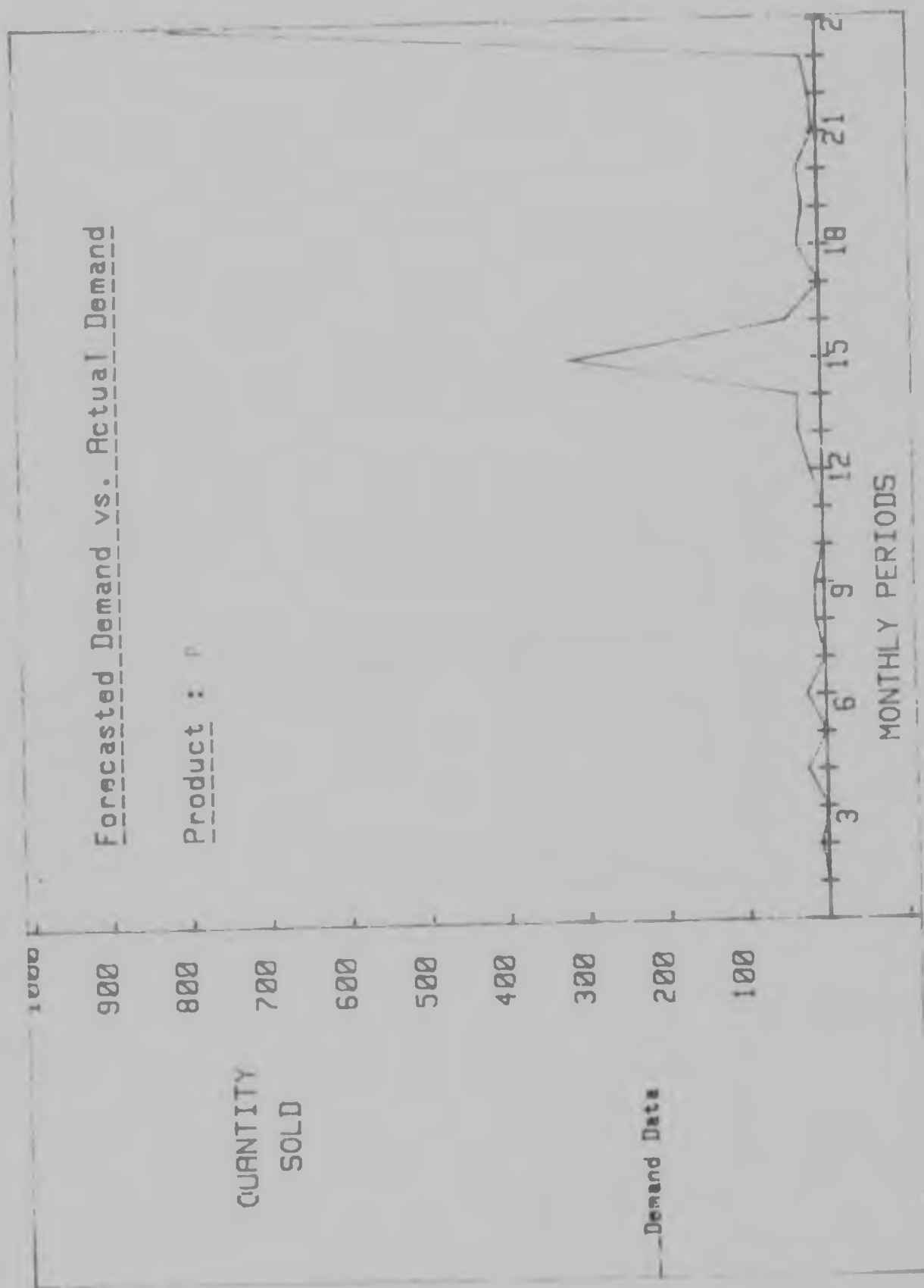


FIGURE 9

A IX 1.3

GRAND TOTAL SALES FOR TWENTY FOUR MONTHS
ENDING FEBRUARY 1981

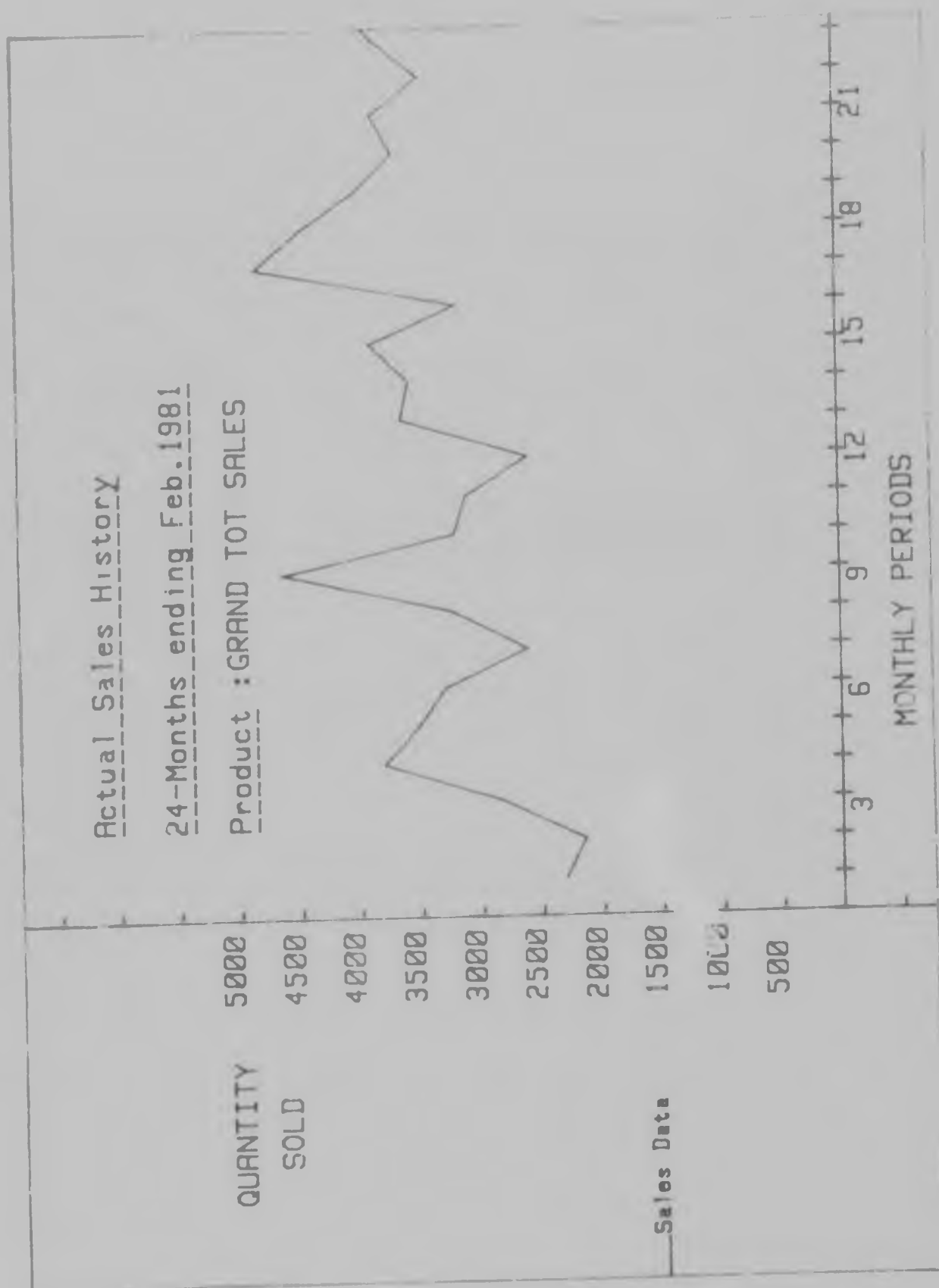


FIGURE 10

APPENDIX 2.1

TABLE 2.1.1. CLASSIFICATION OF DATA

A-B-C ANALYSIS FOR TWENTY FOUR MONTH PERIOD

The results of the A-B-C analysis for the twenty four month period are shown in Table 11.

In this analysis the 'A' level was set at 80% of the sales value and the 'A' and 'B' level at 95%. The report shows that just seventeen out of thirty seven line items account for 80% of the sales value. This report shows both the arithmetic average of the sales over the twenty four month period as well as the mean absolute deviation. The variability in demand is determined by the ratio of mean absolute deviation to the arithmetic average.

From Brown's definition of lumpy demand (section 3.4.1.) any item with a variability factor exceeding 80% can be considered to have lumpy demand.

In this case both the top two 'A' items have lumpy demand. The nature of this demand can clearly be seen in the graphs in Appendix 11.

This analysis is the first step in determining which items are important and should be forecast. Note that the 'C' items account for 50% of the sales value and only 1.950 units per annum.

TABLE 11
ANALYSIS OF SALES FROM 1960 TO FEBRUARY 1961

A I-C ANALYSIS

SALES: MARCH 1959 TO FEBRUARY 1961

LIM	DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (4 MON)	AVE. QTY (MON)	MADE	VAR. %	CUM. % (TOT. %)
A	P1	171	542	466.3	35.97	11.48	
A	P2	9691	404	379.4	93.96	21.50	
A	P3	7200	300	110.1	36.69	30.11	
A	P4	6670	278	121.8	43.79	37.07	
A	P5	217	130	76.1	58.56	41.63	
A	P6	11	43	20.2	46.97	45.79	
A		142	142	102.9	72.21	49.80	
A		171	171	89.1	52.20	53.70	
A		136	136	76.9	56.51	57.5	
A		131	131	67.1	51.29	61.11	
A		59	59	26.4	44.94	64.41	
A		1409	118	134.4	113.91	67.20	
A		1631	60	37.6	55.35	69.80	
A		1291	92	63.4	69.10	72.31	
A		1271	44	14.7	33.21	74.64	
A		1228	30	16.2	53.89	76.80	
A		1761	51	23.5	45.98	78.79	
B		1678	70	80.7	109.98	80.47	
B		1437	70	95.0	135.81	82.02	
B		811	60	83.9	140.05	83.40	
B		667	17	16.9	78.01	84.41	
B		1091	28	29.2	105.77	85.43	
B		1071	39	62.3	158.33	86.40	
B		1071	40	37.3	93.75	87.72	
B		1071	20	16.8	83.33	87.95	
B		1071	25	32.3	126.79	88.69	
B		1071	32	39.6	123.73	89.50	
B		408	17	16.2	95.10	90.04	
B		408	20	22.7	113.04	90.60	
B		408	25	32.9	134.18	91.22	
B		281	10	13.2	128.37	91.70	
B		223	9	5.2	55.94	92.20	
B		1071	13	14.0	109.31	92.69	
B		372	16	23.5	151.88	93.10	
B		252	11	9.5	90.08	93.50	
B		735	31	46.2	150.88	93.94	
B		114	5	6.2	130.70	94.20	
B		301	13	22.1	176.02	94.60	
B		212	9	11.8	133.18	94.97	

TOTAL QUANTITY: 91802
 TOTAL VALUE: \$841622.05

APPENDIX 2.2

SIX MONTHS A-B-C CLASSIFICATIONS

Table 12.1	August 1980 to January 1981
Table 12.2	May 1980 to October 1980
Table 12.3	February 1980 to July 1980
Table 12.4	November 1979 to April 1980
Table 12.5	August 1979 to January 1980
Table 12.6	May 1979 to October 1979

TABLE 12.1
 PARETO REPORT FOR SALES AUGUST 1980 TO JANUARY 1981

A-B-C METHOD

SALES: AUGUST '80 TO JANUARY '81

LIN	DRAWING NO.	TOT. QTY (6 MON)	TOT. VAL (6 MON)	QTY (MON)	VAL (MON)	VAR %	CUM % (TOT. VAL)
A	P2	6245		1041	399.2	38.36	22.82
A	P3	1804		281	105.7	27.14	30.71
A	P4	1728		288	141.0	50.00	37.12
A		1481		267	60.2	24.40	43.42
A		1251		209	59.0	28.30	48.54
A		522		87	38.3	44.06	52.92
A	P1	1220		203	181.4	89.23	56.60
A		529		155	66.8	43.13	60.63
A	P6	244		41	24.6	60.38	64.15
A		585		98	40.0	41.03	67.46
A		765		128	97.7	76.60	70.07
A		675		113	50.0	44.44	72.54
A	P5	459		77	30.8	50.76	74.94
A		498		100	32.0	38.55	77.01
A		470		100	44.1	56.31	78.87
B		230		10	24.8	64.64	80.69
B		129		22	13.8	64.34	82.13
B		238		40	34.1	85.99	83.48
B		188		27	23.2	87.08	84.75
B		174		20	19.0	65.52	85.71
B		250		10	55.6	132.33	86.60
B		220		17	48.9	133.33	87.43
B		175		10	32.3	110.67	88.25
B		249		42	33.7	81.12	89.05
B		61		10	6.6	67.21	89.70
B		184		31	29.6	96.38	90.30
B		104		17	11.7	67.31	90.89
B		65		11	9.2	84.62	91.41
B		84		14	11.3	80.95	91.88
B		250		11	69.4	156.67	92.33
B		100		17	27.8	166.67	92.76
B		111		19	7.0	37.84	93.19
B		81		14	19.8	146.91	93.60
B		98		16	21.8	133.33	94.00
B		60		10	7.0	70.00	94.41
B		100		21	27.3	133.33	94.80

TOTAL QUANTITY: 23201
 TOTAL VALUE: R 1113004.89

TABLE 12.2

PARETO REPORT FOR SALES FEBRUARY 1983 TO OCTOBER 1983

A-B-C ANALYSIS

SHEET: MAY '83 TO OCTOBER '83

LTN	DESCRIPTION	TOT. QTY (C & NON)	TOT. VAL (C & NON)	Avg. QTY (C & NON)	PER (C & NON)	PER (C & NON)	TOT. VAL (C & NON)
A	F2	3527		510	250.0	43.10	161.85
A	F2	2127		405	18.5	18.00	82.44
A	F1	2507		410	200.0	71.38	285.41
A		1049		383	280.7	65.98	38.43
A	F4	1671		279	100.0	55.44	45.81
A		1451		242	38.6	18.17	49.57
A		1172		198	20.8	14.74	53.48
A	F0	388		101	21.2	11.84	57.82
A		322		87	21.2	15.87	81.98
A		318		152	21.2	47.20	89.78
A		623		184	51.8	45.28	88.43
A		347		58	17.8	26.14	71.58
A	F3	454		82	25.5	25.53	74.87
A		683		101	67.0	65.94	78.04
A		543		96	37.8	45.67	78.38
A		218		82	17.8	18.29	75.25
A		477		86	38.0	45.18	81.41
B		411		70	38.0	111.50	25.78
B		239		40	14.1	38.58	88.15
B		240		41	25.1	58.15	85.47
B		455		74	21.0	42.88	88.74
B		233		48	39.8	111.88	87.84
B		94		10	4.8	18.81	88.78
B		331		55	30.0	101.31	88.97
B		228		37	48.3	143.88	98.78
B		167		28	12.0	51.15	81.78
B		118		28	18.8	58.17	92.27
B		118		13	18.7	71.78	82.88
B		82		14	18.7	72.81	83.88
B		149		25	25.1	101.18	83.77
B		56		9	7.8	28.57	94.22
B		94		14	18.8	28.58	94.88

TOTAL QUANTITY: 27953
 TOTAL VALUE:R 1140114.03

TABLE 12.3
PARTIAL BAYONET TEST DATA: FEBRUARY 1980 TO JULY 1981

F 1 C ANALYSIS

SALES: FEBRUARY 1980 TO JULY 1981

LIM	DRAWING NO.	TOT. QTY (6 MON)	TOT. VAL (6 MON)	AVE. QTY (MON)	MAP	VAR %	CUM. S (TOT. VAL)
A	P3	2391		399	105.5	25.47	10.23
A	P1			398	311.3	78.29	18.41
A	P4	1699		283	94.9	33.51	25.70
A	P2	1679		260	176.2	70.10	32.07
A		1430		238	309.1	129.70	37.64
A		1212		202	38.3	18.98	42.87
A				50	18.2	36.70	47.57
A	P6			161	175.3	108.90	51.07
A				150	54.2	36.15	55.67
A		899		127	67.3	52.88	59.91
A		764		58	32.3	55.75	64.15
A		348		138	61.7	44.58	65.70
A		830		82	39.9	47.23	68.74
A		494		136	145.9	107.53	71.17
A		814		80	36.1	45.23	73.89
A	P5	479		49	11.0	22.68	76.41
A		271		58	15.3	26.67	78.46
A		345		26	8.3	32.47	80.28
B		154		73	80.8	111.49	81.30
B		475		69	71.9	104.02	82.71
B		415		46	21.3	46.72	84.57
B		274		34	21.3	63.37	85.84
B		202		66	63.5	96.95	87.10
B		393		20	10.2	52.14	88.16
B		117		46	76.4	166.67	89.20
B		275		30	23.2	77.65	90.18
B		179		21	11.8	57.72	90.97
B		123		10	12.7	129.38	91.60
B		59		17	16.7	100.00	92.10
B		100		26	24.2	94.37	92.77
B		154		13	13.3	100.00	93.29
B		80		9	5.5	60.00	93.76
B		55		13	5.1	38.33	94.20
B		80		17	21.0	123.53	94.60
B		102					

TOTAL QUANTITY: 21716
TOTAL VALUE: \$ 1017363.94

TABLE 12.4
PARTIC REPORT FOR SALES MOVEMENT (NOV. 79 TO APR. 80)

A-B-C ANALYSIS

SALES: NOVEMBER 79 TO APRIL 80

LIN	DRAWING NO.	TOT. QTY (6 MON)	TOT. VAL (6 MON)	IN STOCK (6 MON)	MRD	VAR %	CUM % (TOT. VAL)
A	P1	6186		10.1	117.	71.45	22.77
A	P3	1886		314	117.	37.47	32.85
A	P4	1793		297	121.	40.44	39.99
A	P5	769		128	83.8	65.41	44.59
A		1150		147	75.0	39.13	49.16
A		879		147	180.2	122.98	53.23
A	P6	211		79	12.5	35.55	56.74
A		735		123	71.5	58.37	60.24
A		594		99	85.7	86.53	63.04
A		195		45	10.0	10.77	65.56
A		271		45	9.9	21.89	68.01
A		238		45	24.6	61.90	70.32
A		492		45	42.7	52.03	72.62
A		337		45	18.6	33.04	74.83
A		535		45	136.9	153.58	77.01
A		318		53	20.7	38.99	79.14
B	P2	425		67	94.4	133.33	80.90
B		401		67	69.1	103.41	82.56
B		155		40	23.2	89.68	83.58
B		239		40	34.8	87.45	84.48
B		73		12	12.2	100.46	85.39
B		147		25	26.0	106.12	86.27
B		128		21	12.0	56.25	87.12
B		155		26	27.8	107.53	87.96
B		200		33	33.3	100.00	88.78
B		145		24	32.2	133.33	89.54
B		93		16	12.5	80.65	90.26
B		104		17	16.8	96.79	90.90
B		152		25	16.4	64.91	91.42
B		58		10	6.7	60.97	92.05
B		130		22	22.9	105.64	92.58
B		80		13	17.1	128.33	93.12
B		218		36	43.2	118.96	93.55
B		62		10	6.4	62.37	93.96
B		44		4	2.1	26.79	94.37
B		63		11	10.5	100.00	94.77

TOTAL QUANTITY: 20801
TOTAL VALUE: \$ 919313.95

TABLE 12.5
 PARETO REPORT FOR SALE AUGUST 1979 TO JANUARY 1980

R I C ANALYSIS

SALES: AUGUST 1979 TO JANUARY 1980

LIM	DRAWING NO.	TOT. QTY (6 MON)	TOT. VAL (6 MON)	FILE QTY (MON)	MAD	VAR %	CUM % (TOT. VAL)
A	P1	8166		1361	492.7	36.27	31.64
A	P4	1629		272	115.8	42.66	39.17
A	P5	1060		177	93.8	53.11	45.92
A	P3	1187		198	44.7	22.61	51.87
A		1150		192	61.1	31.88	56.71
A	P6	208		35	10.1	29.17	60.35
A		657		110	62.8	57.38	63.63
A		205		34	11.8	34.47	66.41
A		277		46	9.2	19.98	69.02
A		257		43	9.8	22.96	71.63
A		368		61	17.0	27.72	74.19
A		347		50	29.6	51.20	76.45
A	P2	500		83	104.4	125.33	78.59
B		406		68	34.7	51.23	80.60
B		282		47	21.7	46.10	82.58
B		326		54	43.3	79.75	84.35
B		288		48	27.7	57.64	85.76
B		254		42	39.8	93.96	86.99
B		279		47	42.3	91.04	88.11
B		249		42	27.7	66.67	89.20
B		190		32	52.8	166.67	90.14
B		150		25	41.7	165.67	90.80
B		95		16	19.1	120.70	91.41
B		76		13	11.2	88.80	92.02
B		281		47	56.9	121.90	92.61
B		170		23	25.8	113.73	93.15
B		119		20	13.2	66.67	93.64
B		48		8	2.0	25.00	94.11
B		105		18	23.6	133.33	94.57

TOTAL QUANTITY: 20175
 TOTAL VALUE: \$7,100.01

TABLE 12-6
 PARETO REPORT FOR SALES MAY 1979 TO OCTOBER 1979

A-B-C ANALYSIS

SALES: MAY 79 TO OCTOBER 79

LINE	ORDERING NO.	TOT. QTY (C & NON)	TOT. VAL. (C & NON)	TOT. QTY (C & NON)	QTY	VAL	TOT. A /TOT. VAL
A	P1	3669		61	275.0	56.66	14.25
A	P4	2174		40	26.0	24.28	24.60
A	P5	1624		71	115.0	63.42	52.25
A	P5	1149		142	209.2	94.37	39.66
A	P5	1068		177	80.0	43.28	41.24
A		889		148	15.4	44.17	39.60
A		889		27	18.0	46.15	34.63
A	P6	234		24	14.0	45.48	56.86
A		255		124	57.1	68.01	54.31
A		749		123	44.0	77.00	62.40
A	P2	736		121	178.1	128.10	65.31
A		736		31	11.0	25.70	65.11
A		275		40	6.1	16.90	76.95
A		267		44	39.0	11.49	73.42
A		407		60	12.7	72.65	75.93
A		362		60	65.2	72.81	76.13
A		529		10	91.2	47.27	80.18
A		421		34	78.4	103.88	82.19
A		420		28	24.7	68.62	83.68
A		216		44	84.3	143.91	83.14
A		290		47	97.1	78.40	86.55
A		284		56	81.9	143.36	87.91
A		318		46	45.1	92.80	89.14
A		227		48	81.2	166.67	98.32
A		381		15	27.1	145.24	91.45
A		112		25	13.9	55.19	92.20
A		151		48	97.9	123.64	92.82
A		267		15	11.3	73.91	93.42
A		94		19	14.0	26.85	92.34
A		87		12	4.4	25.93	94.55
A		89					

TOTAL QUANTITY 19329

TOTAL VALUE 661114.47

APPENDIX 2.3

A-B-C CLASSIFICATIONS

Table 12.7 May 1979 to end April 1980

Table 12.8 January 1980 to end January 1981

These two A-B-C classifications were used for ranking the stock at the end of each period. The Stock Ratings at the end of April 1980 and January 1981 are shown in Appendix 6.

TABLE 12.7
 F I TO R I P I FOR SALES MAY 1979 TO APRIL 1980

H B C ANALYSIS

SALES: MAY '79 TO APRIL '80

LIM	DRAWING NO.	TOT. QTY (1 MON)	TOT. VAL (12 MON)	AVE. QTY (MON)	MAD*	VAR %	CUM % (TOT. VAL)
A	F1	9855		821	544.6	66.32	18.66
A	P3	293		293	121.9	41.68	27.45
A	P4	331		331	109.0	32.97	30.20
A	P5	160		160	75.3	47.08	42.41
A		184		184	77.5	42.09	46.78
A		2210		221	15.6	42.02	50.59
A	P6	445		124	79.7	64.45	54.10
A		108		108	98.1	90.51	57.11
A		38		38	15.0	40.00	60.16
A		47		47	9.0	19.85	62.74
A		55		43	18.5	43.37	65.29
A		513		106	148.7	140.40	67.87
A		1271		85	63.6	74.86	70.30
A		1119		58	16.5	28.25	72.68
A		699		95	84.5	89.23	75.01
A	P2	1137		77	60.3	78.45	77.17
A		922		79	66.8	85.07	79.17
A		943		45	23.8	53.37	80.39
B		47		47	34.6	73.84	82.75
B		60		60	30.6	150.00	84.24
B		50		50	51.9	104.76	85.44
B		48		48	56.3	117.07	86.56
B		377		31	34.2	110.22	87.50
B		17		17	19.3	112.85	88.11
B		20		20	17.9	89.89	88.11
B		24		24	40.3	166.67	89.92
B		16		16	15.4	96.68	90.52
B		191		9	9.2	101.85	91.01
B		108		11	14.7	65.92	91.51
B		40		40	51.0	126.08	92.11
B		7		7	7.9	119.17	92.61
B		18		18	14.7	83.33	93.11
B		211		8	3.2	38.38	93.60
B		130		11	12.3	117.75	94.05
B		155		13	18.2	140.86	94.48
B		6		6	6.2	77.08	94.83

TOTAL QUANTITY: 48140
 TOTAL VALUE: F 1760128.42

TABLE 12.8

PARETO REPORT FOR AREA 1 JANUARY 1981 TO JANUARY 1981

1-1 CUMULY IS

SALES: JANUARY '80 TO JANUARY '81

LIM	DRAWING NO.	TOT. QTY (13 PPH)	TOT. VAL (13 PPH)	AVG. QTY (2000)	MADE	VAR %	CUM % (TOT. VAL)
A	P2	79.4		419	463.5	76.84	14.05
A	P3	45.7		188	98.7	28.35	23.43
A	P1	47.6		362	329.7	91.08	30.57
A	P4	35.62		274	115.2	42.06	37.07
A		25.10		193	77.9	40.36	42.18
A		25.13		193	54.3	28.11	47.18
A		5.75		44	21.1	47.60	51.19
A	P6	22.25		171	195.0	113.92	57.00
A		9.08		70	35.2	50.46	58.71
A		17.33		133	66.8	50.10	62.17
A		10.55		143	72.1	50.55	65.36
A		11.59		89	37.9	42.54	68.52
A	P5	12.11		93	50.5	54.18	71.57
A		14.77		114	101.8	89.61	74.39
A		5.74		44	17.4	39.45	76.37
A		3.33		26	13.4	52.21	78.36
A		6.27		48	26.1	54.18	80.05
B		8.85		68	88.4	129.89	81.48
B		5.81		45	41.2	92.10	82.65
B		2.81		22	16.0	73.97	83.77
B		4.59		35	28.6	80.95	84.80
B		6.87		53	43.6	82.57	85.83
B		3.71		23	20.3	71.03	86.78
B		5.46		42	42.3	100.73	87.67
B		3.16		24	18.2	74.78	88.55
B		4.95		38	58.6	153.85	89.43
B		5.58		43	47.0	109.43	90.28
B		4.00		31	42.6	138.46	90.97
B		3.38		26	26.2	100.59	91.50
B		1.83		14	9.8	69.53	92.03
B		1.27		10	7.0	71.47	92.52
B		1.61		12	12.2	98.23	92.94
B		1.49		11	12.3	106.97	93.35
B		1.40		11	11.6	108.08	93.73
B		.75		6	6.6	113.85	94.12
B		.68		5	5.6	106.11	94.47
B		1.32		10	12.9	126.57	94.82

TOTAL QUANTITY: 48018
 TOTAL VALUE: \$ 2269399.07

APPENDIX 3

Table 13 Analysis of 'A' items sales by customer

ANALYSIS OF 'A' ITEMS SALES BY CUSTOMER

Table II breaks the 'A' item sales down to customer level. This report indicates where demand is heavily dependent on a small number of customers. It indicates that six of the 'A' items have more than 75% of their demand originating from one customer.

In one case 95% of the demand originates from one customer. These facts have to be taken into account when making the forecasting policies are decided upon. It has been found customer analysis is the best method of forecasting demand for some items. Certainly the inventory control must recognize the percentage of demand that is dependent on one customer.

TABLE 13

ANALYSIS OF A ITEMS BY CUSTOMER

SALES: MARCH 79 TO FEBRUARY '81

DRAWIN NO.	CUST	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAE	VAR %	CUM % TOT. VAL	CUM % ITEM
P1	682	11259		469	482.0	102.74	9.90	86.25
	685	4.0		18	28.3	161.90	10.28	89.53
	749	325		14	22.6	166.67	10.57	92.02
	365	269		11	18.2	162.21	10.81	94.14
	1105	261		11	18.1	166.67	11.05	96.24
	199	120		5	6.3	166.67	11.16	97.22
	912	120		5	7.9	158.33	11.27	98.19
	254	97		4	6.7	166.67	11.35	98.88
	819	45		2	3.4	183.33	11.39	99.21
	729	34		1	2.4	191.67	11.42	99.44
	875	18		1	1.4	191.67	11.43	99.59
	40	12		1	0.9	183.33	11.44	99.68
	1135	10		0	0.6	191.67	11.45	99.76
	343	6		0	0.5	191.67	11.46	99.81
	1638	3		0	0.4	191.67	11.46	99.84
	299	4		0	0.3	191.67	11.47	99.88
	1058	3		0	0.3	191.67	11.47	99.90
	1103	3		0	0.2	191.67	11.47	99.92
	1287	2		0	0.2	191.67	11.47	99.94
	567	2		0	0.2	191.67	11.48	99.96
	995	2		0	0.2	191.67	11.48	99.97
	1426	2		0	0.2	191.67	11.48	99.98
	1136	1		0	0.1	191.67	11.48	99.99
	1289	1		0	0.1	191.67	11.48	100.00
F2	756	4901		204	207.2	111.84	16.64	51.48
	296	1544		66	107.3	105.17	18.36	68.73
	682	1038		43	107.3	150.00	18.33	78.34
	754	807		34	58.8	175.00	20.18	86.82
	880	595		25	107.3	175.00	20.70	92.05
	1179	348		15	107.3	106.67	21.08	95.81
	752	100		4	0.0	191.67	21.18	96.88
	758	100		4	0.0	191.67	21.29	97.94
	254	65		3	4.7	175.00	21.35	98.56
	904	81		2	3.8	183.33	21.40	99.05
	295	24		1	1.8	183.33	21.43	99.31
	84	24		1	1.9	191.67	21.45	99.54
	310	22		1	1.7	183.33	21.47	99.74
	465	10		0	0.0	191.67	21.48	99.84
	2104	7		0	0.5	183.33	21.49	99.91
	1313	5		0	0.4	183.33	21.49	99.97
	73	3		0	0.0	191.67	21.50	100.00
P3	1361	2760		115	71.3	62.08	24.89	39.35
	332	1999		83	35.9	43.10	27.09	64.33

TABLE IV (continued)

DRAWING NO.	CU-1	TOT. QTY (24 MON.)	TOT. VAL (24 MON.)	AVE. QTY (MON.)	MAD	VAR %	CUM % TOT. VAL	CUM. ITEM
		1999		23	35.9	43.10	29.29	90.51
	474	550		23	32.5	141.67	30.00	98.13
	685	500		21	26.3	126.33	30.65	106.30
	431	271		11	7.2	63.44	31.00	110.35
	1473	270		11	20.6	183.33	31.27	113.48
	752	166		7	6.1	87.65	31.45	115.48
	752	125		5	8.7	166.67	31.62	117.48
	1951	105		4	7.7	175.00	31.74	118.92
	1162	40		3	4.2	166.67	31.82	119.86
	752	40		3	2.5	150.00	31.87	120.46
	2192	33		2	3.1	183.33	31.93	121.07
	930	30		2	3.0	158.33	31.98	121.66
	59	30		1	2.6	175.00	32.02	122.15
	1925	24		1	2.2	175.00	32.06	122.61
	702	24		1	2.4	191.67	32.10	123.04
	1103	15		1	1.8	183.33	32.13	123.42
	1873	12		1	1.9	191.67	32.16	123.71
	2259	10		1	1.6	175.00	32.19	124.11
	997	9		1	1.2	191.67	32.21	124.33
	1474	10		1	1.0	183.33	32.22	124.50
	2190	6		0	1.0	191.67	32.24	124.71
	634	6		0	0.8	191.67	32.25	124.85
	967	6		0	0.7	183.33	32.26	124.98
	1773	5		0	0.8	191.67	32.27	125.11
	1318	1		0	0.6	191.67	32.29	125.23
	919	1		0	0.5	191.67	32.29	125.33
				0	0.5	191.67	32.30	125.41
				0	0.5	191.67	32.31	125.49
				0	0.5	191.67	32.31	125.55
				0	0.4	183.33	32.31	125.57
				0	0.1	191.67	32.31	125.57
				0	0.1	191.67	32.32	125.58
P4	1474	2487		104	73.0	70.44	34.73	34.68
	685	1061		44	29.8	67.36	35.93	51.94
	471	600		25	19.1	76.33	36.60	61.54
	712	596		25	37.7	151.52	37.20	70.16
	295	471		20	22.5	114.54	37.74	77.95
	1426	350		15	26.7	183.33	38.04	82.22
	758	210		9	12.4	141.67	38.28	85.63
	254	150		6	9.5	151.67	38.43	87.87
	2335	110		5	8.8	191.67	38.56	89.66
	421	80		3	5.6	166.67	38.65	91.02
	1473	89		4	4.1	111.52	38.74	92.27
	2254	80		3	5.6	166.67	38.82	93.47
	1135	50		2	3.6	175.00	38.88	94.30

TABLE 13 (Cont.)

DRAWING NO.	CUST	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (24 MON)	MRD	VAR %	CUM % TOT. VAL	CUM % ITEM
	685	1061		21	27.8	67.36	40.08	111.56
	471	600		19	19.1	76.33	40.75	121.16
	712	596		25	27.7	151.62	41.35	129.78
	295	471		22	22.5	114.54	41.89	137.57
	1426	350		15	26.7	183.33	42.19	141.84
	754	210		12	12.4	141.67	42.43	145.25
	251	150		9	9.5	151.67	42.58	147.49
	2335	110		5	8.8	191.67	42.71	149.28
	431	80		3	5.6	166.67	42.80	150.64
	1473	89		4	4.1	111.52	42.89	151.89
	2259	80		5	5.6	166.67	42.97	153.09
	1135	50		3	3.0	175.00	43.03	153.92
	1196	50		4	4.0	191.67	43.08	154.69
	1510	33		1	2.4	175.00	43.12	155.24
	280	30		1	2.3	183.33	43.16	155.74
	183	30		1	2.4	191.67	43.19	156.23
	1094	24		1	1.8	183.33	43.22	156.65
	2190	22		1	1.7	183.33	43.25	157.03
	922	20		1	1.6	191.67	43.27	157.38
	634	19		1	1.3	166.67	43.29	157.70
	752	15		1	1.2	191.67	43.31	157.96
	135	11		0	0.9	191.67	43.32	158.13
	930	10		0	0.9	191.67	43.34	158.31
	1668	10		0	0.8	191.67	43.35	158.48
	1947	10		0	0.8	191.67	43.36	158.64
	666	10		0	0.8	191.67	43.37	158.81
	2192	10		0	0.8	191.67	43.38	158.95
	366	6		0	0.7	175.00	43.39	159.09
	997	6		0	0.5	191.67	43.40	159.20
	514	6		0	0.5	191.67	43.41	159.30
	245	6		0	0.5	191.67	43.41	159.39
	2334	5		0	0.4	191.67	43.42	159.47
	571	4		0	0.3	183.33	43.42	159.54
	1103	4		0	0.3	191.67	43.43	159.60
	953	1		0	0.1	191.67	43.43	159.62
P5	2259	1505		63	53.7	85.57	45.56	46.80
	2012	428		19	20.8	116.67	46.18	60.56
	2114	282		12	16.2	137.94	46.59	69.59
	567	159		7	6.8	102.04	46.84	75.15
	1426	158		9	9.9	150.00	47.04	79.56
	842	121		5	4.6	91.87	47.24	83.79
	326	80		3	5.3	158.33	47.36	86.43
	486	72		4	4.0	133.33	47.47	88.91
	726	36		2	2.6	175.00	47.52	90.11

TABLE 13 (Continued)

REFERENCE NO.	CUST	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVG. QTY (24 MON)	NRD	VAR %	CUM % TOT. VAL	CUM. ITEM
	2012	428		18	20.8	116.67	48.15	103.86
	2114	282		12	16.2	137.94	48.56	112.90
	567	159		7	6.8	102.04	48.81	118.46
	1426	158		7	7.8	150.11	49.01	122.87
	842	121		5	4.6	91.87	49.21	127.40
	326	80		3	3.8	131.53	49.33	129.74
	486	72		3	4.0	133.53	49.41	132.22
	726	36		2	2.0	175.00	49.45	133.42
	295	30		1	2.2	175.00	49.54	134.51
	1214	28		1	1.9	166.67	49.59	135.58
	109	24		1	1.9	191.67	49.63	136.49
	424	23		1	1.1	116.67	49.67	137.34
	1118	21		1	1.5	166.67	49.71	138.10
	1053	20		1	1.3	158.33	49.74	138.81
	1357	20		1	1.6	191.67	49.77	139.49
	1487	20		1	1.5	183.33	49.80	140.17
	1156	20		1	1.6	191.67	49.83	140.83
	873	14		1	1.1	191.67	49.85	141.33
	863	13		1	1.0	183.33	49.87	141.74
	1043	11		0	0.8	183.33	49.89	142.13
	1272	10		0	0.8	191.67	49.91	142.48
	1196	10		0	0.8	191.67	49.92	142.82
	254	8		0	0.6	191.67	49.93	143.06
	48	5		0	0.4	191.67	49.94	143.23
	1308	1		0	0.1	191.67	49.94	143.27
	1235	1		0	0.1	191.67	49.94	143.31
PE	703	974		41	19.2	47.42	53.83	94.29
	350	24		1	1.8	183.33	53.92	96.58
	245	16		1	1.2	175.00	53.99	98.16
	1271	7		0	0.5	183.33	54.02	98.87
	2259	5		0	0.4	183.33	54.04	99.30
	1322	4		0	0.3	191.67	54.05	99.70
	32	3		0	0.2	191.67	54.07	100.00
F	685	1067		44	51.0	114.68	55.37	100.54
	1961	911		38	33.5	88.13	56.41	58.33
	758	488		20	26.7	133.33	56.99	72.92
	474	348		15	24.2	166.67	57.41	83.34
	1474	223		9	10.8	116.67	57.64	89.06
	1473	98		4	4.7	125.56	57.73	91.40
	59	70		3	5.3	183.33	57.81	93.49
	219	64		3	4.2	158.33	57.98	95.13
	514	56		2	4.3	183.33	57.95	96.80

TABLE 13 (Continued)

DRAWING NO.	CUST	TOT. QTY (24 MON)	TOT. VHL (24 MON)	HYE. QTY (24 MON)	VAR	CUM % TOT. VHL	CUM % ITEM
1961		911		33.5	88.13	58.98	122.60
758		480		26.7	133.33	59.57	137.18
474		300		24.2	166.67	59.99	147.61
1474		223		10.8	116.67	60.21	153.32
1473		90		4.7	125.56	60.31	155.67
59		70		5.3	183.33	60.39	157.75
2192		64		4.0	158.33	60.46	159.45
514		56		3.3	181.11	60.52	161.07
254		45		2.0	191.67	60.57	162.31
295		24		1.0	183.33	60.60	163.06
332		18		1.4	191.67	60.62	163.55
2190		10		0.8	191.67	60.64	163.86
1202		8		0.6	191.67	60.65	164.11
207		5		0.4	191.67	60.65	164.26
752		1650		68.6	100.00	62.28	41.09
685		1000		4.0	59.0	181.67	63.24
756		430		18	29.9	166.67	63.66
754		300		13	21.9	175.00	63.96
135		200		1.0	11.0	191.67	64.21
735		20		0.8	16.0	191.67	64.39
681		12		5	9.5	183.33	64.52
417		90		7.2	191.67	64.61	100.00
2335		2750		115	74.6	65.09	67.85
295		60		0.8	175.00	67.92	87.79
685		70		5.3	183.33	68.00	89.70
1426		80		6.4	191.67	68.06	91.35
1474		60		4.6	191.67	68.12	92.98
712		59		4.3	175.00	68.18	94.54
634		46		2.7	141.67	68.23	95.98
254		35		1	2.7	183.33	68.27
905		24		1	1.9	191.67	68.30
2192		24		1	1.9	191.67	68.32
1094		16		1	1.0	191.67	68.34
1094		10		0	0.6	191.67	68.35
1094		10		0	0.8	191.67	68.36
280		5		0	0.4	191.67	68.37
1058		4		0	0.3	183.33	68.37
1126		3		0	0.2	181.33	68.37
887		3		0	0.2	191.67	68.38
435		2		0	0.2	191.67	68.38
967		2		0	0.2	191.67	68.38
1259		1		0	0.1	191.67	68.38
571		1		0	0.1	191.67	100.00

TABLE 13 (Continued)

DRAWING NO	COST	QTY (24 MON)	TOT. VAL (24 MON)	AVE. CT (MON)	MAD	VAR %	CUM % TOT. VAL	CUM. ITEM
	60			3	4.4	175.00	68.45	101.92
	70			3	5.3	183.33	68.53	102.84
	80			1	6.4	191.67	68.59	103.48
1474	60			3	4.8	191.67	68.64	107.12
712	70			2	4.3	175.00	68.71	107.67
644	40			2	4.7	171.67	68.77	110.11
800	70			1	2.7	183.33	68.80	111.04
906	24			1	1.9	191.67	68.83	111.79
2192	24			1	1.9	191.67	68.85	112.44
1454	20			1	1.3	191.67	68.87	112.95
316	10			0	0.8	191.67	68.88	113.23
366	10			0	0.8	191.67	68.89	113.49
748	10			0	0.4	191.67	68.90	113.65
1058	4			0	0.3	183.33	68.90	113.77
1126	3			0	0.2	183.33	68.91	113.86
887	3			0	0.2	191.67	68.91	113.95
435	2			0	0.2	191.67	68.91	114.02
961	2			0	0.2	191.67	68.92	114.06
1259	1			0	0.1	191.67	68.92	114.10
571	1			0	0.1	191.67	68.92	114.13
P	1925	2984		124	64.3	51.70	72.33	95.25
	685	90		4	7.2	191.67	72.43	98.11
	712	40		2	3.2	191.67	72.47	99.33
	283	20		1	1.6	191.67	72.49	99.87
	2335	4		0	0.3	191.67	72.50	100.00
P	959	861		36	16.3	45.41	74.55	61.59
	756	295		12	17.6	143.22	75.26	82.83
	682	70		3	4.6	158.33	75.41	87.39
	656	50		2	3.8	183.33	75.51	90.55
	754	38		2	2.8	175.00	75.60	93.22
	199	20		1	1.5	183.33	75.65	94.69
	365	20		1	1.5	183.33	75.70	96.08
	2190	12		1	0.9	175.00	75.73	96.36
	295	10		0	0.8	191.67	75.75	97.70
	514	8		0	0.6	191.67	75.77	98.26
	969	8		0	0.6	175.00	75.79	98.77
	1166	6		0	0.5	191.67	75.80	99.11
	1139	5		0	0.4	191.67	75.81	99.58
	1166	2		0	0.2	183.33	75.82	99.73
	84	2		0	0.2	191.67	75.82	99.86
	958	1		0	0.1	191.67	75.83	99.94
	2211	1		0	0.1	191.67	75.83	100.00
P	750	1239		52	86.0	166.67	77.14	46.5

DRAWING NO. 10-10-1000-1

DRAWING NO.	CUST	TOT. OLY (24 HOURS)	TOT. VAL C. H. MON.	AVE. OFF CHRG.	MAD	VAR %	CUM % TOT. VAL	CUM % ITEM
	880	723		30	45.2	150.03	77.78	69.38
	682	510		21	37.2	175.00	78.29	87.61
	310	148		6	8.7	141.67	78.42	92.24
	2104	99		4	7.5	181.31	78.53	96.05
	365	60		3	4.8	191.67	78.59	98.17
	904	20		1	1.6	191.67	78.61	98.87
	971	19		1	1.5	183.33	78.63	99.52
	465	10		0	0.8	191.67	78.64	99.88
	254	4		0	0.3	191.67	78.64	100.00

APPENDIX 4

CUSTOMER RANKING IN ORDER OF DEGREE OF
SALES AND SERVICE OF PRODUCTS

CUSTOMER RANKING IN ORDER OF DECREASING ACCOUNT
VALUE AND DETAILS OF PURCHASES

The report shows that only twenty seven customers account for 80% of the sales revenue in this product group. Of these customers, twelve have more than 75% of their account concentrated on one item.

TABLE 14

CUSTOMER RANKING BY ACCOUNT VALUE

SALES: MARCH '79 TO FEBRUARY '81

CUSTOMER: 682		CUM % VALUE: 11.8%				
DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P1	11259		469	462.8	182.74	83.7
P2	1036		43	64.8	150.00	8.1
P	510		21	37.2	175.00	4.3
P	96		4	6.8	170.83	1.3
P	70		3	4.6	158.33	1.3
P	114		5	8.7	183.33	1.0
P	20		1	1.6	191.67	.2
P	10		0	0.8	191.67	.1
CUSTOMER: 756		CUM % VALUE: 21.0%				
DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
F2	4981		201	269.2	131.84	56.3
P	1239		52	86.0	166.67	14.4
P	831		35	64.7	186.85	9.6
P	295		12	17.6	143.22	7.7
P	500		21	39.9	191.67	5.3
P	430		18	29.9	166.67	4.6
F	180		3	14.4	191.67	2.0
CUSTOMER: 1961		CUM % VALUE: 26.6%				
DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P3	2760		115	74.3	27.03	43.8
F	911		38	33.5	28.13	18.6
P	770		32	53.0	165.15	12.3
F	110		5	4.9	106.82	3.8

TABLE 14 (Continued)

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	45		2	3.6	191.67	2.4
P	20		1	1.4	166.67	.8
P	21		1	1.8	175.00	.6
P	15		1	1.0	158.33	.5

CUSTOMER: 685

CUM % VALUE: 31.6%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	1067		44	51.0	114.69	25.9
P4	1061		44	29.8	67.36	23.8
P	1000		42	59.0	141.67	19.1
P3	500		21	26.3	126.33	13.0
F1	420		18	28.3	161.90	7.5
P	145		6	10.6	175.00	3.5
P	90		4	7.2	191.67	2.1
P	66		3	5.1	191.67	1.7
P	70		3	5.3	183.33	1.4
P	45		2	3.6	191.67	1.2
P	100		4	8.0	191.67	.8

CUSTOMER: 703

CUM % VALUE: 35.6%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QT (MON)	MAD	VAR %	% BY VAL
P6	974		41	19.2	47.42	99.3
P	5		0	0.4	191.67	.3
P	5		0	0.4	191.67	.3
F	3		0	0.2	191.67	.1

CUSTOMER: 2259

CUM % VALUE: 39.3%

DRAWING NO.	TOT. QT (24 MON)	TOT. VAL (24 MON)	AVE. QT (MON)	MAD	VAR %	% BY VAL
P5	1505		63	53.7	95.57	57.8
P	305		13	20.0	157.49	11.7
P	184		8	11.6	150.72	7.4
P	123		5	9.0	175.00	7.2

TABLE 14 (Continued)

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	%BY VAL
P4	88		3	5.6	166.67	2.3
P	50		2	3.8	183.33	1.9
P	21		1	1.5	175.00	1.6
P	20		1	1.6	191.67	1.5
P	37		2	2.8	183.33	1.5
P	40		2	3.2	191.67	1.5
P	38		2	3.0	191.67	1.4
P	20		1	1.6	191.67	.8
P	14		1	1.0	175.00	.8
P	8		0	0.6	191.67	.8
P	5		0	0.4	183.33	.5
P6	5		0	0.4	191.67	.5
P	5		0	0.6	191.67	.4
P	10		0	0.8	191.67	.3
P3	10		0	0.3	191.67	.1
P	4		0	0.1	191.67	.1
P	1		0			

CUSTOMER: 1925

CUM % VALUE: 42.7%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	%BY VAL
P	2984		124	64.3	51.70	98.4
P3	24		1	1.8	183.33	.9
P	12		1	1.2	191.67	.5
P	2		0	0.2	191.67	.2

CUSTOMER: 2315

CUM % VALUE: 46.1%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	%BY VAL
P	2750		115	74.6	45.09	96.2
F4	110		5	8.8	191.67	3.7
P	4		0	0.3	191.67	.1

CUSTOMER: 1474

CUM % VALUE: 48.9%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	%BY VAL
P4	2487		104	73.0	70.44	96.9

TABLE 14 (Continued)

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	223			10.8	116.67	8.2
P	60			4.8	191.67	2.2
P	14			0.9	158.33	1.0
P	18		1	1.4	191.67	.6
P3	10		0	0.8	191.67	.4
P	10		0	0.8	191.67	.4
P	2			0.2	191.67	.2
P	2			0.2	191.67	.1

CUSTOMER: 959

DRAWING NO	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	861		36	10.2	45.41	75.9
P	521		21	20.3	93.41	22.0
P	50		2	4.0	191.67	2.1

CUSTOMER: 1426

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	308		13	15.6	121.65	20.9
P	360		15	23.8	158.33	16.5
P4	350		15	26.7	183.33	11.1
P3	270		11	20.6	183.33	10.1
P	190		8	13.2	166.67	9.4
P5	158		7	9.9	150.00	7.5
P	109		5	7.2	158.33	7.4
P	130		5	9.5	175.00	4.8
P	31		1	2.0	158.33	2.7
P	91		4	7.0	183.33	2.4
P	80		3	6.4	191.67	2.3
P	19		1	1.5	191.67	1.3
P	25		1	2.0	191.67	.9
P	25		1	2.0	191.67	.8
P	18		1	1.4	183.33	.8
P	20		1	1.6	191.67	.8
P	2		0	0.2	191.67	.2

TABLE 11 (Cont'd)

DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VOL. (24 MONTHS)	AVE. QTY (MONTH)	QTY	QTY %	QTY VOL.
P1	2		8	8.0	13.33	1
CUM. % VOL. 83.33						
DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VOL. (24 MONTHS)	AVE. QTY (MONTH)	QTY	QTY %	QTY VOL.
P1	1459		89	89.0	6.13	8.7
P2	88		4	4.0	0.27	0.3
P3	18		2	2.0	0.14	0.1
P4	18		1	1.0	0.07	0.1
P5	18		8	8.0	0.56	0.6
CUM. % VOL. 86.41						
DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VOL. (24 MONTHS)	AVE. QTY (MONTH)	QTY	QTY %	QTY VOL.
P1	607		24	24.0	1.72	1.8
P2	283		22	22.0	1.57	1.6
P3	243		13	13.0	0.93	0.9
P4	78		3	3.0	0.22	0.2
P5	35		2	2.0	0.14	0.1
CUM. % VOL. 88.87						
DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VOL. (24 MONTHS)	AVE. QTY (MONTH)	QTY	QTY %	QTY VOL.
P1	723		20	20.0	1.43	1.4
P2	595		23	23.0	1.67	1.6
P3	225		16	16.0	1.16	1.1
P4	108		13	13.0	0.93	0.9
P5	205		9	9.0	0.65	0.6
P6	46		3	3.0	0.22	0.2
P7	42		2	2.0	0.14	0.1
P8	4		0	0.0	0.00	0.0
CUM. % VOL. 90.85						
DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VOL. (24 MONTHS)	AVE. QTY (MONTH)	QTY	QTY %	QTY VOL.
P1	1504		89	89.0	5.98	6.0

Table 1 (Continued)

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	3		0	0.2	191.67	.3

CUSTOMER: 177

CUM % VALUE: 64.8%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	64		27	14.1	52.64	99.7
P3	5		0	0.4	183.33	.3

CUSTOMER: 296

CUM % VALUE: 66.7%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P2	1594		66	68.8	185.07	89.2
P	150		6	11.5	183.33	7.7
P	40		2	3.1	183.33	2.5
P	10		0	0.8	191.67	.6

CUSTOMER: 752

CUM % VALUE: 68.7%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	1650		69	68.8	188.92	84.3
P3	125		5	8.7	166.67	6.5
P2	100		4	8.0	191.67	5.5
P4	15		1	1.2	191.67	.9
P	5		0	0.4	191.67	.8
P	1		0	0.1	191.67	.1

CUSTOMER: 365

CUM % VALUE: 70.3%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	1025		43	64.1	150.00	59.7
P1	269		11	18.2	162.21	14.9
P	147		6	8.7	141.67	10.0
P	46		2	3.5	183.33	4.3
P	60		3	4.8	191.67	3.7

TABLE 14 (Continued)

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	20		1	1.5	150.00	2.8
P	40		2	3.2	191.67	2.5
P	20		1	1.6	191.67	1.2
P	10		0	0.8	191.67	0.6

CUSTOMER: 1100

CUM % VALUE: 71.7%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	577		24	15.3	167.87	95.4
P	20		1	1.6	191.67	4.6

CUSTOMER: 1179

CUM % VALUE: 73.0%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	495		21	36.1	175.00	40.1
P2	348		15	24.2	166.67	29.4
P	107		4	7.1	159.30	14.2
P	92		4	7.0	183.33	7.7
P	47		2	3.6	183.33	6.4
P	18		1	1.3	115.00	2.3

CUSTOMER: 474

CUM % VALUE: 74.2%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P3	550		23	32.5	141.67	50.4
P	348		15	24.2	166.67	34.7
P	52		2	4.2	191.67	4.9
P	10		0	0.8	191.67	2.0

CUSTOMER: 1105

CUM % VALUE: 75.4%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	689		29	43.1	150.00	53.3
P1	291		11	14.1	166.67	20.4

(continued)

DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VBL (24 MONTHS)	AVG. QTY (MONTH)	QTY	VAR %	SBY VBL
P	444		18	18.1	171.48	19.0
P	100		4	4.0	191.67	4.4
P	30		1	0.4	191.67	2.1

CUM. S. TOTAL 78.6%

CUSTOMER: 706

DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VBL (24 MONTHS)	AVG. QTY (MONTH)	QTY	VAR %	SBY VBL
P	100		4.0	4.0	143.12	42.3
P1	212		9	12.4	191.67	20.1
P2	100		4	4.0	191.67	9.0
P	50		2	1.0	191.67	6.0
P3	40		1	0.1	191.67	4.4
P4	40		1	0.1	175.00	4.2
P	40		1	0.2	191.67	3.1
P	12		1	0.1	191.67	2.7
P	30		1	0.1	191.67	1.1
P	6		0	0.1	191.67	1.1

CUM. S. TOTAL 77.7%

CUSTOMER: 295

DRAWING NO.	TOT. QTY (24 MONTHS)	TOT. VBL (24 MONTHS)	AVG. QTY (MONTH)	QTY	VAR %	SBY VBL
P4	471		20	22.5	114.54	47.3
P	50		4	7.0	191.67	8.4
P	33		1	1.7	175.00	6.0
P	20		1	4.4	175.00	6.3
P	23		1	1.4	142.03	6.3
P	30		1	1.0	175.00	4.1
P3	30		1	1.0	175.00	3.0
P3	30		1	1.2	191.67	2.7
P	20		1	1.0	191.67	2.6
P	24		1	1.0	191.67	2.3
P2	24		0	0.0	191.67	2.1
P	10		1	1.0	191.67	2.0
P	20		0	0.0	191.67	1.4
P	10		1	1.0	191.67	1.1
P	12		0	0.0	191.67	.9
P	6		0	0.0	191.67	.7
P	6		0	0.0	191.67	.7

(b) (4) (Confidential)

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P			0	0.2	191.67	.6
P			0	0.3	191.67	.4
P	1		0	0.	191.67	.4

CUSTOMER: 631

CUM % VALUE: 78.6%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
P	450		19	34.4	183.33	47.4
P	300		13	22.1	176.67	38.9
P	40		2	3.1	183.33	7.0
P	46		2	3.2	191.67	4.6
P	20		1	1.5	183.33	2.2

CUSTOMER: 2012

CUM % VALUE: 79.4%

DRAWING NO.	TOT. QTY (24 MON)	TOT. VAL (24 MON)	AVE. QTY (MON)	MAD	VAR %	% BY VAL
F5	428		18	20.8	116.67	71.7
P	134		6	8.4	150.00	22.2
P	37		2	3.0	191.67	6.1

APPENDIX 5

SAFETY STOCKS

Table 5.1 Safety stock factors

Table 5.2 Load time adjustment factors

SAFETY STOCK DETERMINATION

Tables 15.1 and 15.2 are used to find the following values:

Service level

Standard normal deviate Z corresponding to service level

Lead time standard deviation

Mean standard deviation of demand

For the service level

Service factor k (from Table 15.1)

Factor of lead time standard deviation L (from Table 15.2)

Lead time standard deviation σ_L (from Table 15.2)

Therefore

Safety stock = $Z \cdot \sigma_L \cdot L$

or

TABLE 15.1
SAFETY STOCK FACTORS BASED ON MEAN ANNUAL DEMAND $\mu = 1000$

Service Level	Factor
80%	1.05
90%	1.65
92%	2.33
94%	2.33
95%	2.58
98%	3.09

Source: Block, "Inventory Management: Heuristics Revisited."

TABLE 15.2
 (17) THE ADJUSTMENT FACTORS F x SAFETY STOCK

Ratio of Load Time to Demand Interval	Adjustment Factor
2	1.53
3	2.10
4	2.56
5	2.99
6	3.41
8	4.29
10	5.01

where F = value from Table 15.1) (Factor
 (1) = value [5.7] Mean absolute
 error (m))

APPENDIX 6

INVENTORY STATUS

Table 16.1	Inventory status at end of April 1980
Table 16.2	Inventory status at end of January 1981

The inventory status at 04-25-1980 and 01-25-1981 are shown in Tables 16.1 and 16.2 respectively. The products are ranked in decreasing order of importance as determined by an A-B-C analysis over twelve preceeding months (see Appendix 2.3).

The following points can be noted:

- a) There are no stockouts recorded in April 1980.
Table 16.1.
- b) Two 'B' items in Table 16.1 have less than one months stock of average sales on hand.
- c) One stockout of a 'B' item is recorded in Table 16.2.
- d) Three 'A' items have less than one months stock of average sales on hand stock.

The figures in Table 16.1 were used as a starting point for the inventory simulation exercise in Section 7. This exercise goes through to January 1981 where the results are compared with the actual stock figures shown in Table 16.2.

Inventory savings (or increases) are computed on the basis of the difference between the simulated figures and the actual January 1981 figures.

TABLE 16.1
INVENTORY STATUS AT 25 APRIL 1980

PRODUCT	Ending April '80 12 Month Sales	Sales Ave	M.A.D.	Stock on Hand	Stock Turn- Over in Mths	Cum % Stock Value
P1	9855	821	545	1203	1,47	4,19
P3	3510	293	122	891	3,04	9,70
P4	3967	331	109	1091	3,30	15,80
P5	1831	153	76	460	3,01	19,51
	2210	184	77	477	2,59	21,48
P6	445	37	16	87	2,35	23,02
	1483	124	80	569	4,59	26,20
	1300	108	98	722	6,69	30,23
	450	38	15	106	2,79	31,59
	558	47	9	211	4,49	33,71
	513	43	19	140	3,26	35,06
	1271	106	149	649	6,12	37,73
	1019	85	64	383	4,15	39,87
	699	58	17	244	4,21	41,84
P2	1137	95	85	743	7,82	45,21
	922	77	60	530	6,88	48,28
	943	79	67	108	1,37	48,77

Note: Cumulative percentage of stock value only calculated for 'A' items.

Total number of line items	76
Total number of units	13 145

TABLE 16.2
INVENTORY STATUS AT 25 JANUARY 1981

PRODUCT	Ending Jan 1981 12 Month Sales	Sales Ave	M.A.D.	Stock on Hand	Stock Turn- Over in Mths	Cum % Stock Value
P2	7924	610	464	12	0,02	0,06
P3	4527	348	99	1706	4,90	12,61
P1	4706	362	330	1096	3,03	16,99
P4	3562	274	115	808	2,95	22,25
	2510	193	78	547	2,83	25,92
	2513	193	54	533	2,76	29,39
P6	575	44	21	117	2,66	31,91
	2225	171	195	104	0,61	32,47
	908	70	35	155	2,21	34,28
	1733	133	67	105	0,79	34,97
	1855	143	72	563	3,94	37,70
	1159	89	38	345	3,88	40,82
P5	1171	90	50	411	4,57	44,83
	1477	114	102	313	2,75	46,87
	574	44	17	159	3,61	48,84
	333	26	13	63	2,42	49,83

Note: Cumulative percentage pf stock value was only calculated for 'A' items.

Number of items	69
Number of units	13 842

APPENDIX 7

SAMPLE EXPONENTIAL SMOOTHING RESULTS

2. If the model results to dependent variables 7, 8 and 9 are listed in the following table:

model 7	Exponential smoothing with no control.
model 8	Exponential smoothing with control of the amount for trend's tracking signal.
model 9	Exponential smoothing for T_k and T_{k+1} and T_{k+2} .
model 10	Exponential smoothing by a Bon Bon model.

7.1.1 Model 1 - Exponential Smoothing With No Control

The model is based on equation 1

$$NF = \alpha ND + (1 - \alpha)OF$$

Where NF new forecast
 ND new demand information
 OF previous forecast
 α smoothing coefficient = Alpha

This model is included purely for reference purposes. It would not be used in practical applications unless monitored. It forms the basis of models two, five and six.

7.1.2 Model 2 - Exponential Smoothing With Control

This model is based on model 1 but is controlled by means of the tracking signal (refer to section 4.3.2.4).

$$TS = \frac{E_t}{MAD_t}$$

Control is exercised in the following manner:

- a) The limit for the tracking signal is determined from Table 2. It depends on the value of the smoothing factor and confidence level required. In this work a confidence level of 95% has been used.
- b) If successive forecasts produce signals that exceed the limit, it is assumed that a definite trend has been detected. The forecast is recalculated with alpha set to 0.8 and a new tracking signal is calculated.

- c) Alpha is maintained at 0,8 until the tracking signal drops below the limit. Alpha is then reset to the original specified value.
- d) The selected value of alpha equal to 0,8 can be varied to speed up or slow down the model's response. The allowed number of forecasts, where the tracking signal is out of control, can also be altered.

7.1.3 Model 5 - Exponential Smoothing - Run Based Model

This method is also based on equation 1 and the tracking signal. In this instance the value of alpha is reset, in each time period, equal to the absolute value of the tracking signal. Since the model is closely following the sales data, the tracking signal will be very small and the forecast will be stable. When large forecast errors occur, the tracking signal will become large and the model will respond quickly to any changes.

7.1.4 Model 6 - Exponential Smoothing - Run Based Model

This model is adequately explained in section 4.3.5.

7.2 Start Up Conditions For All Models

- a) Forecast for period two equals demand in period one.
- b) Alpha = 0,5 for periods one and two and is then reset to the specified value.
- c) Gamma (the smoothing factor for mean absolute deviation equals 0,3 for periods one and two).

APPENDIX B.3

COMPARISON OF EXPECTED DEMAND VERSUS ACTUAL DEMAND
FOR THE FIRST SET 'A' LOTS

The following rules are shown for all four
 models.

Page 108

Note the following points:

- (1) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (2) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (3) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (4) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (5) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (6) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (7) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (8) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (9) The demand curve is downward sloping (see Fig. 2.1; curve VI).
- (10) The demand curve is downward sloping (see Fig. 2.1; curve VI).

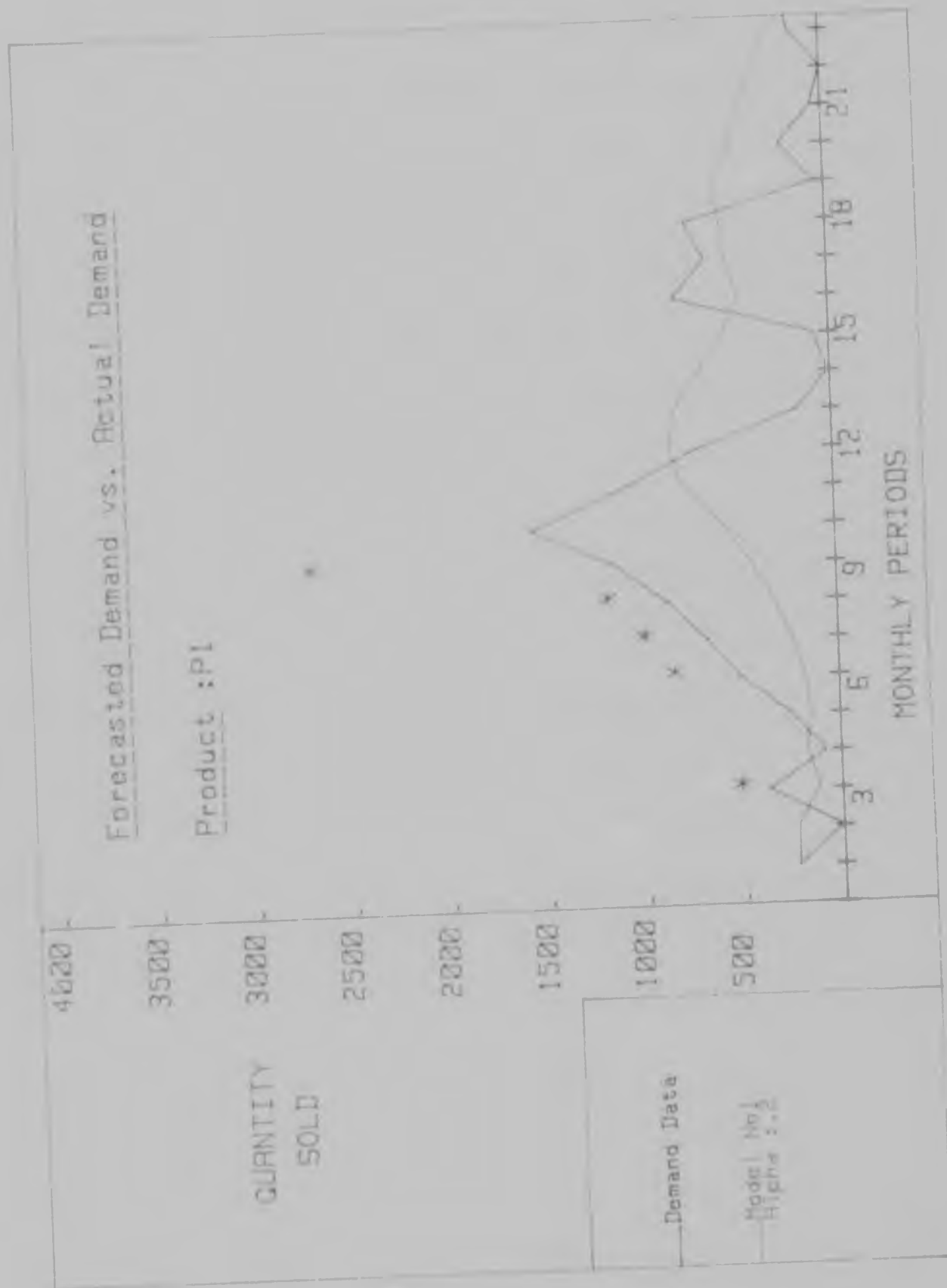


FIGURE 11

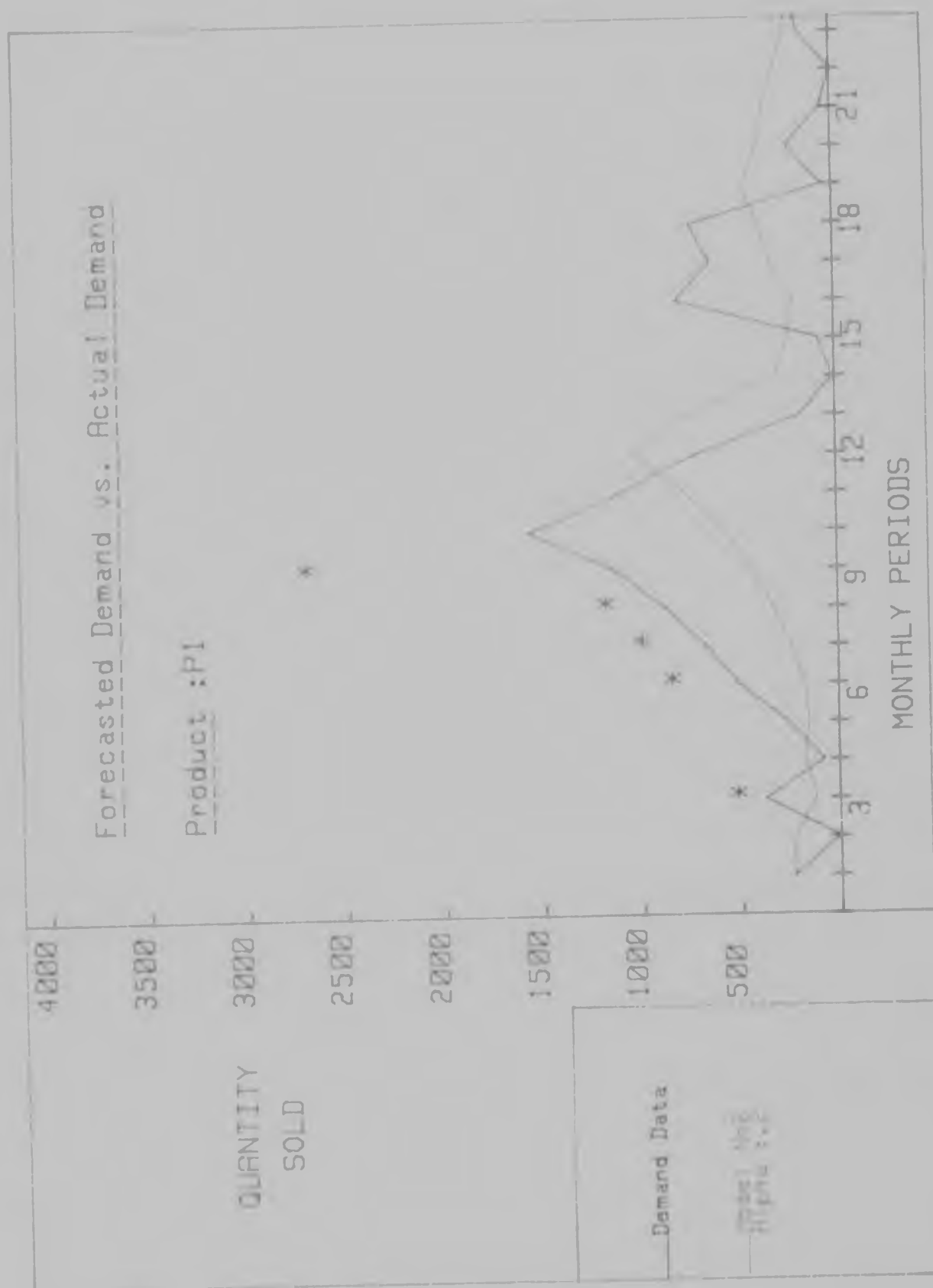


FIGURE 12

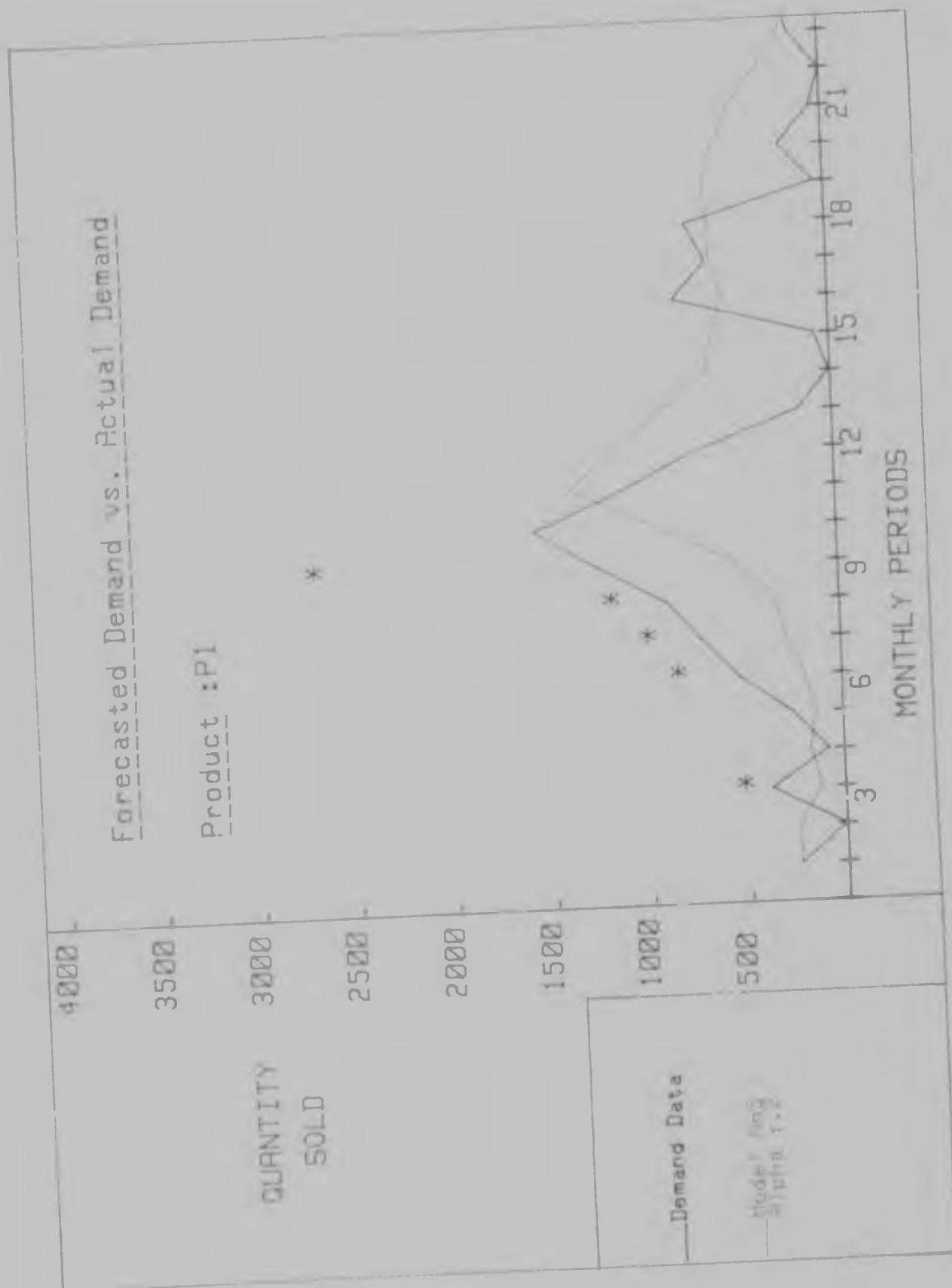


FIGURE 13

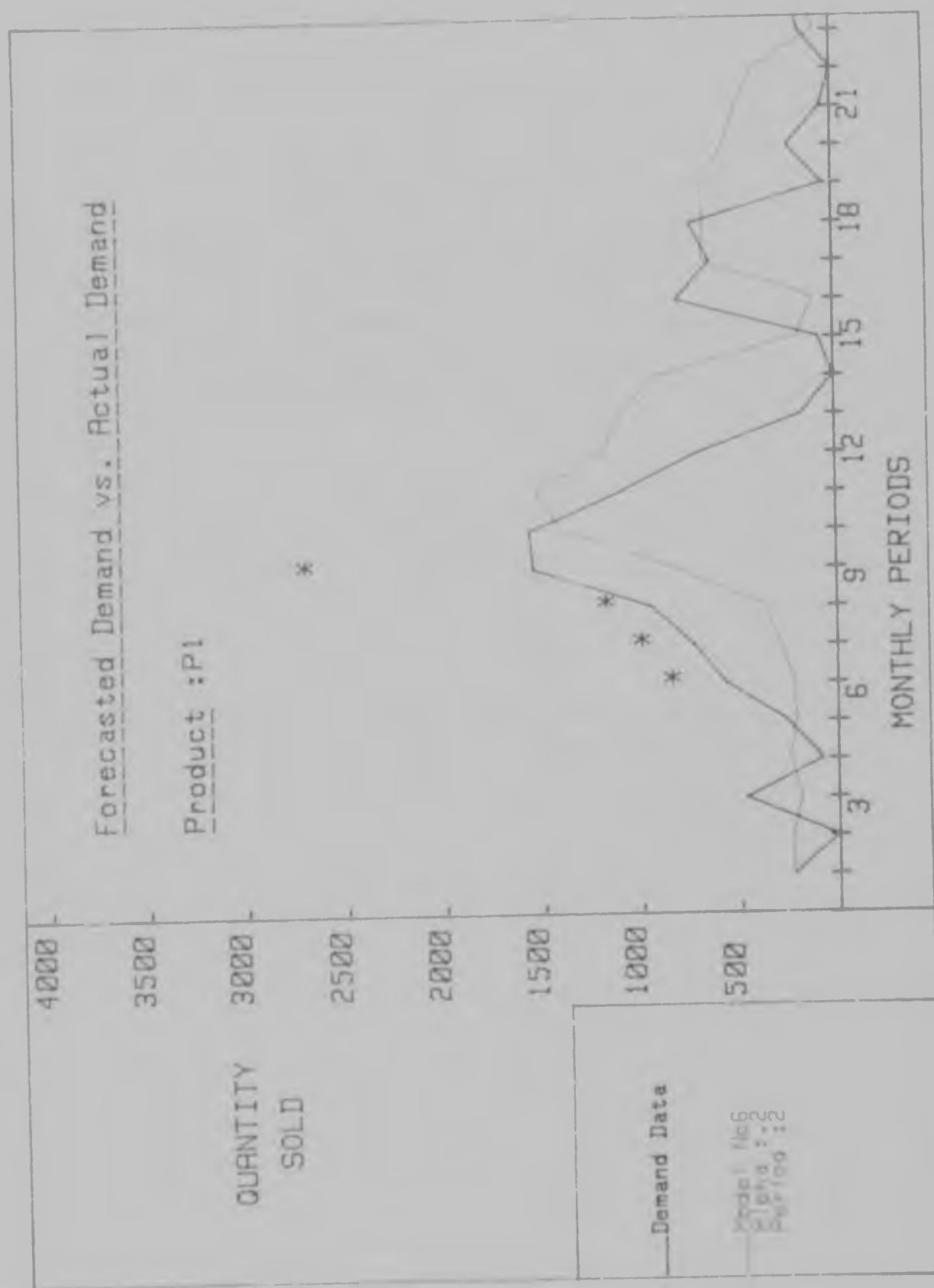


FIGURE 14

7.3.2 Product 1 P2

Note the following points:

- a) Demand variability is 94% (ref Appendix 2.1; table 11)
- b) Model 1 produces the smoothest forecast but badly lags the upward trend.
- c) Model 6 follows the trend most closely.
- d) External marketing information is required to forecast an increase in demand for this item.

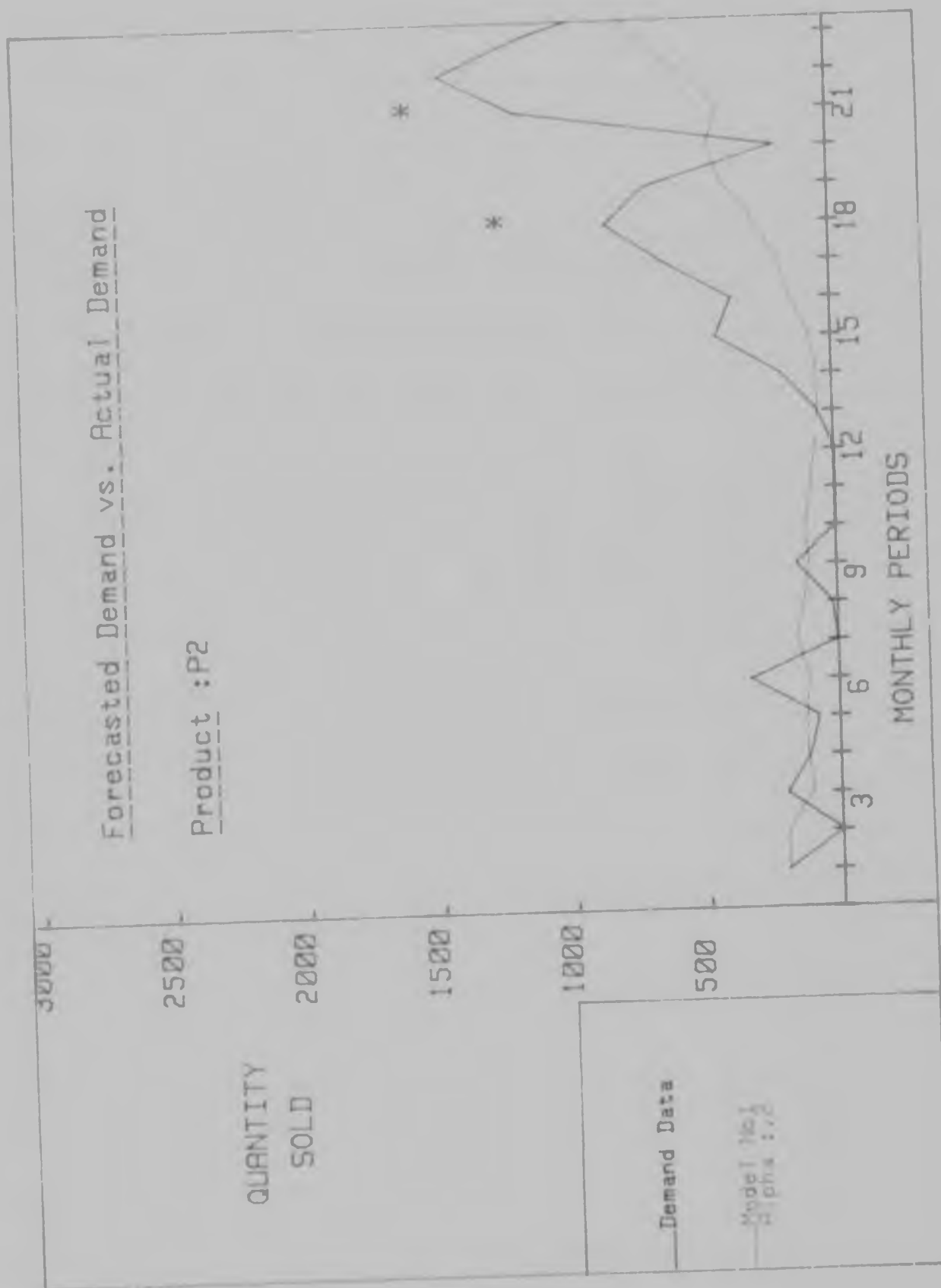


FIGURE 15

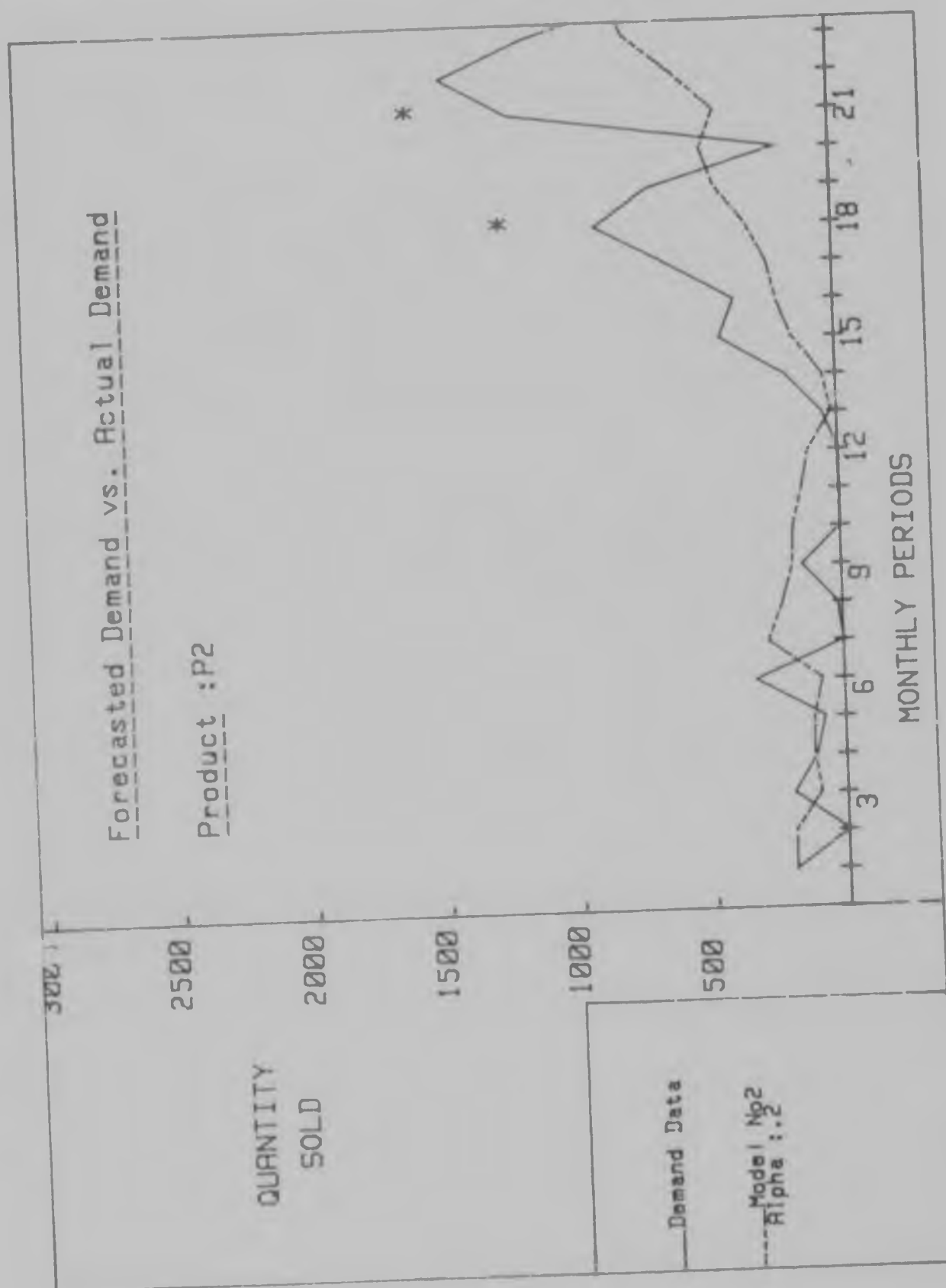


FIGURE 16

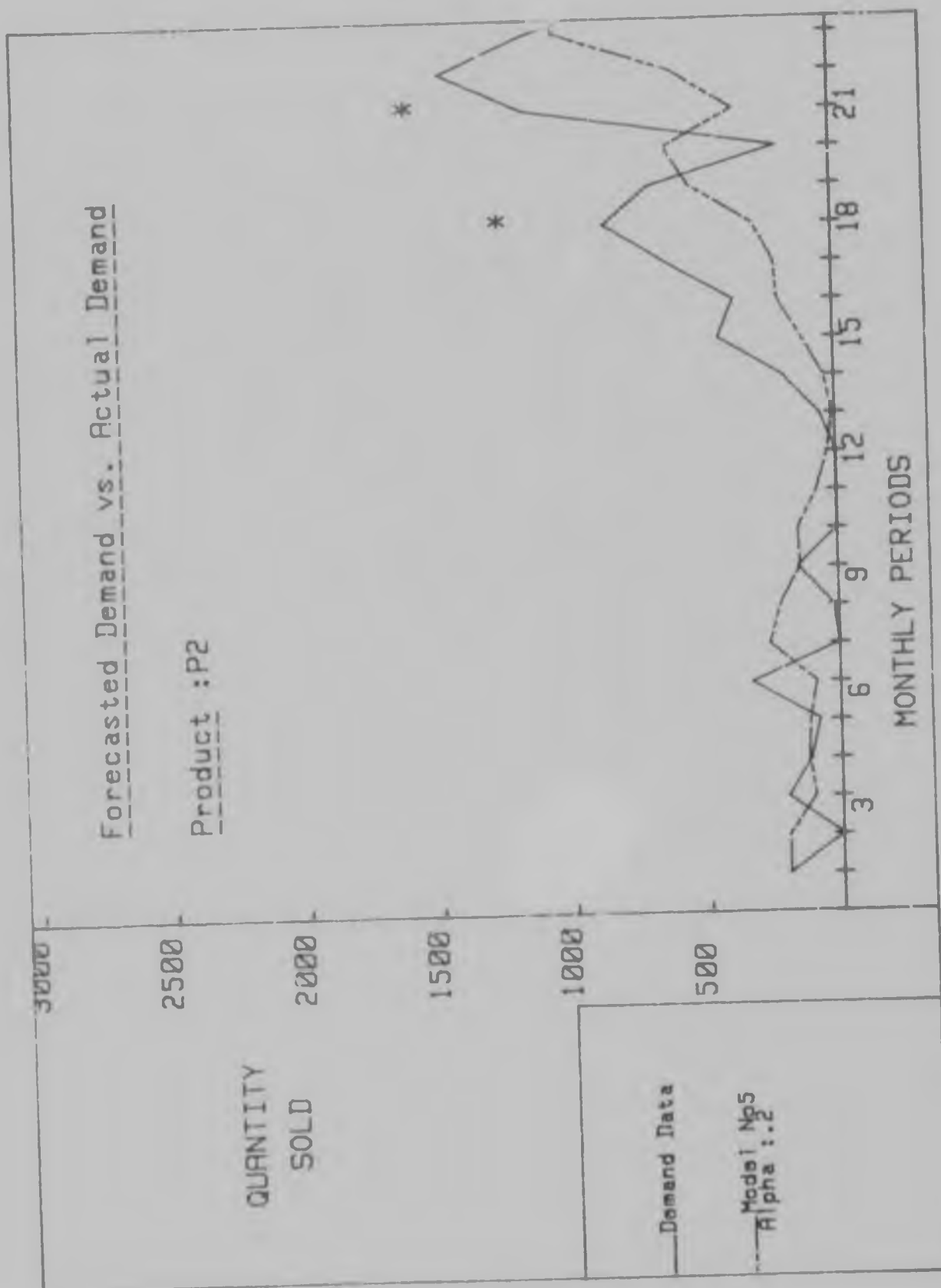


FIGURE 17

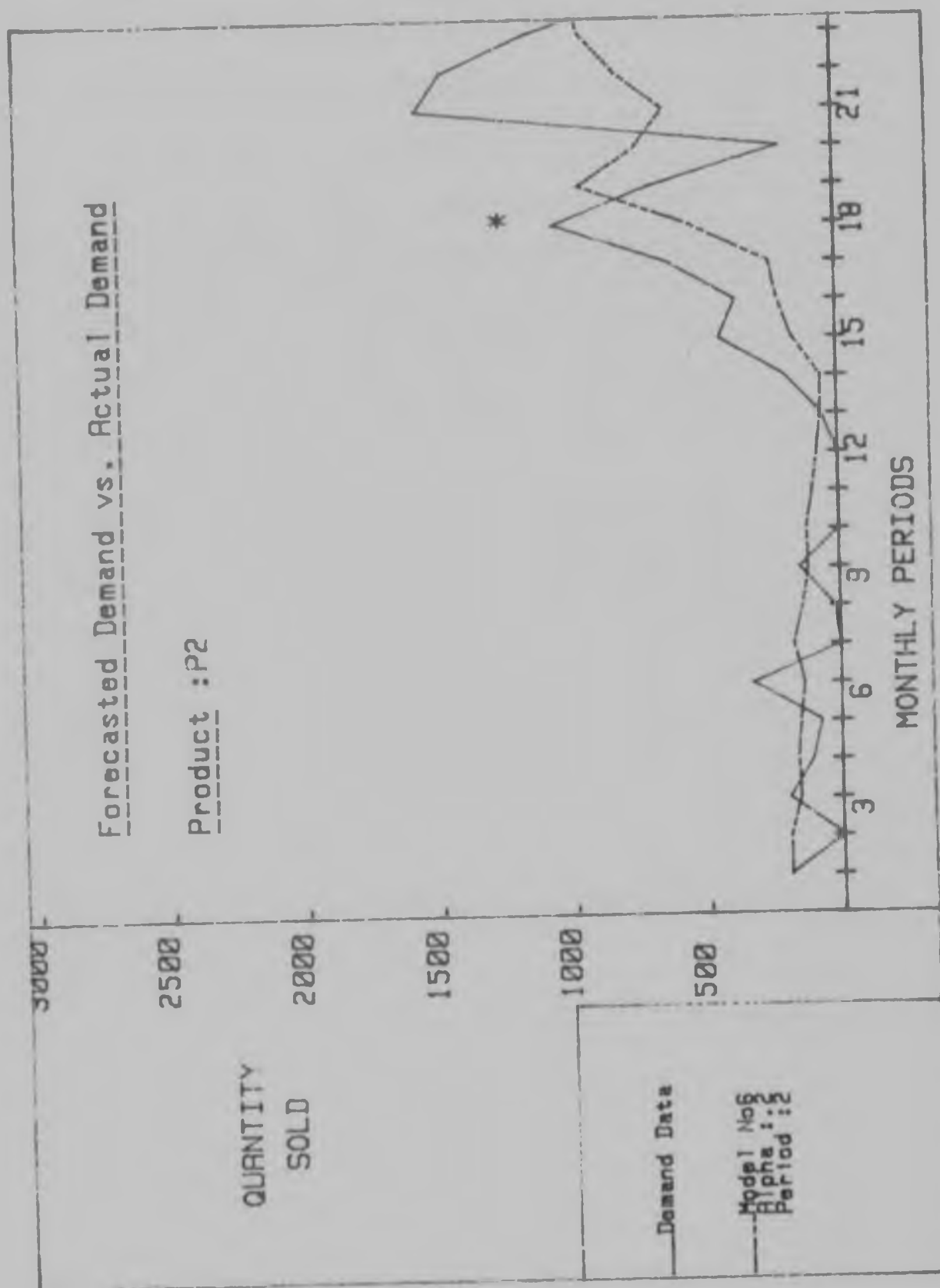


FIGURE 18

7.3.3 Product : P3

Note the following points:

- a) The demand variability is 37% (Ref Appendix 2.1; Table 11)
- b) All models follow the sales data fairly well.
- c) Model one's slow response to the change in demand level is clearly evident.

7.3.3 Problem 3 P3

Write the following points

- a) The demand variability is 3% (see Appendix 2.1; Table 11)
- b) All models follow the sales data fairly well.
- c) Retailer's response to the change in demand level is quite slow.

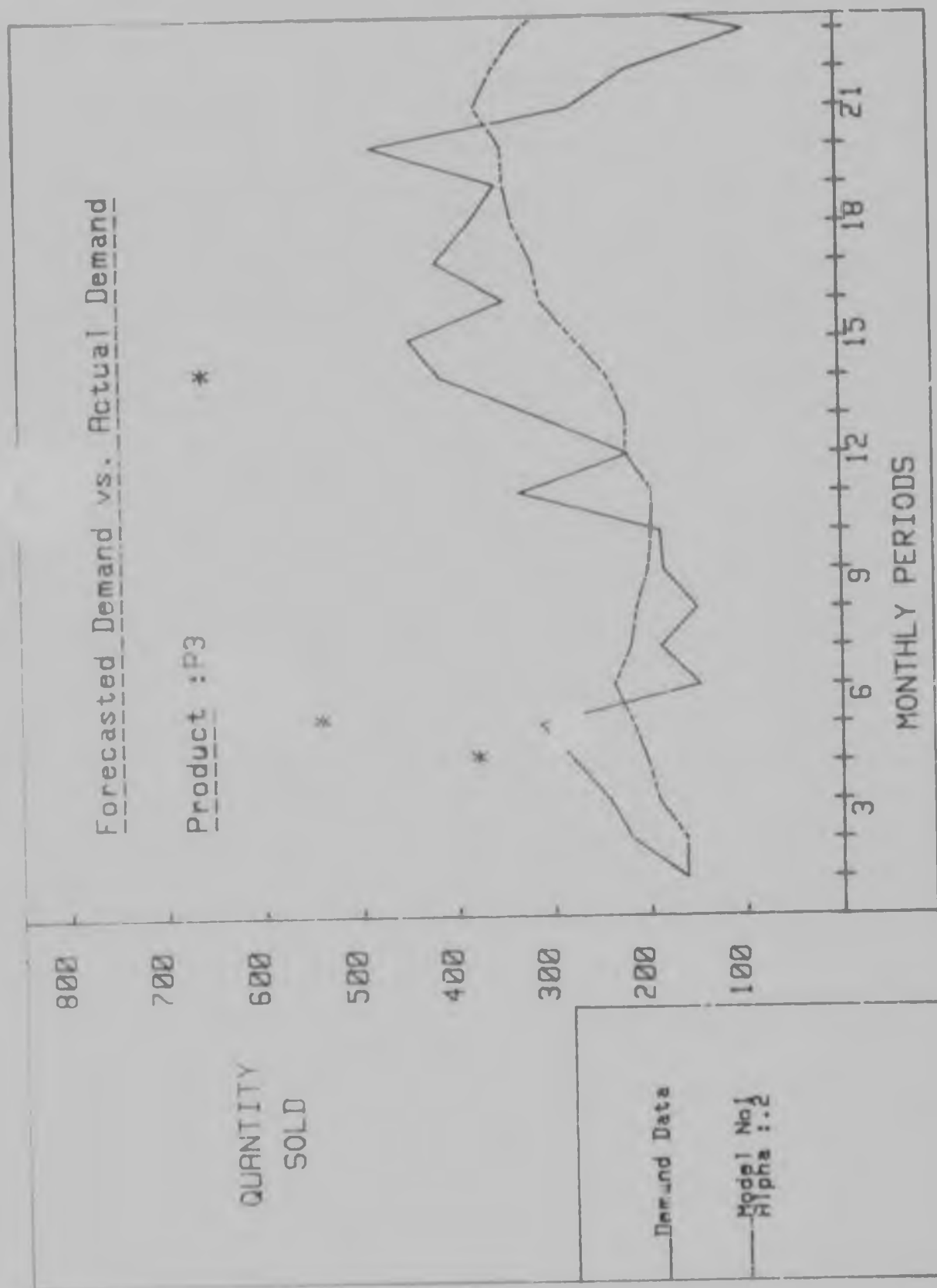


FIGURE 19

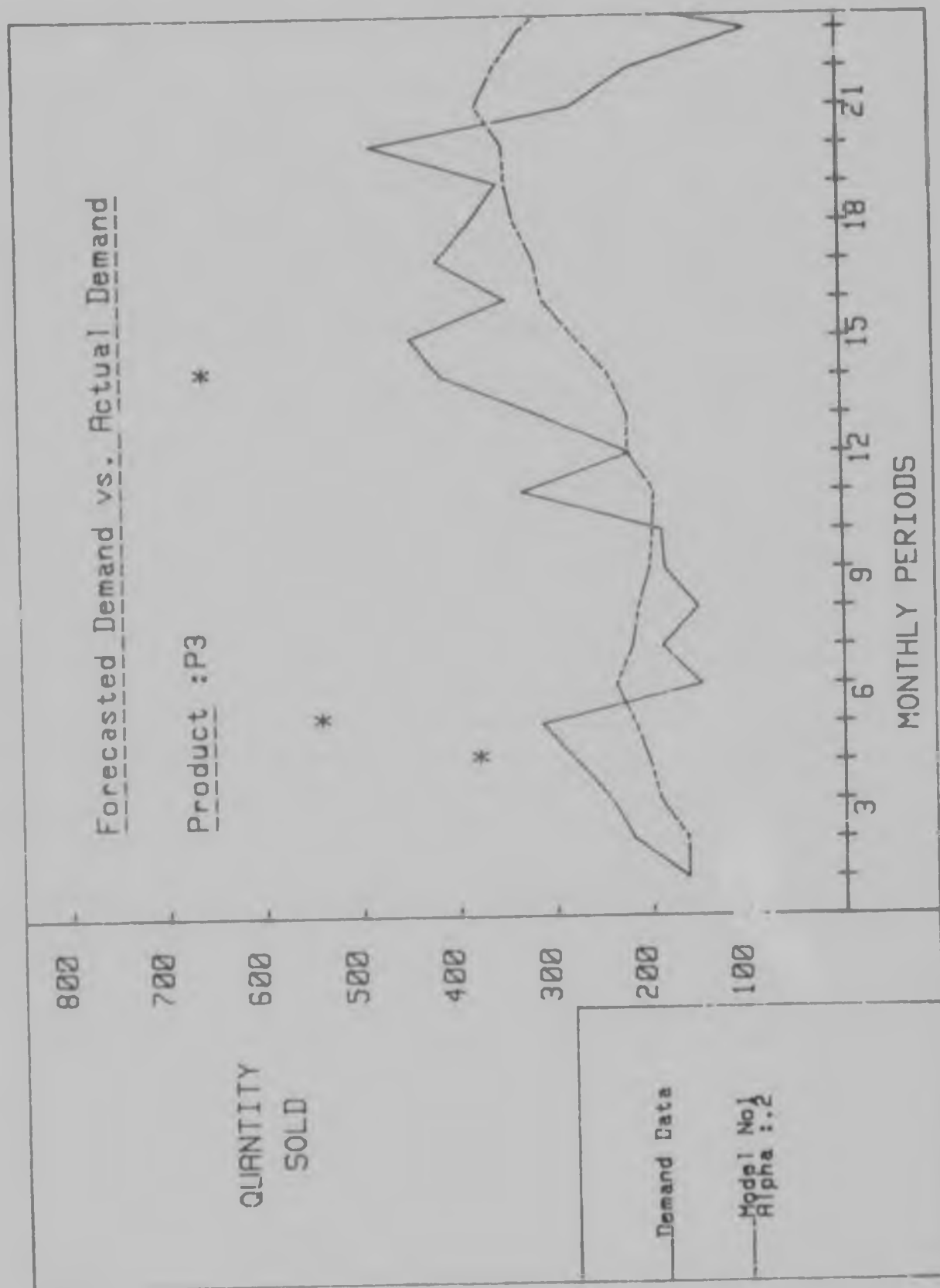


FIGURE 19

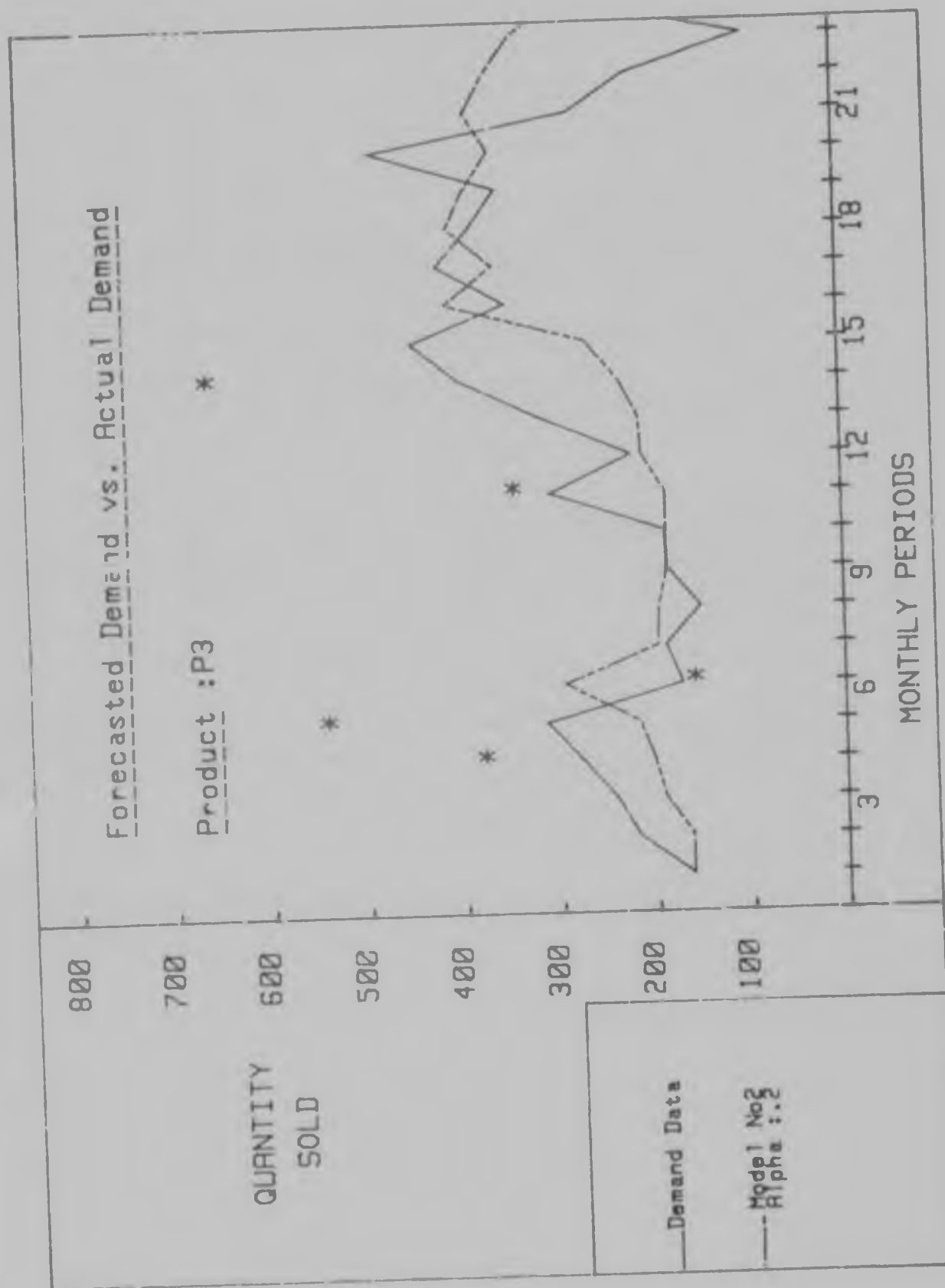


FIGURE 20

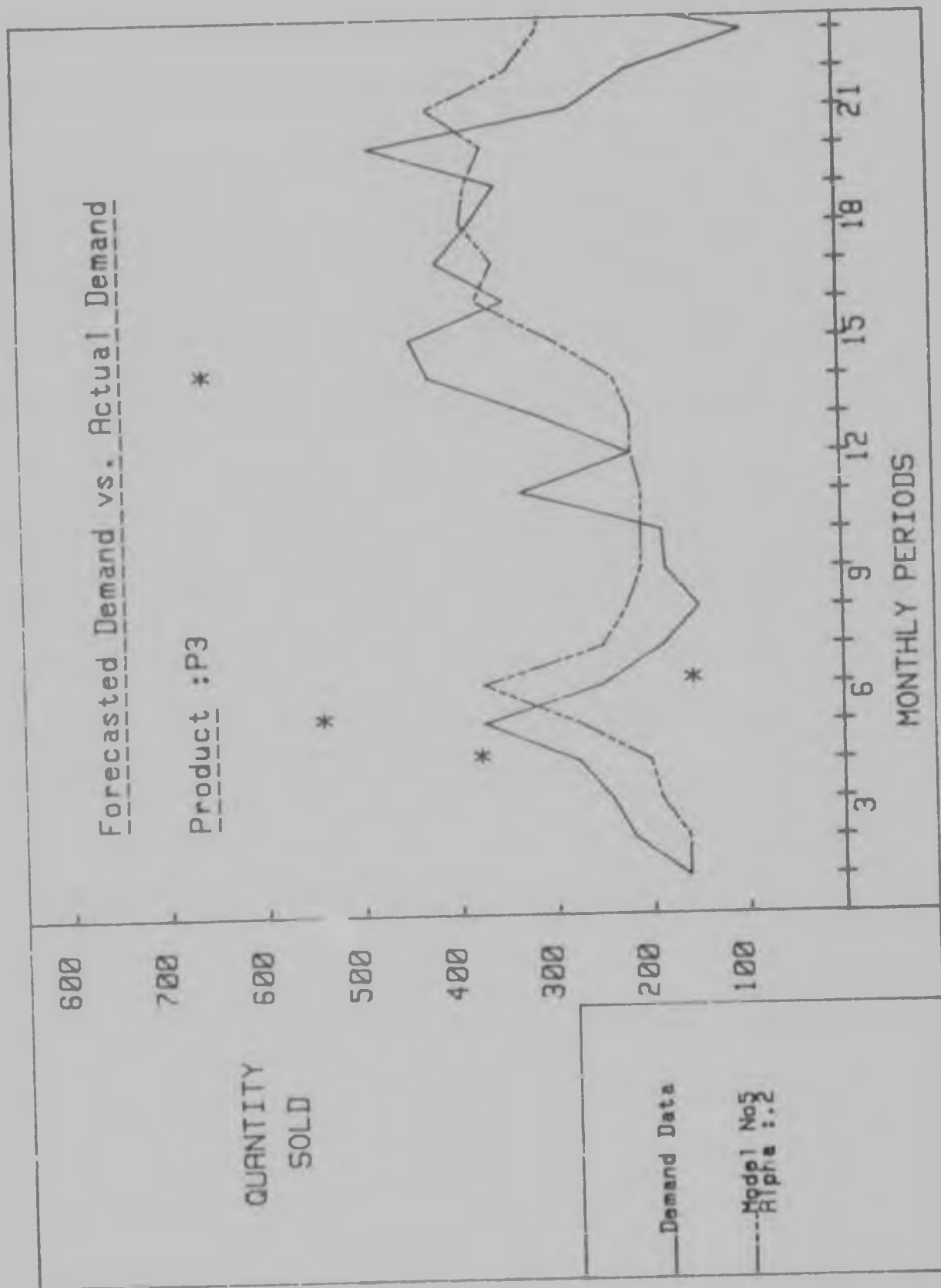


FIGURE 21

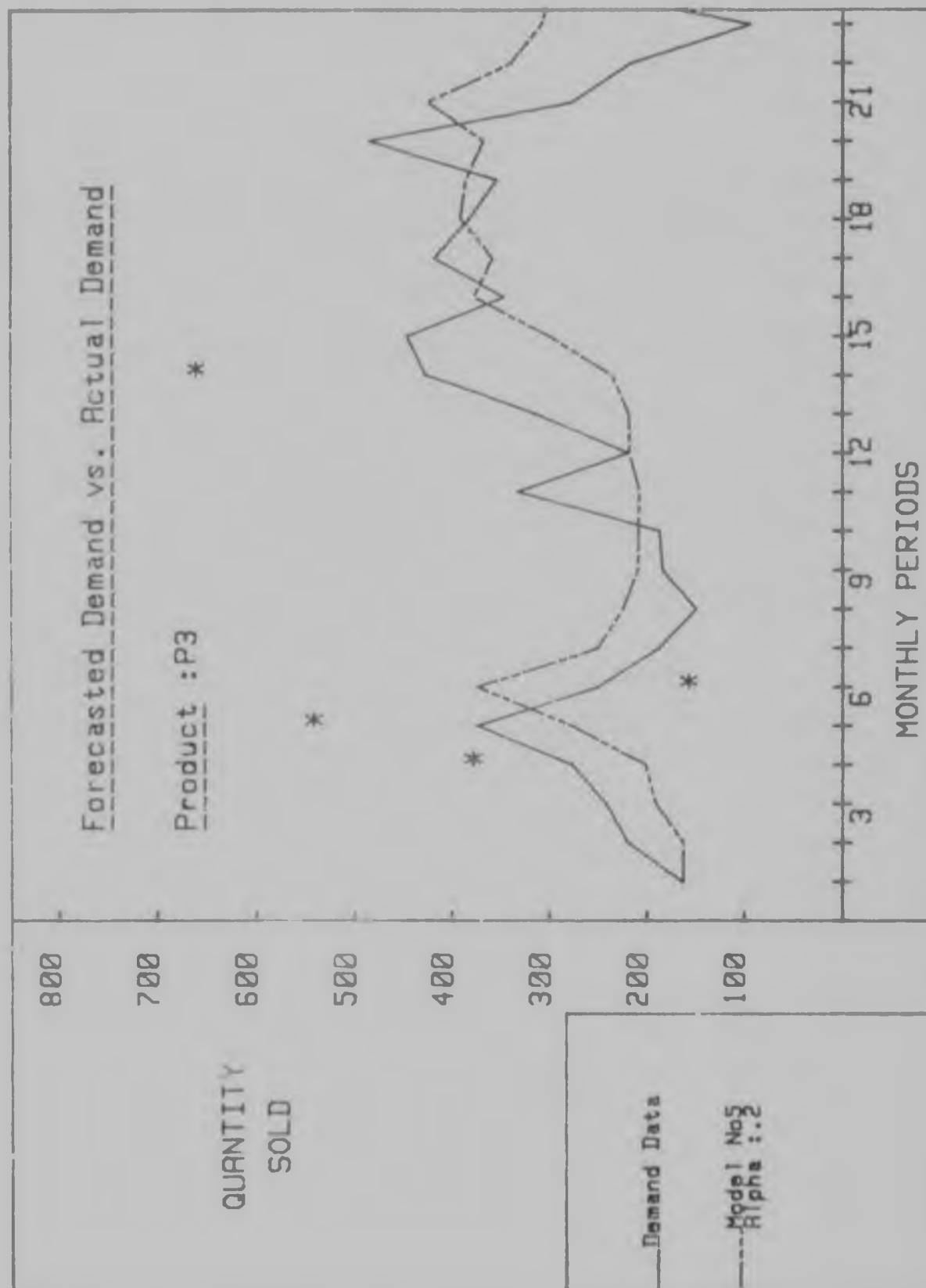


FIGURE 21

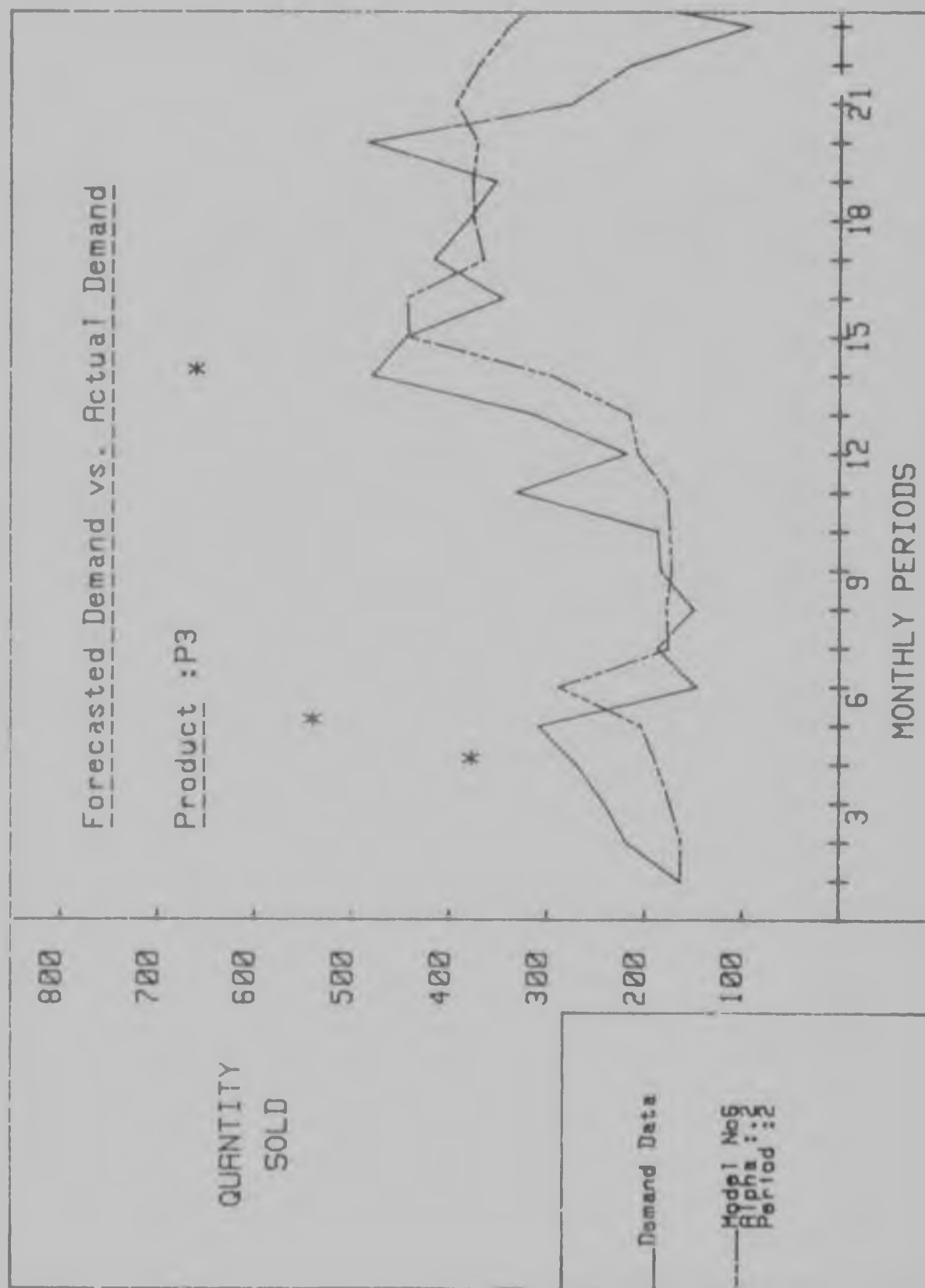


FIGURE 22

7.3.4 Product 1 P4

Note the following points:

- a) The demand variability is 44% (cf Appendix 2.1; Table 11)
- b) All models follow the sales data well.
- c) A lot of filtering of the early demand periods occurs due to the start up conditions of the model.

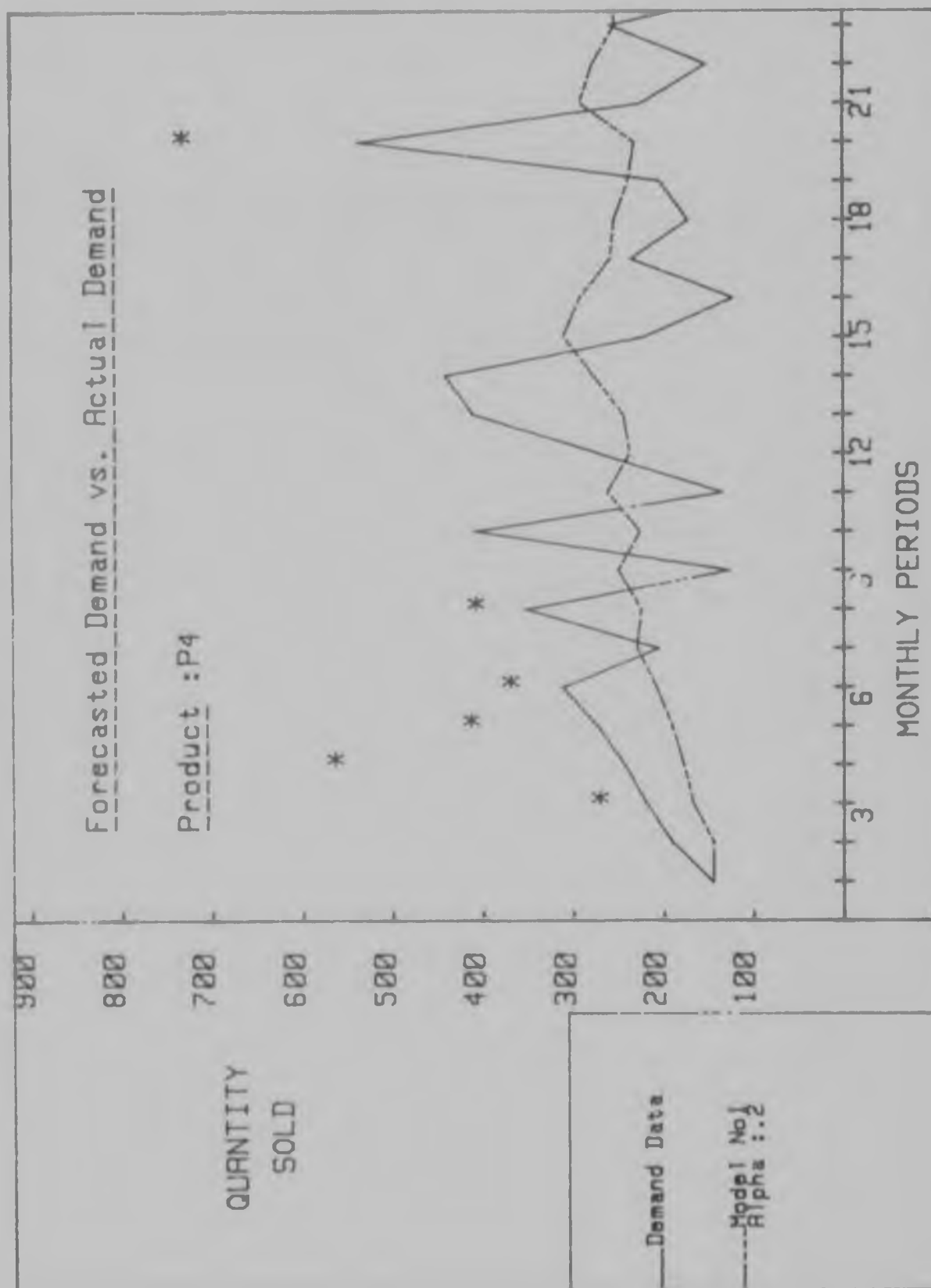


FIGURE 23

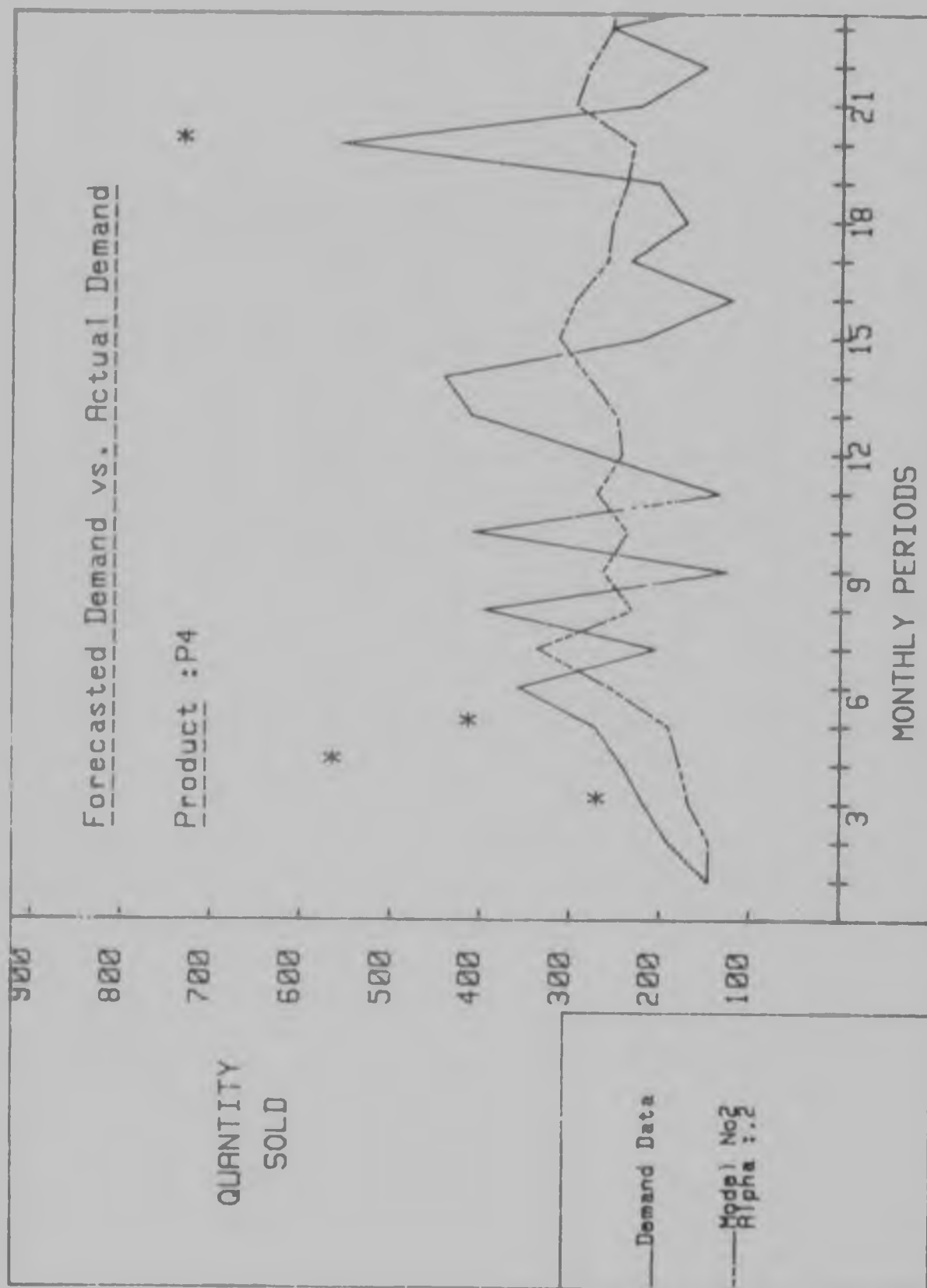


FIGURE 24

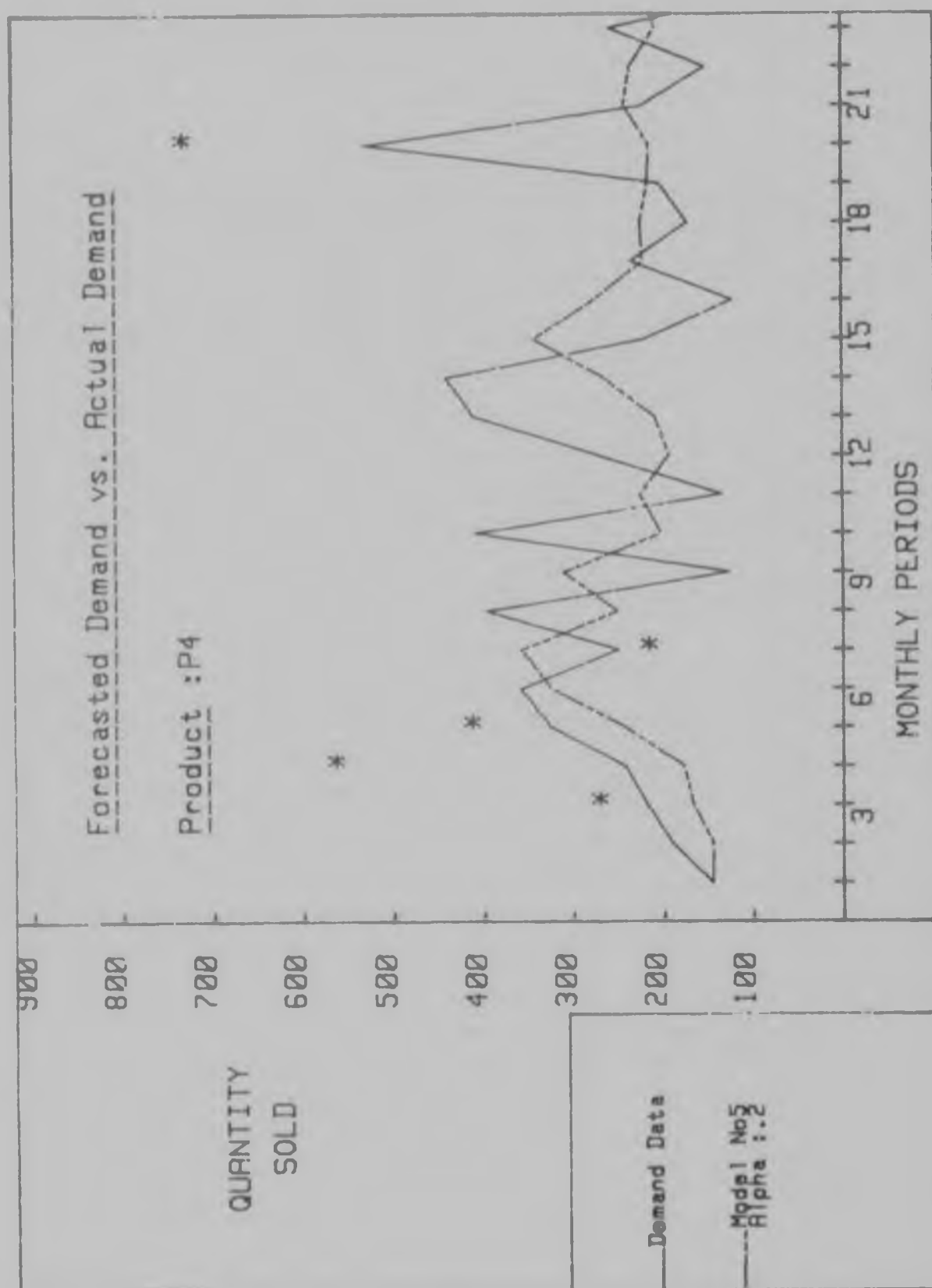


FIGURE 25

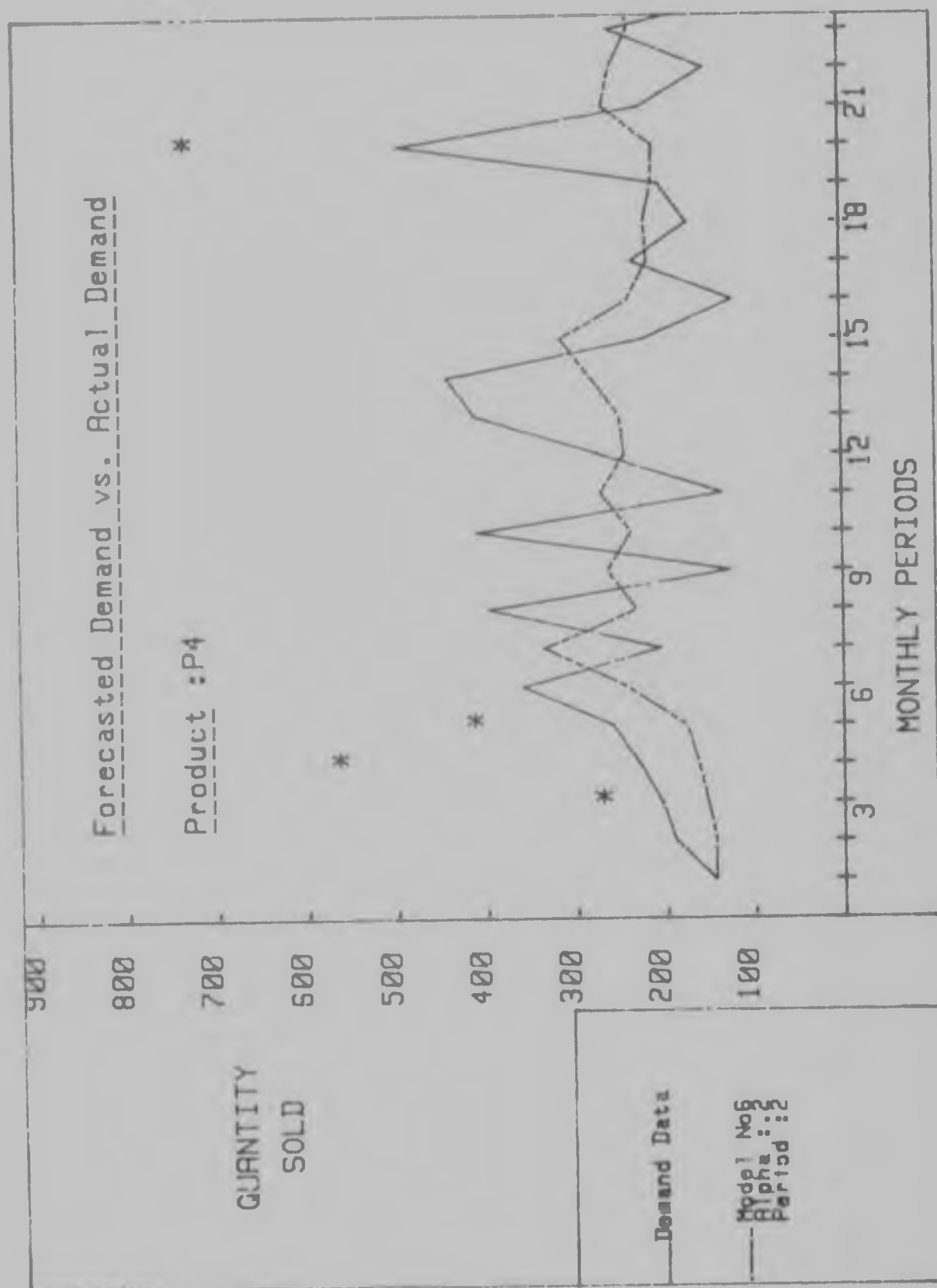


FIGURE 26

7.3.5 Product : P5

Note the following points:

- a) The demand variability is 5% (Ref Appendix 2.5 Table 11)
- b) The demand is very erratic
- c) The forecast tends to lag the demand trend.

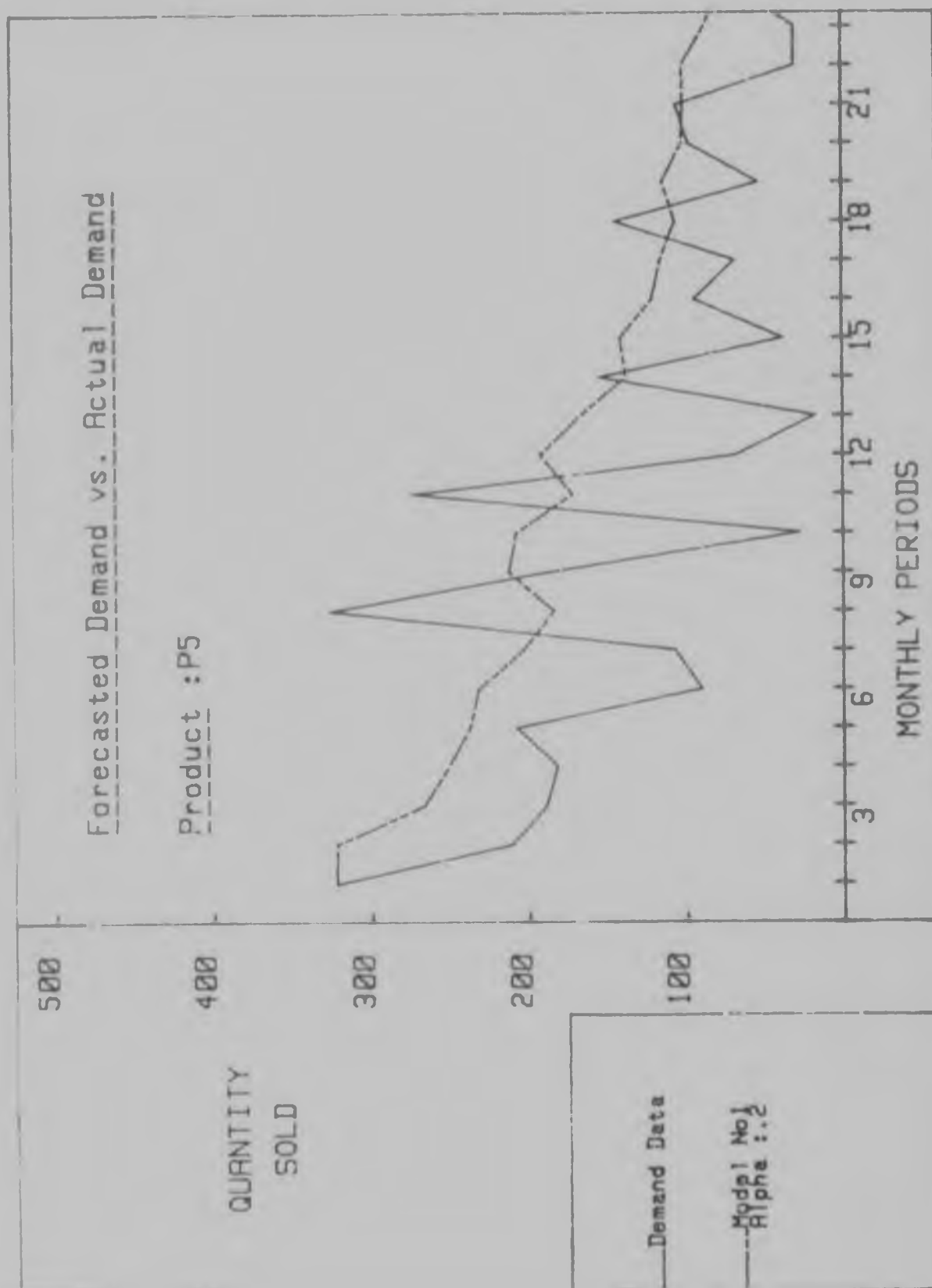


FIGURE 27

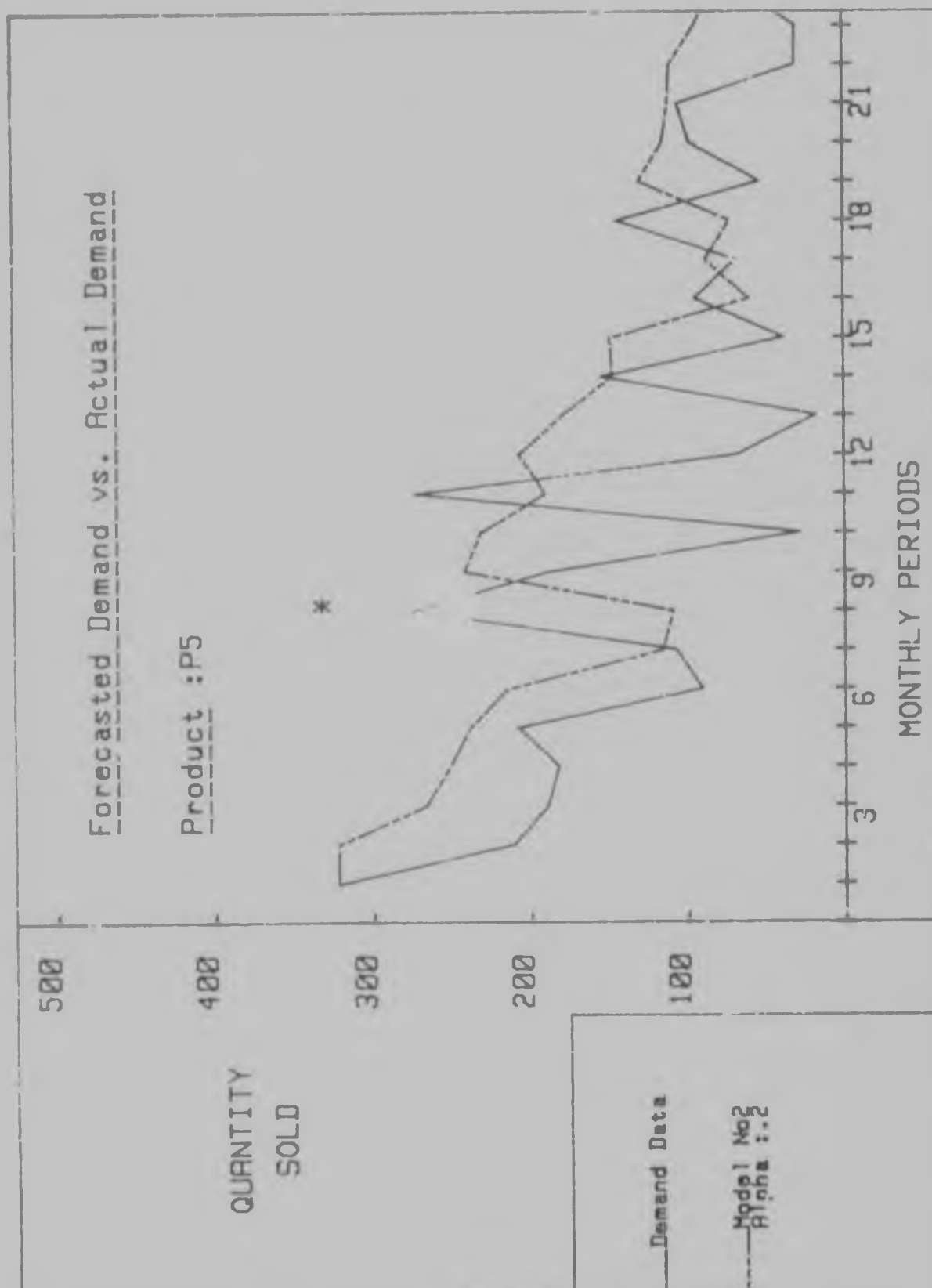


FIGURE 28

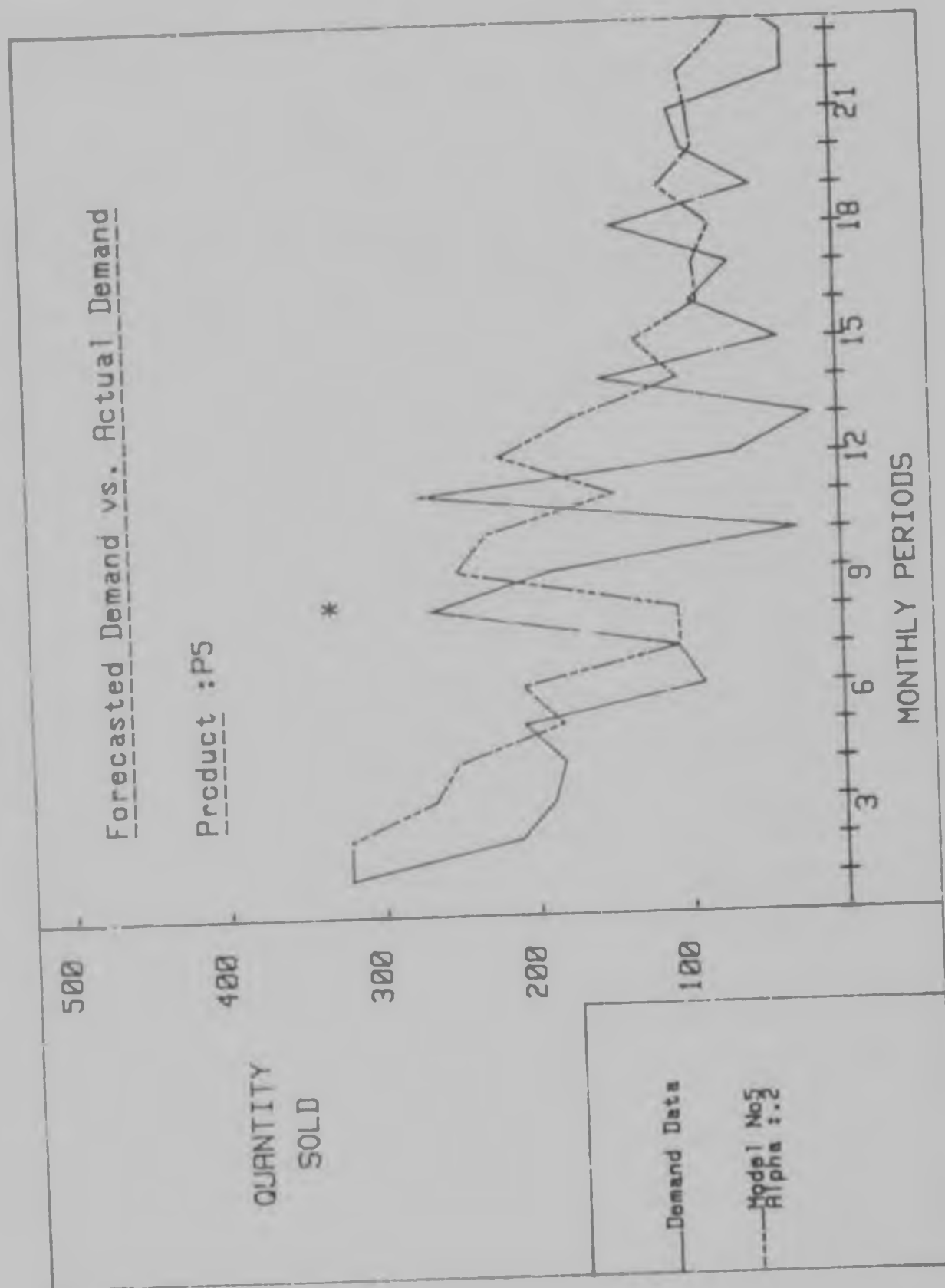


FIGURE 29

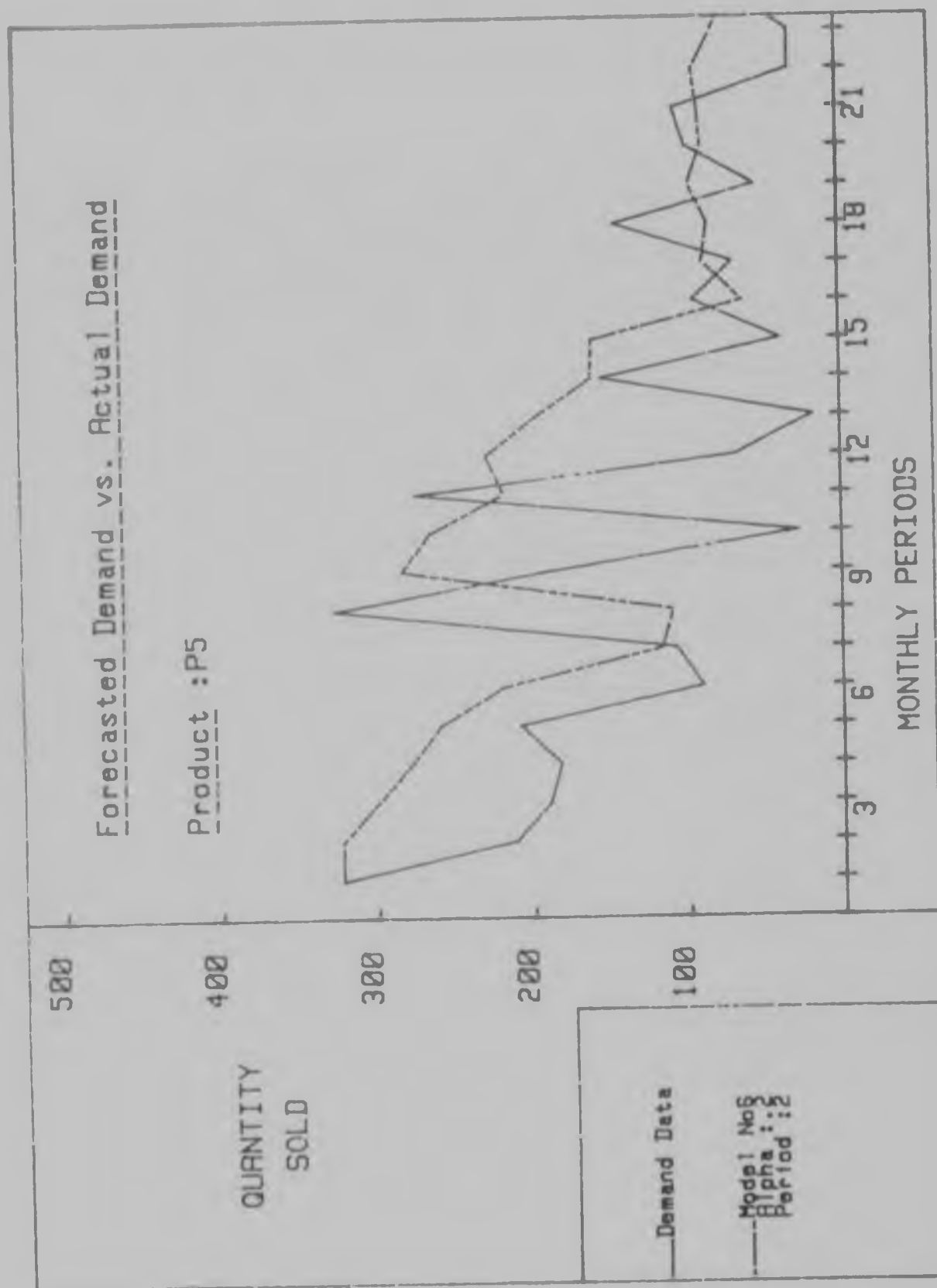


FIGURE 30

7.3.9 *Product* : B6

note the following points:

- a) The annual variability is 47% (Ref Appendix 2.4; Table 11)
- b) The annual pattern is horizontal.
- c) There is very little noticeable difference between the months.

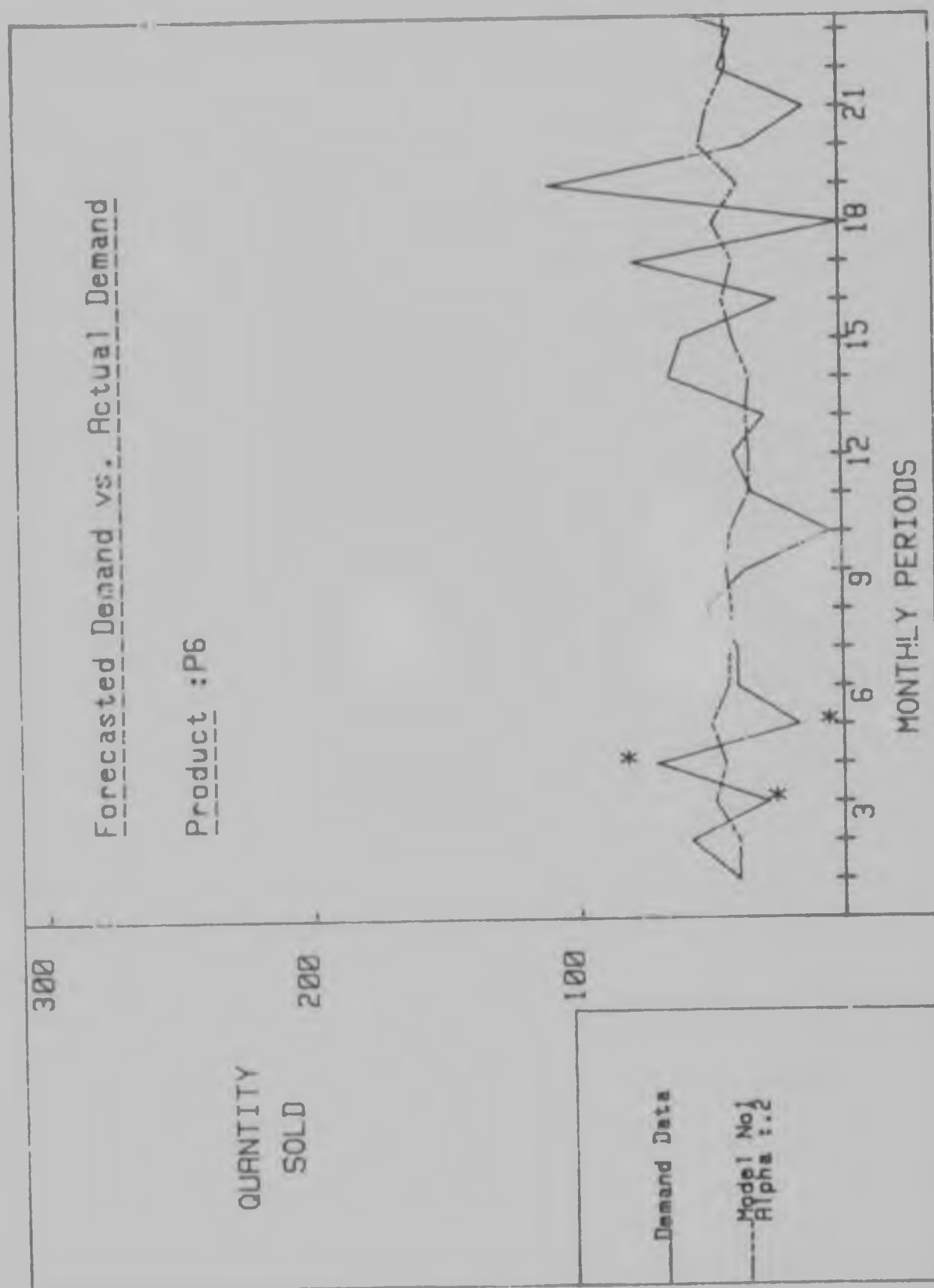


FIGURE 31

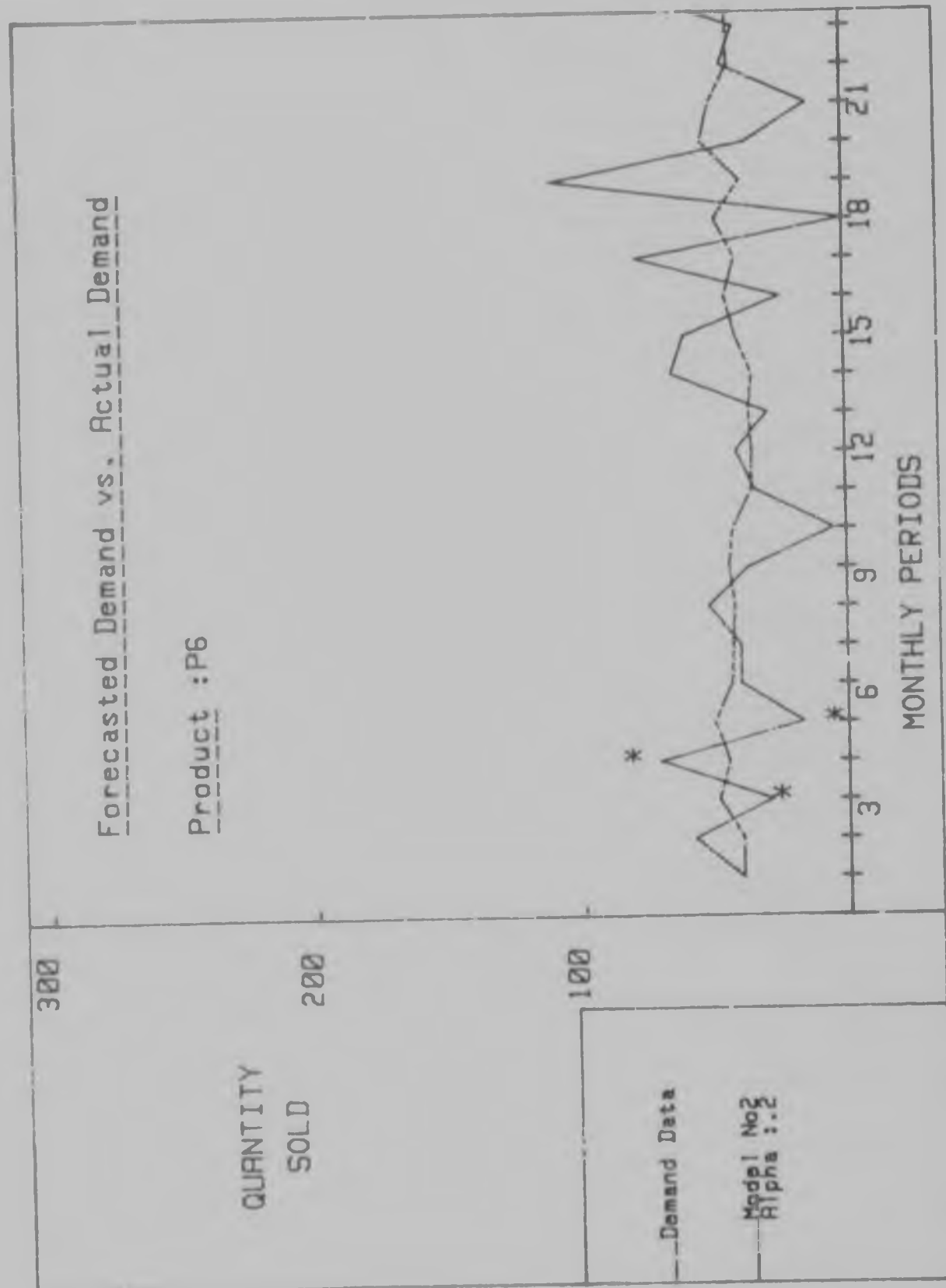


FIGURE 32

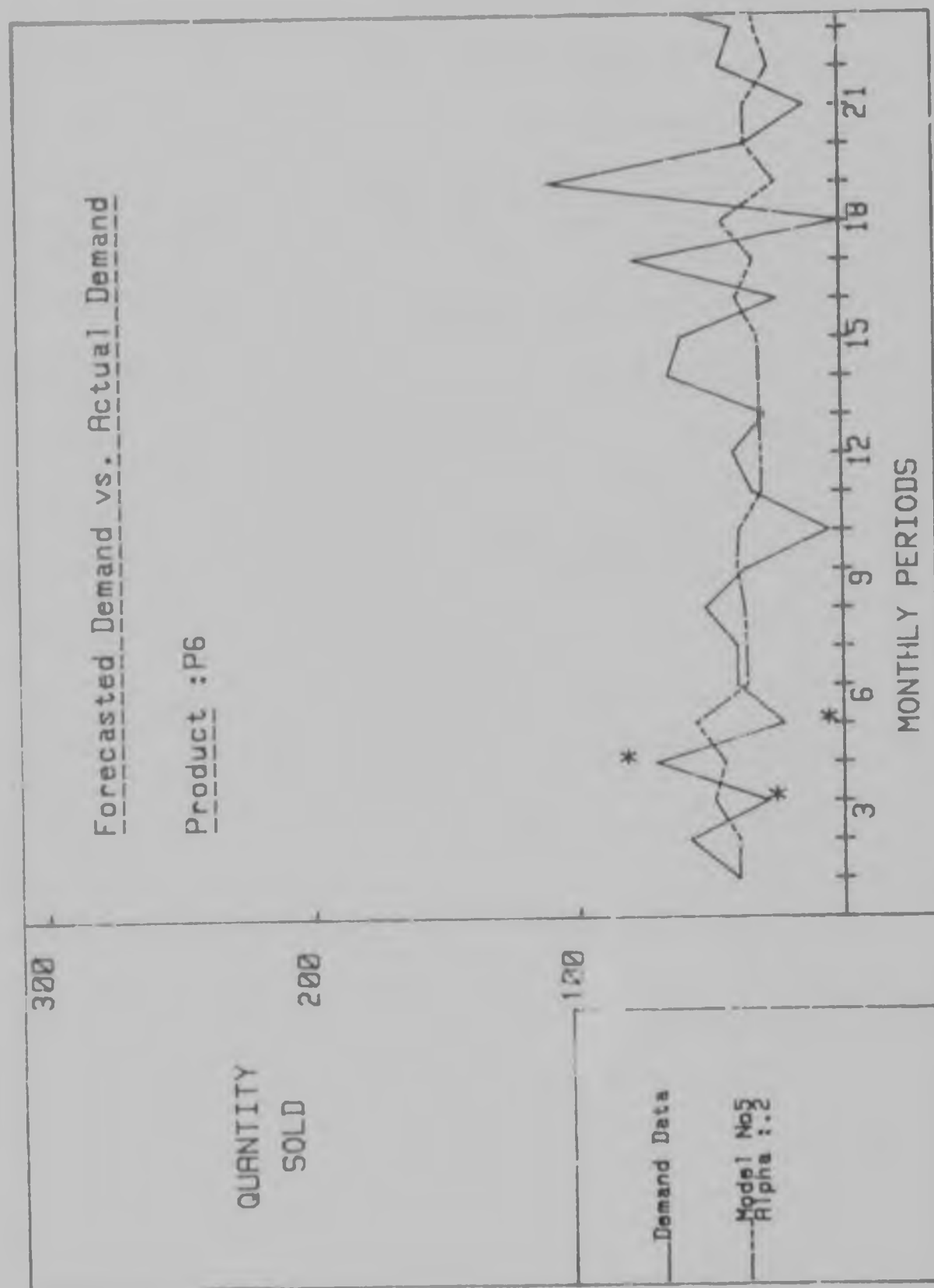


FIGURE 33

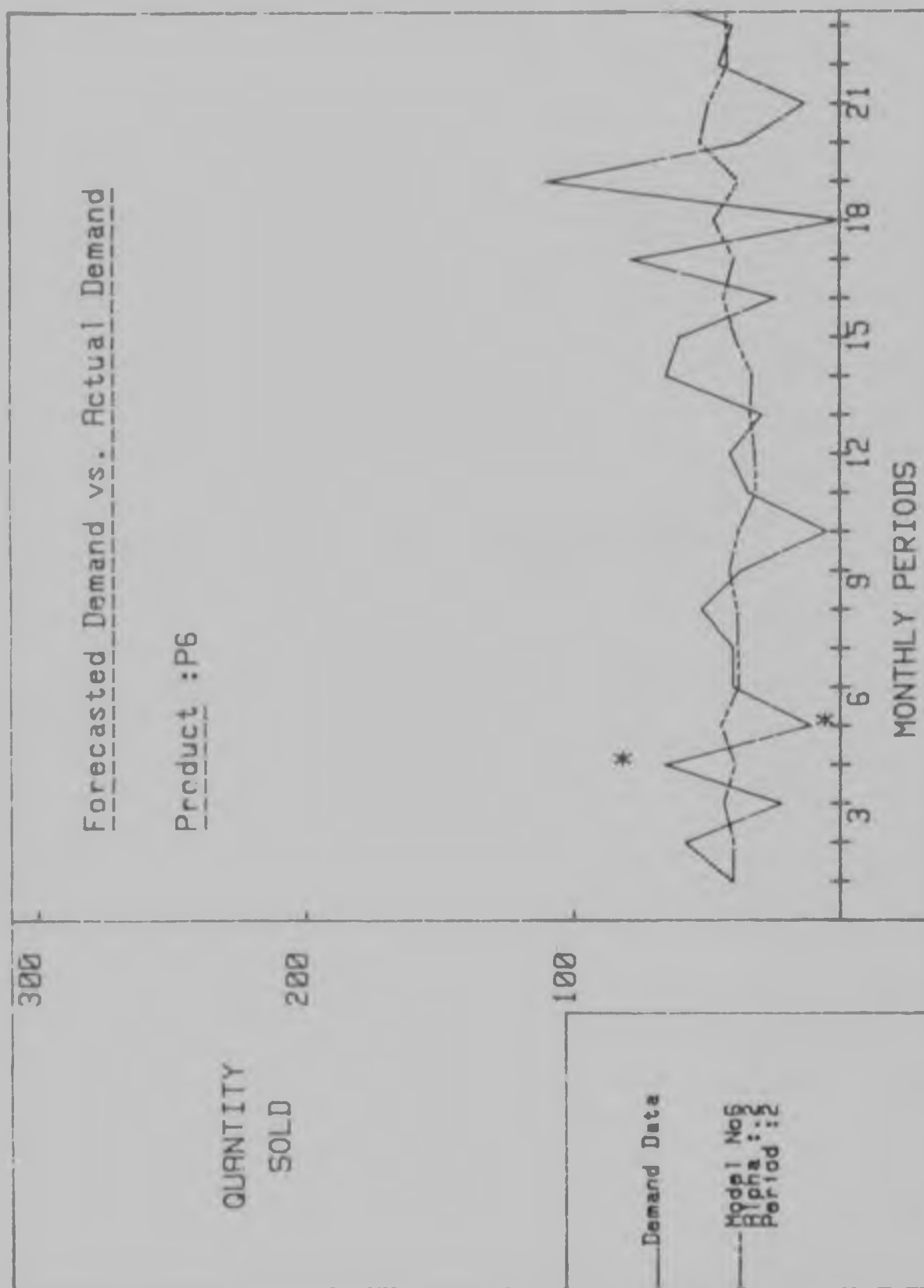


FIGURE 34

APPENDIX 5

TABLES AND CHARTS SHOWING THE RESULTS OF THE
FOLLOW-UP STUDY

THE DATA FROM THE FOLLOW-UP STUDY SELECTED FOR
FURTHER ANALYSIS.

APPENDIX B.1

FORECASTING RESULTS FOR P1

TABLE 17.1
FORECASTING RESULTS FOR P1

Models	Alpha	Total Forecast Error	M.A.D.	Forecast Exceeds Total Demand	Tracking Signal at End of Run
1	0,2	-430	170	-3,3	-
2*	0,2	979	294	7,5	0,02
5	-	1198	316	9,2	0,48
6*	0,2 P=2	1661	339	12,7	0,44
2	0,1	932	285	7,1	0,05
2	0,3	43	301	0,3	0,3
6	0,1 P=2	2091	366	16,0	0,49
6	0,3 P=2	1287	315	9,8	0,39
6	0,2 P=3	2184	373	16,7	0,52
6	0,2 P=4	2037	365	15,6	0,52

* Initial model selected from initial run for further testing.

In the time series model for forecasting by time series

analysis, the model is able to handle the sudden changes in demand.

However, only the period considered, model 2 (alpha = 0,1)

produces the best results.

TABLE 17.2
FORECASTING RESULTS USING MODEL 2 WITH ALPHA EQUAL TO 0.2

INITIAL VALUE OF SMOOTHING FACTOR .50
SMOOTHING FACTOR FOR ERROR & TEND .10
NO. OF PERIODS BEFORE ERROR ARE SUMMED 2.00
ALPHA VALUE WHEN FORECAST IS OUT OF CONTROL .80
TRACKING SIGNAL MUST NOT EXCEED .50
AFTER THESE PERIODS, THE FACTORS ARE RESET
RESET VALUE OF ALPHA .20
RESET VALUE OF GAMMA .10

P1

PERIOD	FILTER DEMAND	ACTUAL DEMAND	NEXT PERIOD FCST	CUSUM	ERRUP	SMOOTH M.A.D.	ALPHA	TRACK-SIGNAL
1	232	232	232	0	0	0.0	.50	0.00
2	0	0	232	0	232	232.0	.50	1.00
3	875	875	171	0	255	86.0	.20	.81
4	0	0	171	0	81	87.4	.20	.87
5	259	259	171	-16	-107	89.1	.20	.78
6	308	308	243	-350	-318	113.0	.20	-1.88
7	0	0	243	-778	-826	144.9	.20	-1.35
8	0	0	435	-1428	-542	184.3	.20	-1.54
9	1127	2694	570	-2017	-693	225.0	.20	-1.68
10	1559	1559	780	-2999	-946	310.5	.20	-1.79
11	1180	1180	1088	0	-330	312.5	.20	-1.80
12	785	785	770	0	329	314.2	.20	-1.81
13	170	170	139	601	601	316.0	.20	-1.82
14	0	0	234	803	292	336.8	.20	-1.16
15	0	0	283	1016	151	348.4	.20	-1.31
16	790	790	322	811	-595	346.0	.20	-1.37
17	624	624	363	119	-302	341.6	.20	-1.43
18	726	726	451	-284	-342	340.0	.20	-1.27
19	53	53	372	199	310	347.9	.20	-1.21
20	245	245	342	349	147	327.3	.20	-1.30
21	55	55	295	421	287	328.1	.20	-1.00
22	0	0	278	910	385	319.5	.20	-1.00
23	181	181	214	979	67	294.2	.20	-1.02

EVALUATION REPORT

NO OF FORECASTS HIGH 10.0
AMOUNT FORECASTED HIGH 2639.0
NO OF FORECASTS LOW 10.0
AMOUNT FORECASTED LOW -4659.0
M.A.D. AT END OF RUN 294.2

TABLE 17.3
FORECASTING RESULTS USING MODEL 2 WITH ALPHA EQUAL TO 0.1

INITIAL VALUE OF SMOOTHING FACTOR .50
SMOOTHING FACTOR FOR ERROR & MAD .20
NO OF PERIODS BEFORE FORECASTS ARE MADE .00
ALPHA VALUE WHEN FORECAST IS OUT OF CONTROL .00
TRACKING SIGNAL MUST NOT EXCEED .42
INITIAL VALUE OF GAMMA .10
INITIAL VALUE OF GAMMA .10

P1

PERIOD	FILTER	ACTUAL DEMAND	PERIOD FORECAST	ERROR	MADE	SMOOTH	MADE	TRACKING
1	233	233	233	0	0	0.0	0.0	0.0
2	0	6	128	122	0	66.1	128	0.0
3	37	487	14	473	255	66.8	14	0.0
	80	80	139	59	65	64.6	139	0.0
	259	259	151	108	-120	60.2	151	0.0
4	481	792	184	608	-331	112.5	184	0.0
7	686	944	226	760	422	143.4	226	0.0
8	764	1127	280	883	-530	182.9	280	0.0
9	965	2644	340	2304	-60	233.2	340	0.0
10	122	1559	1848	326	0	97.3	1848	0.0
11	1180	1180	1090	90	-52	272.0	1090	0.0
12	705	705	782	77	385	204.0	782	0.0
13	170	170	292	122	612	316.3	292	0.0
14	0	0	264	264	284	313.5	264	0.0
15	81	81	246	165	183	308.5	246	0.0
16	790	790	301	489	552	325.6	301	0.0
17	624	624	333	291	-323	325.4	333	0.0
18	720	720	372	348	-393	332.1	372	0.0
19	53	53	341	288	319	348.9	341	0.0
20	225	225	329	104	116	385.3	329	0.0
21	55	55	382	327	274	385.9	382	0.0
22	0	0	271	271	382	385.4	271	0.0
23	161	161	260	99	110	285.9	260	0.0

EVALUATION REPORT

NO OF FORECASTS HIGH 10.0
AMOUNT FORECASTED HIGH 2649.0
NO OF FORECASTS LOW 10.0
AMOUNT FORECASTED LOW 4291.7
M.A.D. AT END OF RUN 285.9

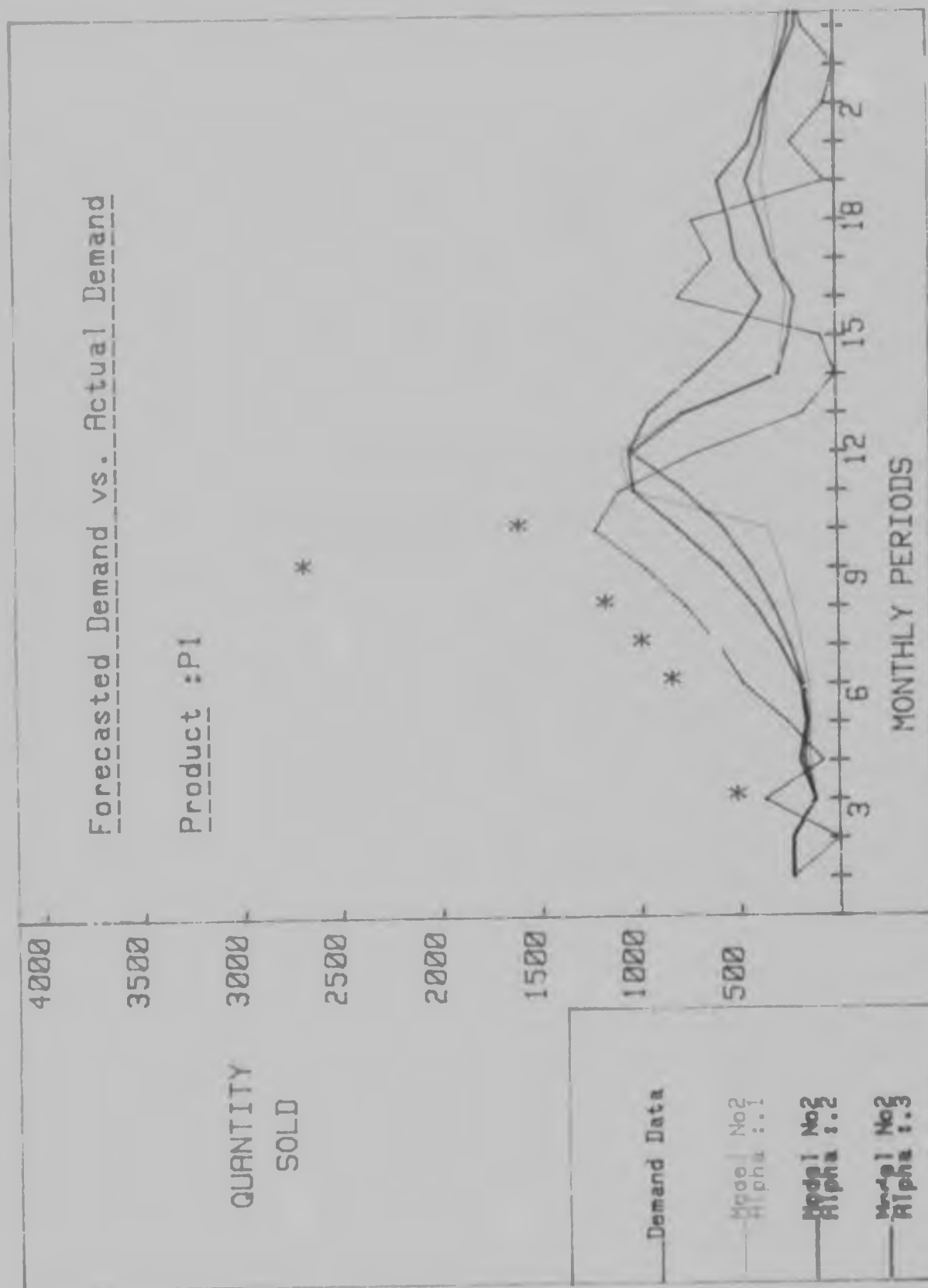


FIGURE 35

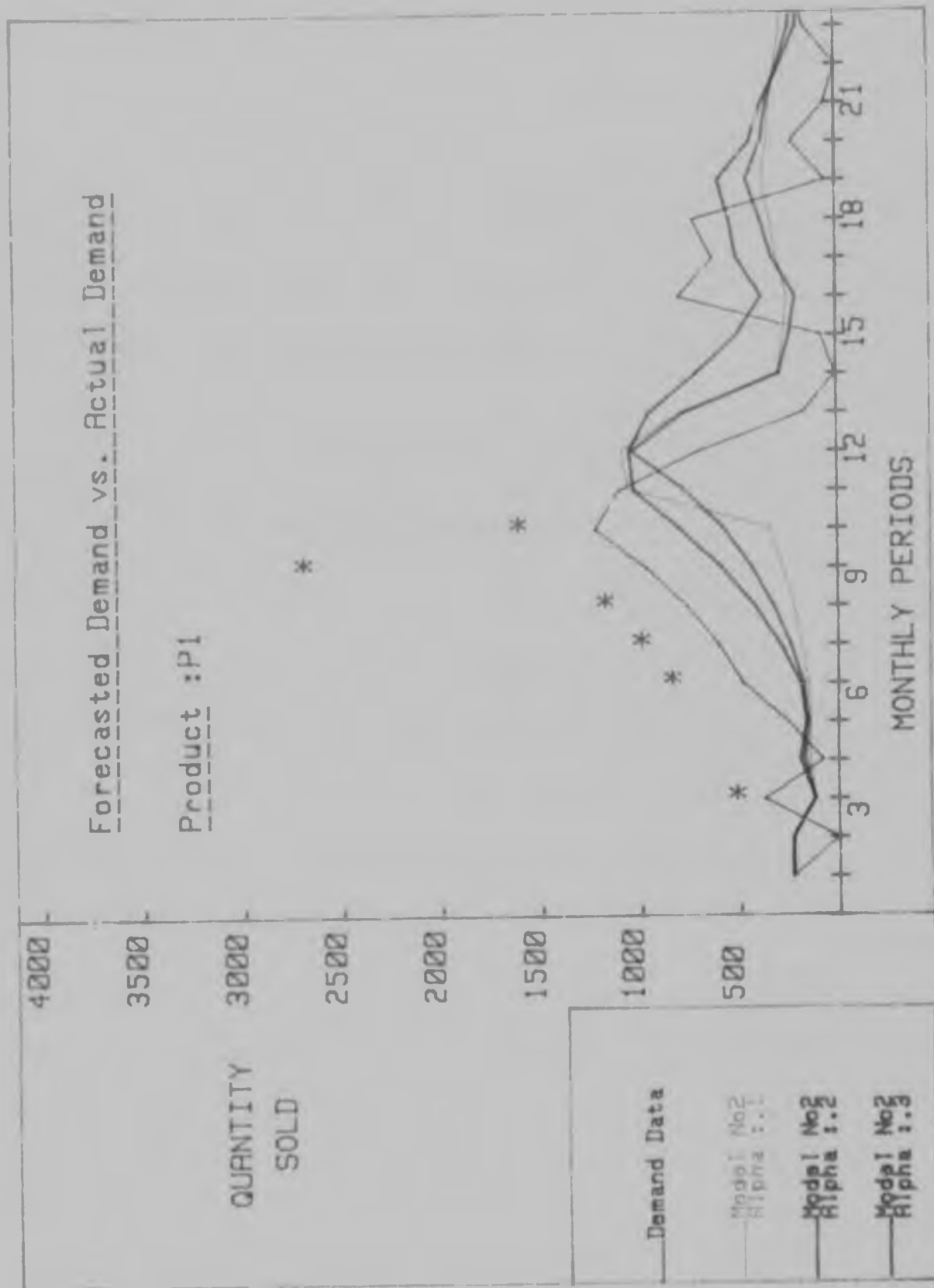


FIGURE 35

APPENDIX 8.2

FORECASTING RESULTS FOR P2

TABLE 18.1
FORECASTING RESULTS FOR Q2

Quarter	Alpha	Total Forecast Error	M.A.D.	Forecast Exceeds Total Demand	Tracking Signal at End of Run
1	0,2	-3487	333	-36,0	-
2*	0,2	-3494	330	-36,0	-0,69
3	-	-2621	304	-27,0	-0,65
4*	0,2 $P=2$	-1856	309	-19,0	-0,48
5	0,1	0	396	0	-0,74
6	0,2	-2827	297	-29,0	-0,69
7	0,1 $P=2$	-7741	330	-18,0	-0,47
8	0,2	-7003	292	-18,6	-0,46
9	0,2	-6007	287	-21,0	-0,57
10	0,2	-5003	369	-38,0	-0,71

* Forecast errors calculated from initial run for further testing.

(C) Forecast errors calculated by time series forecasting (using 100 runs from 10 error runs $1/10$ period).

Run 1 & 100 = 0,2 and 5 = 2 were selected as it best

reflects the actual trend of report data.

APPEL X 8.2

FOREIGN STI 1250 302 G10

TABLE 18.3
FORECASTING RESULTS USING MODEL 2 WITH ALPHA EQUAL TO 0.2

INITIAL VALUE OF SMOOTHING FACTOR .50
SMOOTHING FACTOR FOR ERROR & MAD .20
NO OF PERIODS BEFORE ERRORS ARE LINED .00
INITIAL VALUE WHICH FORECAST IS OUT OF CONTROL .00
TRAILING SIGNAL MUST NOT EXCEED .50
WITH THESE PERIODS, THE FACTORS ARE RESET
RESET VALUE OF ALPHA .20
RESET VALUE OF GAMMA .10

P2

PERIOD	FILTER DEMAND	ACTUAL DEMAND	NEW PERIOD	CUSUM	ERROR	SMOOTH	ALPHA	TRAILING
1	200	200	100	0	0	0.50	.50	0.00
2	0	0	100	0	200	0.60	.50	1.00
3	200	200	120	0	-100	0.40	.20	.00
4	110	110	110	10	10	0.50	.20	.00
5	70	70	80	0	40	0.60	.20	.00
6	300	300	200	-240	-240	0.40	.20	.00
7	0	0	220	30	220	0.60	.20	.00
8	20	20	100	240	200	0.40	.20	.00
9	150	150	170	270	20	0.50	.20	.00
10	0	0	140	450	140	0.60	.20	.00
11	0	0	110	560	110	0.40	.20	.00
12	0	0	0	0	0	0.50	.20	.00
13	0	0	0	0	0	0.60	.20	.00
14	100	100	100	-100	-100	0.40	.20	.00
15	400	400	210	-400	-400	0.60	.20	.00
16	370	370	240	-500	-130	0.40	.20	.00
17	0	0	300	-900	-900	0.60	.20	.00
18	0	0	400	-1300	-1300	0.40	.20	.00
19	0	0	400	-1700	-1700	0.60	.20	.00
20	200	200	420	-1400	-200	0.40	.20	.00
21	1200	1200	500	-2200	-800	0.60	.20	.00
22	1000	1000	500	-3100	-1100	0.40	.20	.00
23	1100	1100	0	-3400	-300	0.60	.20	.00

EVALUATION REPORT

NO OF FORECASTS HIGH 9.0
AMOUNT FORECASTED HIGH 1209.6
NO OF FORECASTS LOW 11.0
AMOUNT FORECASTED LOW -4063.5
M.A.D. AT END OF RUN 330.4

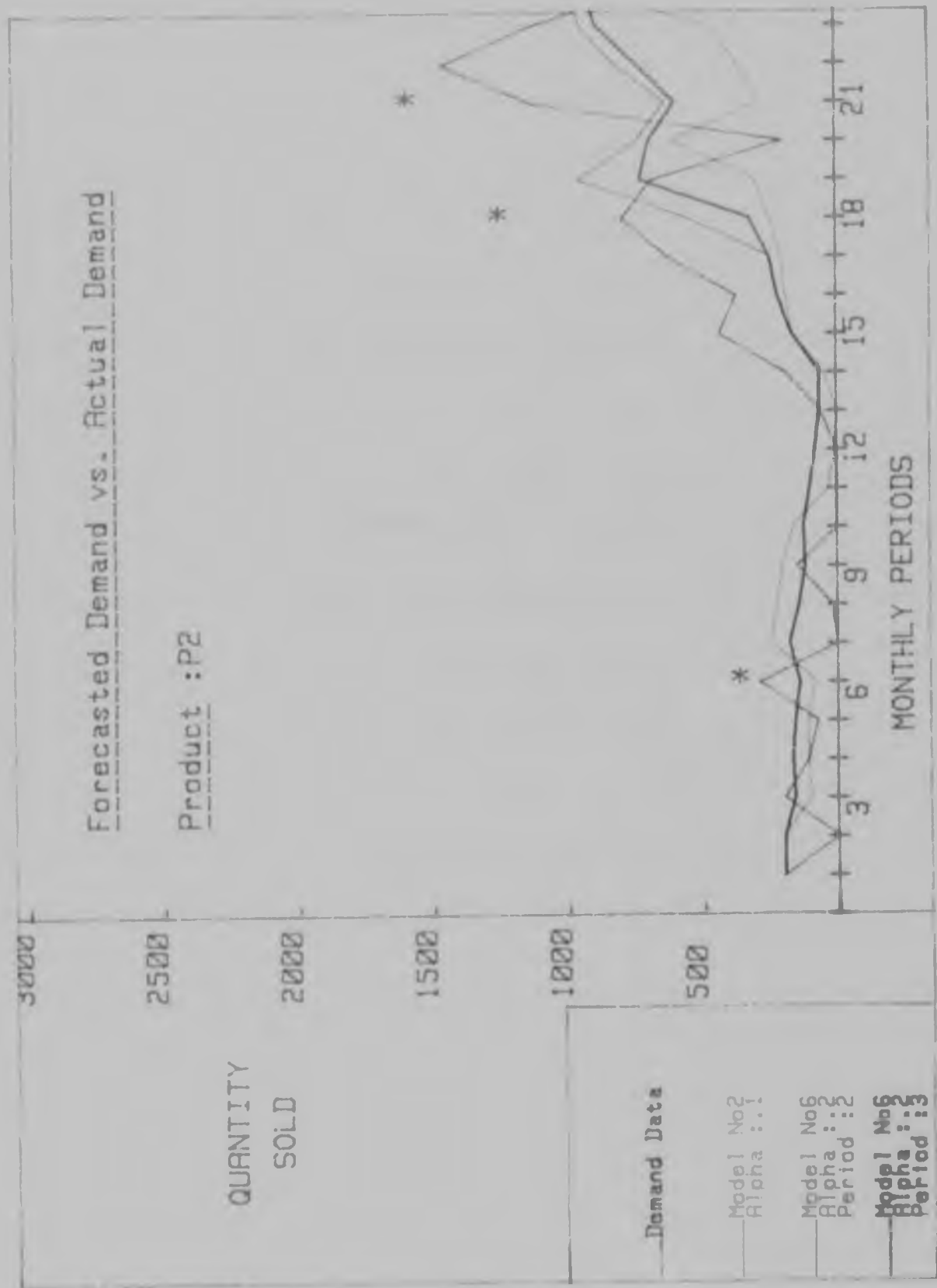


FIGURE 36

PI IX 8.

FOOTASTING I SUITS FOR P3

TABLE 19.1
FORECASTING RESULTS FOR P3

Models	Alpha	Total Forecast Error	M.A.D.	Forecast Exceeds Total	Tracking Signal At End of Run
1*	0,2	- 395	94	-	-
2*	0,2	405	94	5,6	0,18
5	-	- 43	91	-	0,19
6*	0,2 P=2	- 31	90	-	0,27
1	0,3	- 151	90	-2,0	-
2	0,1	407	92	5,6	0,26
2	0,2	462	91	6,4	0,2
6	0,1 P=2	- 79	91	-1,0	0,26
6	0,3 P=2	- 159	92	-2,2	0,19
6	0,2 P=3	- 132	90	-1,8	0,25
6	0,2 P=4	- 74	89	-1,0	0,21

* This implies models selected from initial run for further testing.

The mean absolute deviations of all the models are very similar.

Model 6, alpha = 0,2 and P = 2 was selected as it had the lowest total forecast error.

TABLE 19.2

FITTING RESULTS USING MODEL 2 WITH ALPHA EQUAL TO 0.2

INITIAL VALUE OF SMOOTHING FACTOR .50
 SMOOTHING IN EQUATION 4 AND .30
 SMOOTHING IN EQUATION 5 AND 2.5
 SMOOTHING IN EQUATION 6 AND .00
 SMOOTHING IN EQUATION 7 AND .50
 SMOOTHING IN EQUATION 8 AND .10
 SMOOTHING IN EQUATION 9 AND .10
 SMOOTHING IN EQUATION 10 AND .10
 SMOOTHING IN EQUATION 11 AND .10
 SMOOTHING IN EQUATION 12 AND .10
 SMOOTHING IN EQUATION 13 AND .10
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 SMOOTHING IN EQUATION 95 AND .10
 SMOOTHING IN EQUATION 96 AND .10
 SMOOTHING IN EQUATION 97 AND .10
 SMOOTHING IN EQUATION 98 AND .10
 SMOOTHING IN EQUATION 99 AND .10
 SMOOTHING IN EQUATION 100 AND .10

PERIOD	FILTER DEMAND	ACTUAL DEMAND	PERIOD FCST	PERIOD SUM	PERIOD DIFF	SMOOTH M.A.D.	ALPHA	BACK-GRADE
1	121	121	121	0	0	16.8	.50	1.00
2	219	219	121	0	-96	16.8	.50	1.00
3	242	242	231	0	-51	20.2	.20	-1.00
4	368	368	216	-76	-76	25.1	.20	-1.00
5	313	338	294	0	-97	32.9	.00	1.00
6	170	147	195	123	123	41.9	.20	-.41
7	187	187	193	131	0	38.5	.20	-.38
8	150	150	183	175	43	39.8	.20	-.23
9	184	184	185	176	1	35.2	.20	-.23
10	187	187	185	173	14	31.9	.20	-.23
11	303	332	289	54	-120	48.7	.20	-.45
12	219	219	211	44	-16	37.6	.20	-.47
13	314	314	232	-59	-103	44.2	.20	-.59
14	397	650	265	-225	-166	56.3	.20	-.71
15	445	445	359	0	-180	68.7	.00	-.79
16	346	346	359	0	63	60.1	.00	-.62
17	417	417	407	0	50	67.1	.00	-.66
18	302	0	387	0	23	62.0	.00	-.59
19	353	353	360	34	24	59.9	.20	-.51
20	484	484	385	-91	-124	66.3	.20	-.60
21	276	276	363	10	100	70.5	.20	-.35
22	216	216	333	165	147	70.2	.20	-.10
23	93	93	285	485	240	74.4	.20	.10

EVALUATION REPORT

NO OF FORECASTS HIGH 10.0
 AMOUNT FORECASTED HIGH 791.5
 NO OF FORECASTS LOW 10.0
 AMOUNT FORECASTED LOW -936.0
 M.A.D. AT END OF RUN 94.4

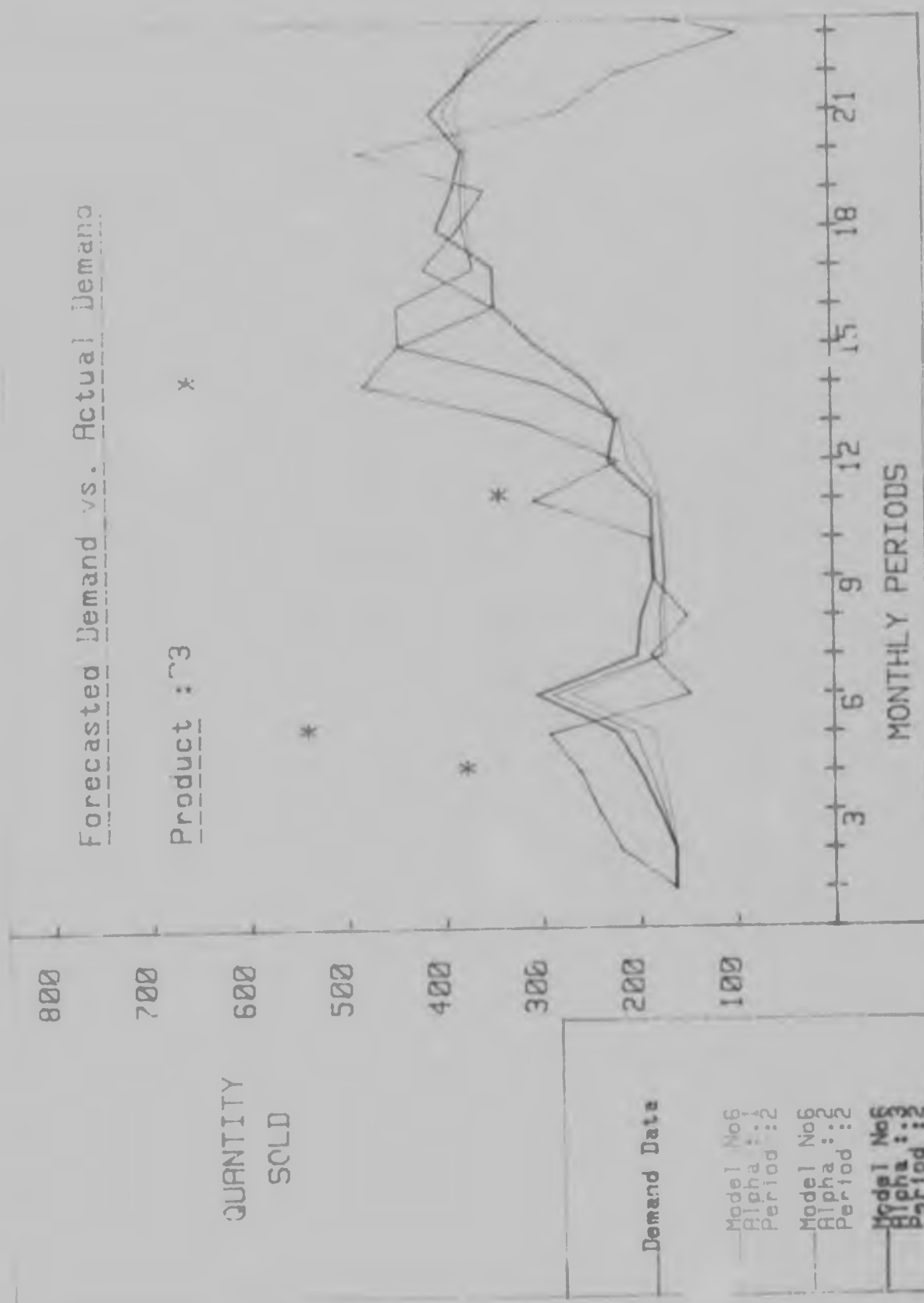


FIGURE 37

APPENDIX B.4

FORECASTING RESULTS FOR P4

TABLE 2D.1
 COMPARING RESULTS FOR 19

Model	Alpha	Total Forecast Errors	M.A.D.	Forecast Excesses Total Demand	Tracking Signal At End Of Run
1	0.2	-380	93	-5.7	*
2	0.2	10	98	-0.1	-0.02
3	-	-645	92	-6.9	0.78
4*	0.2 P=2	-458	85	6.8	-0.18
5	0.1	357	119	5.3	-0.2
6	0.3	76	100	1.1	0.0
7	0.1 P=2	-524	80	-3.3	0.23
8	0.3 P=2	-340	91	-5.7	-0.12
9	0.4 P=2	-290	98	-3.9	-
10	0.2 P=3	66	131	1.8	0.24
11	0.3 V=y	-20	130	0.4	0.24

* This implies model's selected from initial run for further testing.

Model 2 with alpha = 0.2 was selected as having the lowest total forecast error, mean absolute deviation and tracking signal.

TABLE 20.2
FORECASTING RESIDUAL UNIT MODEL 6 WITH ALPHA EQUAL TO 0.2

INITIAL VALUE OF SMOOTHING CONSTANT α 0.2
 SMOOTHING CONSTANT FOR ERROR β 0.1
 NO. OF PERIODS BEFORE SMOOTHING CONSTANT IS RESET 10
 RESET VALUE OF GAMMA γ 0.1
 ALPHA VALUE WHEN FORECAST IS OUT OF CONTROL 0.5
 LENGTH OF PERIOD BEFORE ALPHA IS RESET 10
 ALPHA IS RESET TO 0.2

P4

PERIOD	FILTER DEMAND	ACTUAL DEMAND	PERIOD FORECAST	ERROR	SMOOTHED M. V. $\hat{m}_t$	ALPHA	TRACK-SIGNAL
1	100	100	100	0	100	0.2	0.00
2	100	100	100	0	100	0.2	-1.00
3	100	100	100	0	100	0.2	-1.00
4	100	100	100	0	100	0.2	-1.00
5	100	100	100	0	100	0.2	-1.00
6	100	100	100	0	100	0.2	-1.00
7	100	100	100	0	100	0.2	-1.00
8	100	100	100	0	100	0.2	-1.00
9	100	100	100	0	100	0.2	-1.00
10	100	100	100	0	100	0.2	-1.00
11	100	100	100	0	100	0.2	-1.00
12	100	100	100	0	100	0.2	-1.00
13	100	100	100	0	100	0.2	-1.00
14	100	100	100	0	100	0.2	-1.00
15	100	100	100	0	100	0.2	-1.00
16	100	100	100	0	100	0.2	-1.00
17	100	100	100	0	100	0.2	-1.00
18	100	100	100	0	100	0.2	-1.00
19	100	100	100	0	100	0.2	-1.00
20	100	100	100	0	100	0.2	-1.00
21	100	100	100	0	100	0.2	-1.00
22	100	100	100	0	100	0.2	-1.00
23	100	100	100	0	100	0.2	-1.00
24	100	100	100	0	100	0.2	-1.00
25	100	100	100	0	100	0.2	-1.00
26	100	100	100	0	100	0.2	-1.00
27	100	100	100	0	100	0.2	-1.00
28	100	100	100	0	100	0.2	-1.00
29	100	100	100	0	100	0.2	-1.00
30	100	100	100	0	100	0.2	-1.00
31	100	100	100	0	100	0.2	-1.00
32	100	100	100	0	100	0.2	-1.00
33	100	100	100	0	100	0.2	-1.00
34	100	100	100	0	100	0.2	-1.00
35	100	100	100	0	100	0.2	-1.00
36	100	100	100	0	100	0.2	-1.00
37	100	100	100	0	100	0.2	-1.00
38	100	100	100	0	100	0.2	-1.00
39	100	100	100	0	100	0.2	-1.00
40	100	100	100	0	100	0.2	-1.00
41	100	100	100	0	100	0.2	-1.00
42	100	100	100	0	100	0.2	-1.00
43	100	100	100	0	100	0.2	-1.00
44	100	100	100	0	100	0.2	-1.00
45	100	100	100	0	100	0.2	-1.00
46	100	100	100	0	100	0.2	-1.00
47	100	100	100	0	100	0.2	-1.00
48	100	100	100	0	100	0.2	-1.00
49	100	100	100	0	100	0.2	-1.00
50	100	100	100	0	100	0.2	-1.00
51	100	100	100	0	100	0.2	-1.00
52	100	100	100	0	100	0.2	-1.00
53	100	100	100	0	100	0.2	-1.00
54	100	100	100	0	100	0.2	-1.00
55	100	100	100	0	100	0.2	-1.00
56	100	100	100	0	100	0.2	-1.00
57	100	100	100	0	100	0.2	-1.00
58	100	100	100	0	100	0.2	-1.00
59	100	100	100	0	100	0.2	-1.00
60	100	100	100	0	100	0.2	-1.00
61	100	100	100	0	100	0.2	-1.00
62	100	100	100	0	100	0.2	-1.00
63	100	100	100	0	100	0.2	-1.00
64	100	100	100	0	100	0.2	-1.00
65	100	100	100	0	100	0.2	-1.00
66	100	100	100	0	100	0.2	-1.00
67	100	100	100	0	100	0.2	-1.00
68	100	100	100	0	100	0.2	-1.00
69	100	100	100	0	100	0.2	-1.00
70	100	100	100	0	100	0.2	-1.00
71	100	100	100	0	100	0.2	-1.00
72	100	100	100	0	100	0.2	-1.00
73	100	100	100	0	100	0.2	-1.00
74	100	100	100	0	100	0.2	-1.00
75	100	100	100	0	100	0.2	-1.00
76	100	100	100	0	100	0.2	-1.00
77	100	100	100	0	100	0.2	-1.00
78	100	100	100	0	100	0.2	-1.00
79	100	100	100	0	100	0.2	-1.00
80	100	100	100	0	100	0.2	-1.00
81	100	100	100	0	100	0.2	-1.00
82	100	100	100	0	100	0.2	-1.00
83	100	100	100	0	100	0.2	-1.00
84	100	100	100	0	100	0.2	-1.00
85	100	100	100	0	100	0.2	-1.00
86	100	100	100	0	100	0.2	-1.00
87	100	100	100	0	100	0.2	-1.00
88	100	100	100	0	100	0.2	-1.00
89	100	100	100	0	100	0.2	-1.00
90	100	100	100	0	100	0.2	-1.00
91	100	100	100	0	100	0.2	-1.00
92	100	100	100	0	100	0.2	-1.00
93	100	100	100	0	100	0.2	-1.00
94	100	100	100	0	100	0.2	-1.00
95	100	100	100	0	100	0.2	-1.00
96	100	100	100	0	100	0.2	-1.00
97	100	100	100	0	100	0.2	-1.00
98	100	100	100	0	100	0.2	-1.00
99	100	100	100	0	100	0.2	-1.00
100	100	100	100	0	100	0.2	-1.00

EVALUATION RESULTS

M. OF FORECAST ERROR 9.0
 AMOUNT FORECAST ERROR 013.6
 M. OF FORECAST ERROR 11.0
 AMOUNT FORECAST ERROR 1141.2
 M.A.D. AT END OF PERIOD 85.5

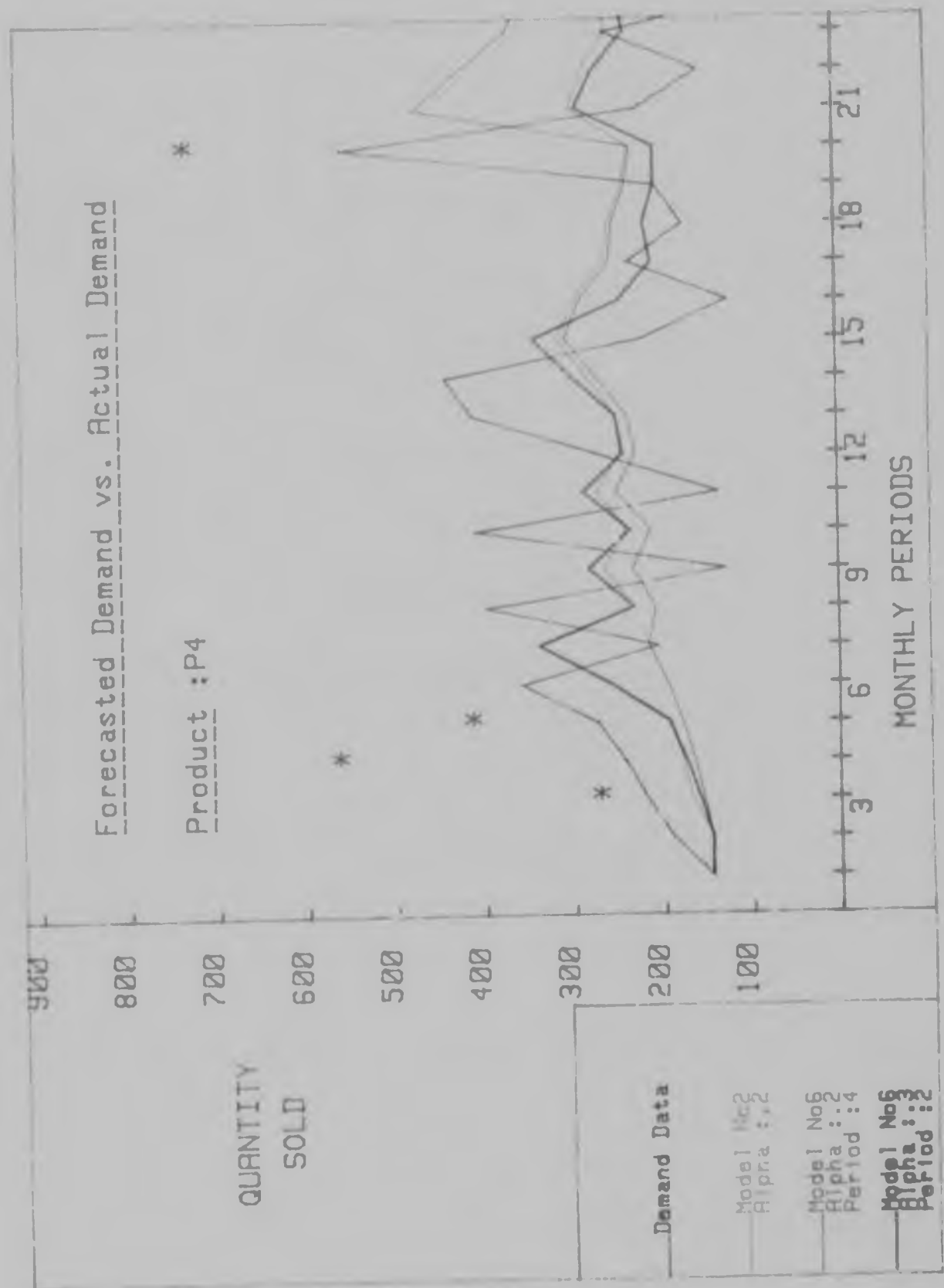


FIGURE 38

APPENDIX 8.5

FORECASTING RESULTS FOR P5

TABLE 21.1
FORECASTING RESULTS FOR P5

Models	Alpha	Total Forecast Error	M.A.D.	Forecast Exceeds Total Demand	Tracking Signal At End of Run
1	0,2	57	58	1,8	
2*	0,2	171	62	5,5	0,62
5	-	590	58	0,19	0,5
6*	0,2	861	62	21,8	0,57
2	0,1	211	69	6,8	0,54
2	0,3	418	55	13,5	0,54
5	0,1 P=2	1136	67	36,0	0,66
5	0,3 P=2	714	55	23,0	0,6
6	0,3 P=3	861	62	35,0	0,71
6	0,2 P=4	1257	72	40,0	0,74

* This implies models selected from initial run for further testing.

Model 5 was selected having a low total forecast error and mean absolute deviation.

TABLE 21.1
FORECASTING RESULTS FOR 195

Model	Alpha	Total Forecast Error	M.A.D.	% Error of Exceeds Total Demand	Tracking Signal At End of Run
1	0.2	57	58	1.8	
2*	0.2	171	62	8.0	0.68
3	-	560	58	0.19	8.5
6*	0.2	861	63	22.8	0.57
7	0.1	211	69	0.0	0.28
2	0.3	418	55	12.5	0.54
8	0.1 P=2	1136	67	36.0	0.00
8	0.3 P=2	713	59	22.0	0.0
6	0.3 P=3	861	62	32.0	0.11
6	0.2 P=4	1257	72	60.0	0.74

* This implies models selected from initial run for further testing.

Model 5 was selected having a low total forecast error and mean absolute deviation.

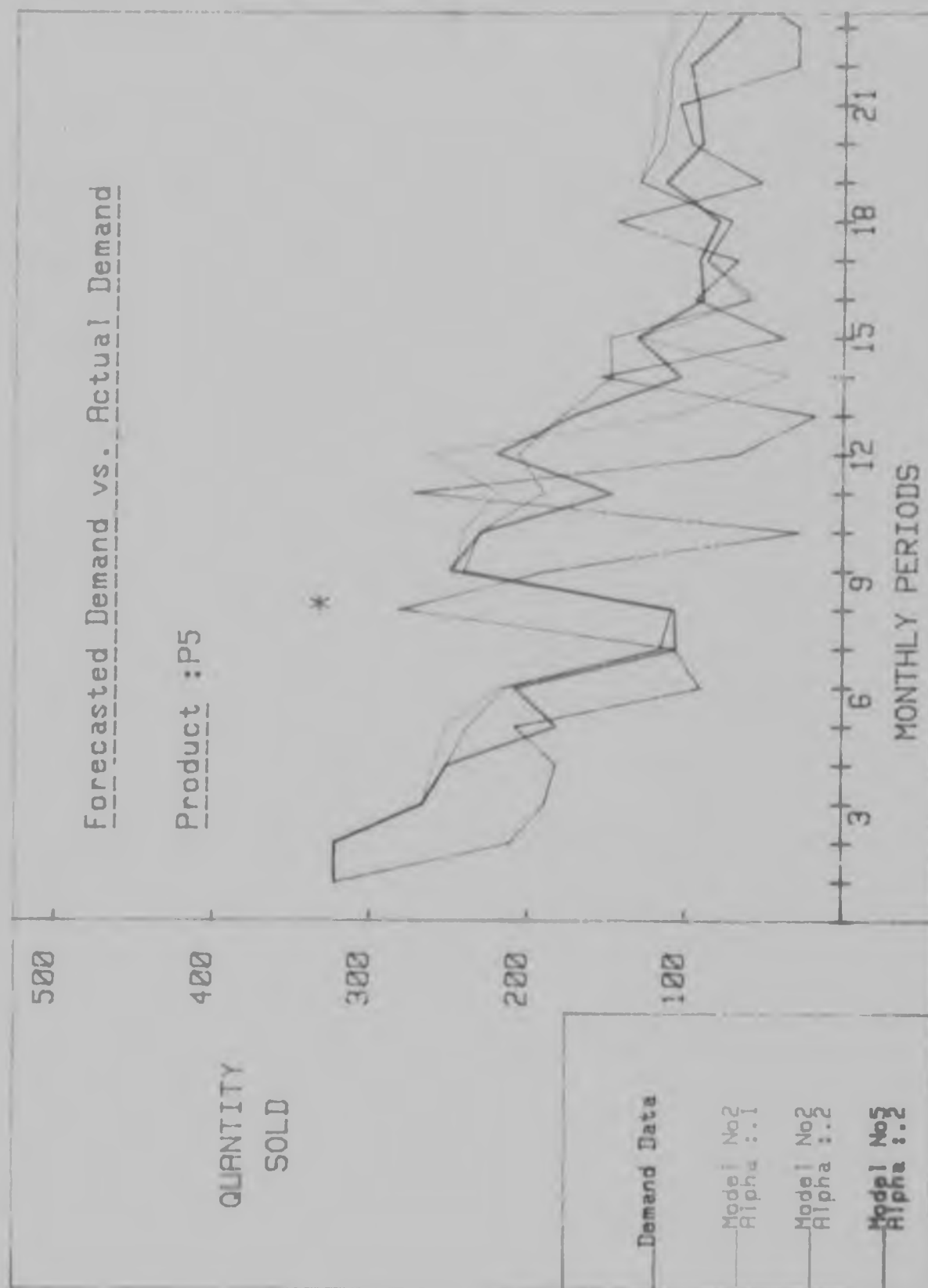


FIGURE 39

APPENDIX B.6
FORECASTING RESULTS FOR P6

TABLE 22.1
FORECASTING RESULTS FOR P6

Iteration	Alpha	Total Forecast Error	M.A.D.	Forecast Error (Total Demand)	Tracking Signal at End of Run
1	0.7	3	21	0.7	
2	0.7	19	21	1.7	0.01
3	-	-8	22	-0.7	0.06
4	0.7	-25	23	2.8	0.07
5	0.1	-41	21	3.8	0.00
6	0.3	6	22	0.3	0.01
7	0.7	-18	22	1.7	-0.01
8	0.3	-3	19	0.77	-0.01
9	0.7	-14	21	1.3	-0.00
10	0.3	-15	21	1.3	-0.07

MAE Alpha = 0.1 selected from initial run for tracking study.

Run 5 with Alpha = 0.1 and P = 2 was selected by viewing the results and analyzing deviation and one of the forecast errors.

TABLE 22.3
 FORECASTING RESULTS USING MODEL 1.2 WITH ALPHA $E_1, |A|$ TO 0.2

INITIAL VALUE OF SMOOTHING FACTOR .50
 SMOOTHING FACTOR FOR ERROR & TREND .50
 NO OF PERIODS BEFORE ERROR AND TREND .50
 ALPHA VALUE WHEN FORECAST IS OUT OF CONTROL .50
 TRACKING SIGNAL MUST NOT EXCEED .50
 AFTER THESE PERIODS, THE FACTORS ARE RESET:
 RESET VALUE OF ALPHA .40
 RESET VALUE OF GAMMA .10

P6

PERIOD	FILTER DEMAND	ACTUAL DEMAND	NEXT PERIOD FORECAST	CUSUM	CRASH	SMOOTH M.A.E.	ALPHA	TRACK-SIGNAL
1	44	44	44	0	0	0.5	.50	0.00
2	44	44	44	0	0	0.5	.50	0.00
3	44	44	44	0	0	0.5	.50	0.00
4	44	44	44	0	0	0.5	.50	0.00
5	44	44	44	0	0	0.5	.50	0.00
6	44	44	44	0	0	0.5	.50	0.00
7	44	44	44	0	0	0.5	.50	0.00
8	44	44	44	0	0	0.5	.50	0.00
9	44	44	44	0	0	0.5	.50	0.00
10	44	44	44	0	0	0.5	.50	0.00
11	44	44	44	0	0	0.5	.50	0.00
12	44	44	44	0	0	0.5	.50	0.00
13	44	44	44	0	0	0.5	.50	0.00
14	44	44	44	0	0	0.5	.50	0.00
15	44	44	44	0	0	0.5	.50	0.00
16	44	44	44	0	0	0.5	.50	0.00
17	44	44	44	0	0	0.5	.50	0.00
18	44	44	44	0	0	0.5	.50	0.00
19	44	44	44	0	0	0.5	.50	0.00
20	44	44	44	0	0	0.5	.50	0.00
21	44	44	44	0	0	0.5	.50	0.00
22	44	44	44	0	0	0.5	.50	0.00
23	44	44	44	0	0	0.5	.50	0.00

EVALUATION RESULTS

NO OF FORECASTS HIGH 12.0
 AMOUNT FORECASTED HIGH 217.1
 NO OF FORECASTS LOW 6.0
 AMOUNT FORECASTED LOW -287.0
 M.A.E. AT END OF RUN 10.4

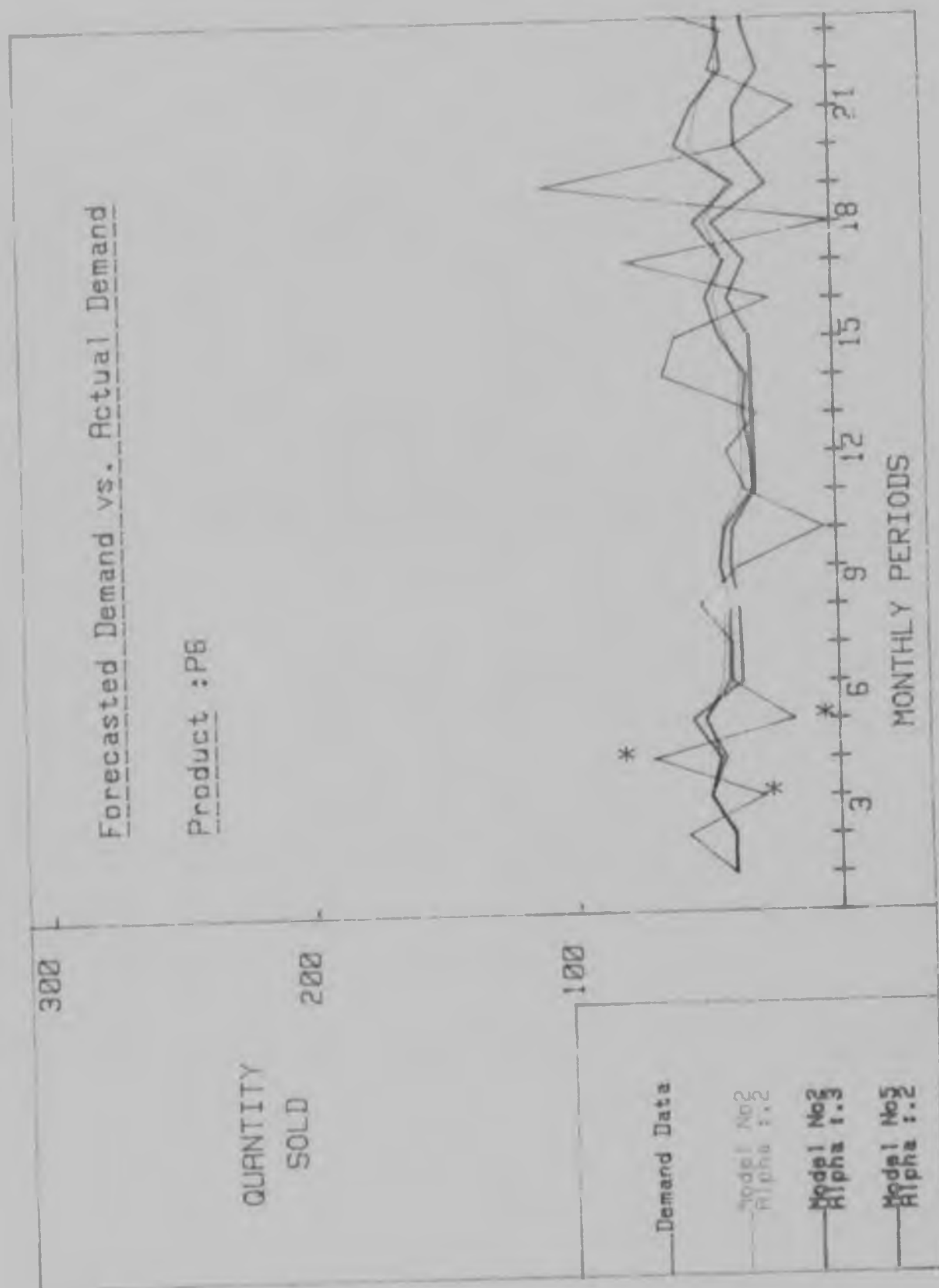


FIGURE 40

APPENDIX 8.7

FORECASTING RESULTS FOR GERMANY

TABLE 23.1
 FORECASTING RESULTS FOR GRAND TOTAL SALES

Models	Alpha	Total Forecast Error	M.A.D.	Forecast Exceeds Total Demand	Tracking Signal At End of Run
1	0,1	7265	369	8,6	
2*	0,2	61	440	0,07	-0,55
5		-4038	376	-4,8	0,29
6*	0,2	-7119	384	8,5	-0,74
2	0,1	532	398	0,6	-0,27
2	0,3	357	366	0,4	-0,56
6	0,1 P 2	-4921	488	5,5	-0,21
6	0,3 P-2	-4981	367	6,8	-0,58
6	0,2 P 3	-4984	366	5,0	-0,48
6	0,2 P 4	-4971	367	5,3	-0,5

* This implies models selected from initial run for further testing.

Model 2 with alpha 0,1; 0,2 and 0,3 give the lowest forecast error. With alpha 0,2, the smoothest forecast is obtained.

TABLE 23.2
FORECASTING RESULTS USING MODEL 2 WITH ALPHA EQUAL TO 0.2

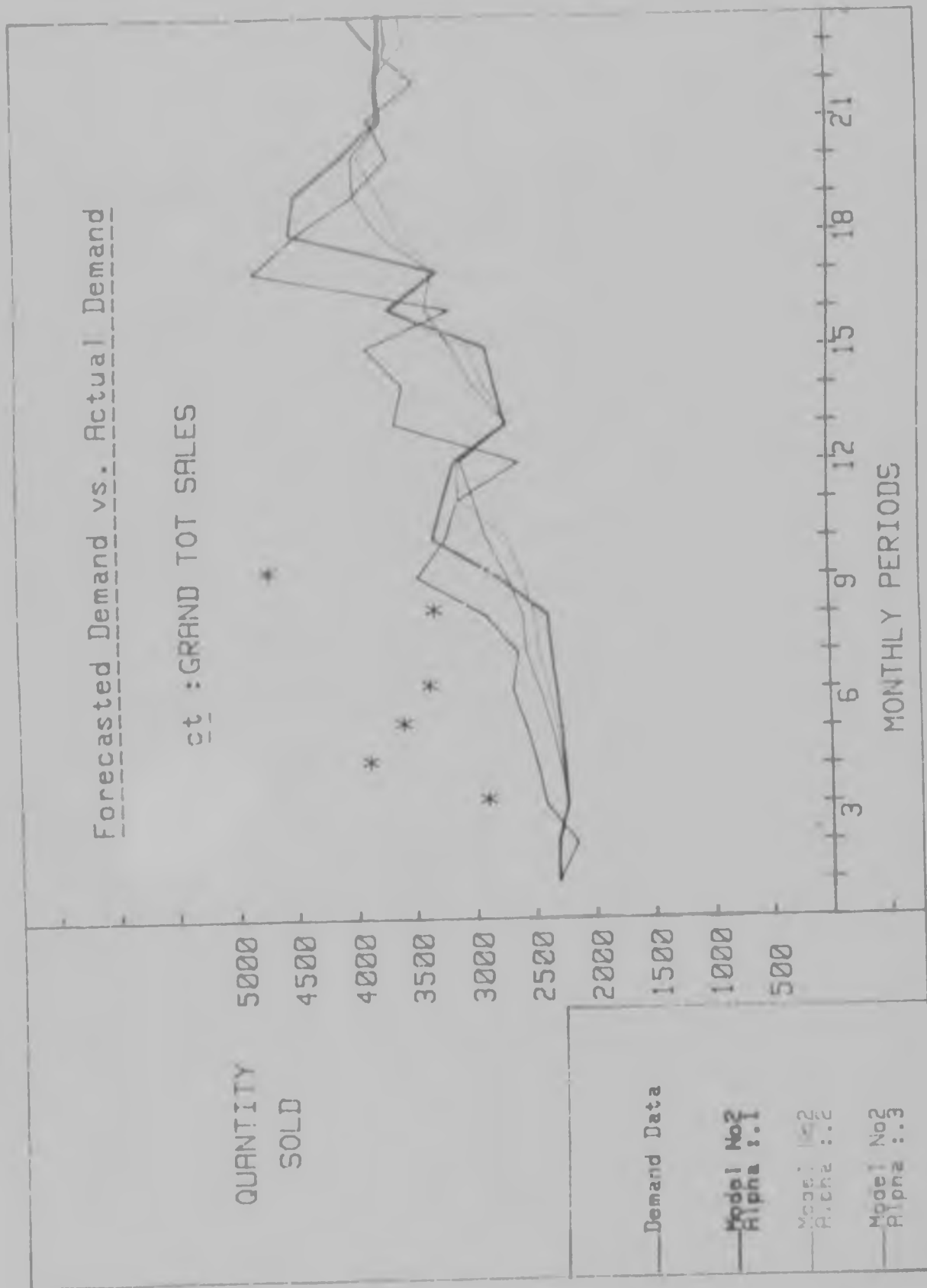
INITIAL VALUE OF SMOOTHING FACTOR .50
SMOOTHING FACTOR FOR ERROR & MRS .50
NO. OF PERIODS BEFORE ERROR ARE SMOOTHED .50
ALPHA VALUE WHEN FORECAST IS OUT OF CONTROL .50
TRACKING SIGNAL MUST NOT EXCEED .50
AFTER THESE PERIODS, THE FACTORS ARE RESET:
RESET VALUE OF ALPHA .20
RESET VALUE OF GAMMA .10

GRAND TOT SALES

PERIOD	FILTER DEMAND	ACTUAL DEMAND	NEXT PERIOD FORECAST	LOW	ERROR	SMOOTH M.R.D.	ALPHA	TRACK-SIGNAL
1	2140	2140	2140	0	0	0	.50	0.00
2	2140	2140	2140	0	0	0	.50	1.49
3	2140	2140	2140	0	0	0	.50	1.41
4	2140	2140	2140	0	0	0	.50	1.41
5	2140	2140	2140	0	0	0	.50	1.41
6	2140	2140	2140	0	0	0	.50	1.41
7	2140	2140	2140	0	0	0	.50	1.41
8	2140	2140	2140	0	0	0	.50	1.41
9	2140	2140	2140	0	0	0	.50	1.41
10	2140	2140	2140	0	0	0	.50	1.41
11	2140	2140	2140	0	0	0	.50	1.41
12	2140	2140	2140	0	0	0	.50	1.41
13	2140	2140	2140	0	0	0	.50	1.41
14	2140	2140	2140	0	0	0	.50	1.41
15	2140	2140	2140	0	0	0	.50	1.41
16	2140	2140	2140	0	0	0	.50	1.41
17	2140	2140	2140	0	0	0	.50	1.41
18	2140	2140	2140	0	0	0	.50	1.41
19	2140	2140	2140	0	0	0	.50	1.41
20	2140	2140	2140	0	0	0	.50	1.41
21	2140	2140	2140	0	0	0	.50	1.41
22	2140	2140	2140	0	0	0	.50	1.41
23	2140	2140	2140	0	0	0	.50	1.41
24	2140	2140	2140	0	0	0	.50	1.41
25	2140	2140	2140	0	0	0	.50	1.41
26	2140	2140	2140	0	0	0	.50	1.41
27	2140	2140	2140	0	0	0	.50	1.41

EVALUATION RESULTS

NO. OF FORECASTS HIGH 4.0
AMOUNT FORECASTED HIGH 1040.2
NO. OF FORECASTS LOW 10
AMOUNT FORECASTED LOW -8215.0
M.R.D. AT END OF RUN 440.3



(Figure 4)

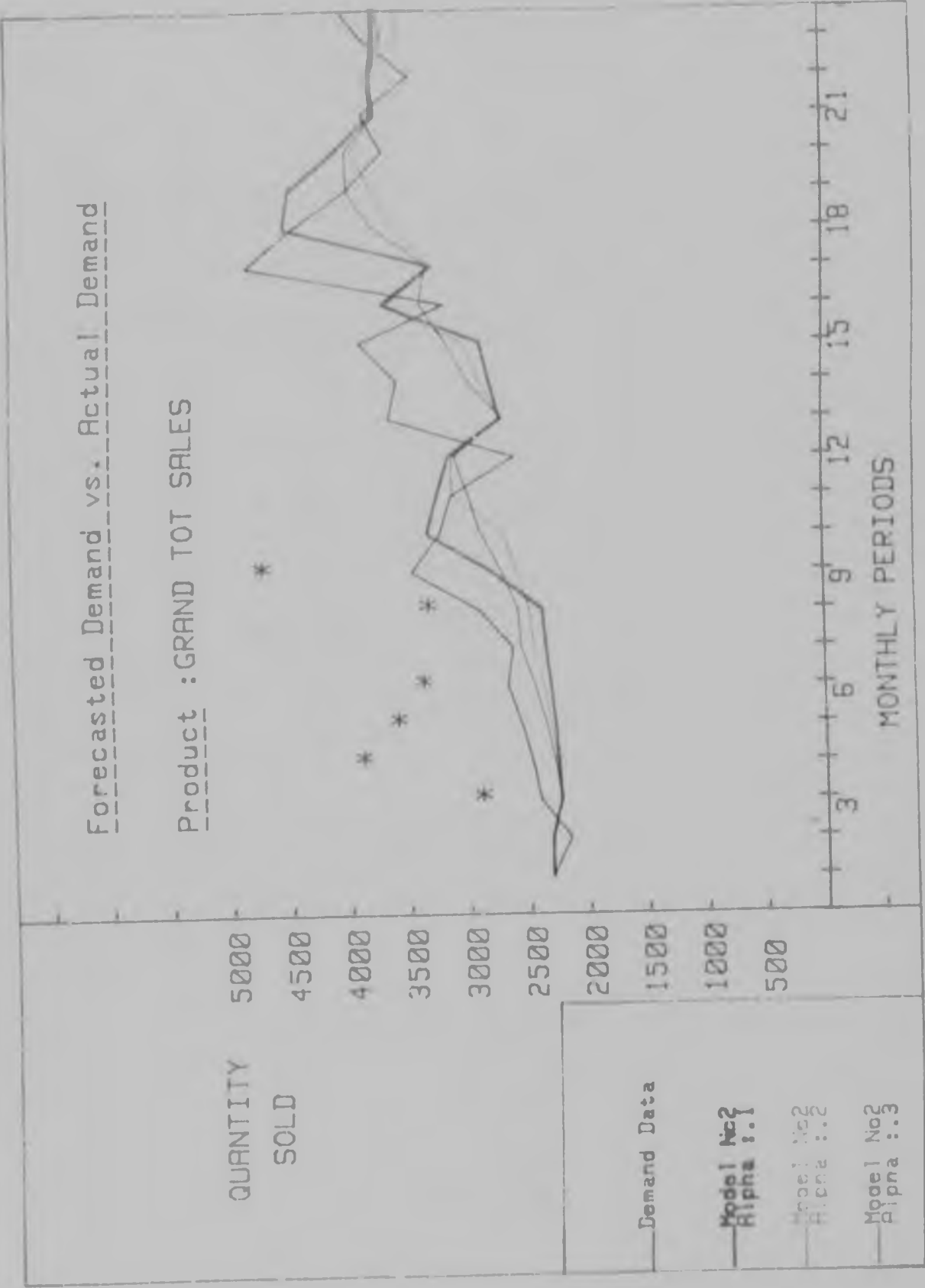


Figure 4.1

APPENDIX B.8

RESULTS FOR A SAMPLE 'B' ITEM

TABLE 24
 FORECASTING RESULTS FOR P5

Models	Alpha	Total Forecast Error	I.A.D.	Forecast Exceeds Demand	Tracking Signal at End of Run
1	0,2	-65	8,0	-22,0	-
2	0,1	-25	8,2	- 8,5	0
2	0,2	-27	8,8	- 9,2	-0,03
2	0,3	-38	9,9	-12,9	-0,05
5	-	-22	8,6	-7,5	0,04
6	0,2	-34	8,7	-11,6	-0,07
	P=2				

APPENDIX

EXPERIMENTAL PROCEDURE AND RESULTS

APPENDIX E.1

INTERIOR SIMULATION

RECALCULATION ORDER POINTS EVERY THREE MONTHS BASED ON
SIX MONTHS MOVING AVERAGE

Notes on the simulation exercise.

1. Lead times. A constant lead time of eight weeks is assumed for each order.
2. Order quantity. The order quantity is equal to the sales average (or forecast) level, rounded to the nearest fifty units, ie the order quantity in period two equals the rounded sales average (or forecast) calculated in period one.
3. Multiples of the order quantity are ordered every time the stock on hand plus on order drops below the order point. Sufficient order quantities are ordered so that stock on hand plus on order exceed the order point.
4. Order point. The order point is calculated as described in section 4.6.
Safety stock is based on a 90% service level.

TABLE 25.1
 PERIODIC REVIEW, INVENTORY SIMULATION FOR P1
 'A' ITEM

MONTH	FORECAST	MAD	DDLT	SS	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	821	544	1642	1419	3060			1800	1203	
May						1203		800	1122	81
June						1121	1800	800	2124	798
July	398	311			1607	2124	800	-	2300	624
August						2300	800	-	3174	726
September						3174	-	-	3121	53
October	418	298			1611	3121			2896	225
November						2896	-	-	2841	55
December						2841			2841	0
Jan 1981	202	181			878	2841			2575	161

TABLE 25.2
 PERIODIC REVIEW, INVENTORY SIMULATION FOR P2

MONTH	FORECAST	MAD	DDLT	SS	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	95	85			411			-	734	
May						743		100	311	432
June						311		400	(60)	371
July		196			1071	(60)	100	600	(585)	819
August						(585)	400	1800	(1400)	1215
September						(1400)	600	800	(1484)	881
October					1838	(1484)	1800	300	116	1900
November						116	800	1500	(637)	1553
December						(637)	300	2000	(1794)	1451
Jan 1981	1041				3122	(1794)	1500		(1430)	1136

TABLE 25.3
 PERIODIC REVIEW, INVENTORY SIMULATION FOR P3
 'A' ITEM

MONTH	FORECAST	MAD	DDLT	SS	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	293	122	600					300	891	445
May						891		300	4	445
June						446	600	300	400	346
July	399	106				400	600	600	283	417
August						283	600	400	201	382
September						201	600	400	448	353
October	405	44				448	600	400	364	484
November						364	400	400	493	271
December						493	400		677	216
Jan 1981	301	101			878	677	400		984	93

TABLE 25.4
 PERIODIC REVIEW, INVENTORY SIMULATION FOR P4
 'A' ITEM

MONTH	FORECAST	MAD	DDLT	SS	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	331	109	600	194	704				1091	
May						1091		300	871	220
June						871			740	122
July	283				814	740	300	300	815	234
August						815			643	172
September						643	300	300	740	203
October	279	147			847	740		600	20	720
November						20	300		91	231
December						91	600	600	241	197
Jan 1981	288	144			951	241		300	281	258

TABLE 25.6
PERIODIC REVIEW, INVENTORY SIMULATION FOR P5
'A' ITEM

Month	Forecast	RAO	DEL	LS	OP	OPENING STOCK	CURRENT STOCK	QTY. ORDERED	TRANSIT STOCK	SALES
1st April	151	70	100	100	500			150	400	
Feb						400			470	50
Mar						470	100	100	470	50
July	70	30			230	470			470	50
August						410	110		430	100
September						510			500	50
October	80	20			200	500			500	50
November						560		80	560	100
December						100		100	100	50
Jan 1991	70	30			200	100	100	100	100	50

TABLE 25.6
PERIODIC REVIEW, INVENTORY SIMULATION FOR P5
'A' ITEM

Month	Forecast	RAO	DEL	LS	OP	OPENING STOCK	CURRENT STOCK	QTY. ORDERED	TRANSIT STOCK	SALES
1st April	30	0	70	10	110			100	80	
Feb						80			90	10
Mar						70	100	100	140	10
July	20	10	100	10	110	140			90	10
August						80		50	60	0
September						80	100	100	140	100
October	30	0	100	10	100	140	100	100	170	10
November						170	100	100	170	10
December						110	50		110	10
Jan 1991	30	0	80	10	140	110	100	100	140	10

APPENDIX 9.2

INVENTORY SIMULATION

RECALCULATING THE ORDER POINT EVERY MONTH BASED ON
EXPONENTIAL SMOOTHING WITH BEST MODEL

TABLE 26.1
 CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P1
 MODEL 2 $\alpha = 0,1$

MONTH	FORECAST	MAD	DDL1	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	264	313	528	1344		250	1203	
May	246	300	492	1274	1203		1122	81
June	301	325	602	1449	1122	250	574	798
July	373	325	666	1513	574	600	(50)	624
August	372	332	744	1463	(50)	900	124	726
September	341	330	682	1542	124	600	671	53
October	329	390	656	1463	671	800	1246	225
November	302	305	60	1246	1541		1541	55
December	271	305	542	1541			1541	0
Jan 1981	260	300	520	1541			1380	161

TABLE 26.2
 CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P2
 MODEL 6 $\alpha = 0,7 = P = 2$

MONTH	FORECAST	MAD	DDL1	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	165	33	33	549			743	
May	218	107	436	702	400		311	432
June	249	107	498	777	311	500	(60)	371
July	550	134	1100	1449	(60)	400	(285)	625
August	952	170	1904	1449	(285)	500	(1000)	1215
September	738	180	1476	1449	(1000)	750	(934)	684
October	630	216	1800	1449	(934)	1650	516	200
November	815	286	1670	2375	516	1900	863	1553
December	943	322	1886	2200	863	1600	(594)	1457
Jan 1981	982	300	1964	1800	(594)	1300	(430)	1100

TABLE 26.3
 CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P3
 MODEL 6 $\alpha = 0,2$; $P = 2$

MONTH	FORECAST	MAD	DDL1	SS	OP	OPENING STOCK	QUANTITY RECEIVED	QTY	CLOSING STOCK	SALES
End April	442	63	884	164	1048			450	891	
May	444	57	888	148	1036	891			446	445
June	366	61	672	219	891	446			550	346
July	376	60	752	156	908	550			583	417
August	377	55	754	143	897	583			201	382
September	372	52	744	135	879	201			198	353
October	395	58	790	151	941	198			114	484
November	371	64	742	166	908	114			243	271
December	340	73	680	190	870	243	700	350	727	216
Jan 1981	291	90	582	234	816	727		-	634	93

TABLE 26.4
 CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P4
 MODEL 2 $\alpha = 0,2$

MONTH	FORECAST	MAD	DDL1	SS	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	314	92	628	240	868			-	1091	-
May	295	92	590	240	830	1091		300	871	220
June	260	100	520	261	781	871		300	749	122
July	255	93	510	243	753	749	300		815	234
August	238	92	476	240	716	815	300		943	172
September	231	86	462	224	686	943			740	203
October	296	110	592	287	879	740		750	20	720
November	281	106	562	276	838	20		300	(203)	223
December	256	109	512	284	796	(203)	750	300	395	152
Jan 1981	256	98	512	254	766	395	300	0	437	258

TABLE 26.5
 CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P5
 MODEL 5

MONTH	DEMAND	MR	MRX	IP	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
June (1)	100	100	262	224	486			150	450	
July	80	87	178	227	580	460		150	422	38
August	100	100	184	300	390	422	150		478	94
September	100	100	180	190	350	478	150		560	68
October	100	100	175	189	414	560			416	144
November	80	71	175	185	365	416		100	363	53
December	93	100	186	190	356	363			266	97
January	100	100	196	154	350	266	100	100	261	105
February	100	100	180	180	300	261		100	231	80
March	100	100	180	180	257	231	100		301	30

TABLE 26.6
 CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P6
 MODEL 2 $\alpha = 0.2$

MONTH	DEMAND	MR	MRX	IP	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
June (1)	80	100			113			50	87	
July	100	13			124	87		50	71	16
August	100	100			119	71	50		90	24
September	100	100			138	97	50	100	69	100
October	100	100			126	69			69	70
November	100	100			171	69	100	100	59	110
December	100	24			161	59			23	80
January	100	100			140	23	100	50	110	13
February	100	100			146	110		50	65	45
March	100	21			139	65	50	50	75	40

APPENDIX 9.3

INVENTORY SIMULATION
RECALCULATING THE ORDER POINT MONTHLY
BASED ON EXPONENTIAL SMOOTHING WITH MODEL 2

TABLE 27.1
CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P1

MODEL 2 $\alpha = 0,2$

MONTH	FORECAST	MAD	DDLT	SALES	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	234	137					250	1203	
May	203	318			(203)			1122	81
June	322	346					800	574	798
July	381	342		1658	574		900	(50)	624
August	451	342					800	24	726
September	372	347			24		450	871	53
October	342	327			871			1446	225
November	285	323			1446			1896	55
December	225							1896	0
Jan 1981	214				1896			1735	161

TABLE 27.2
CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P2

MODEL 2 $\alpha = 0,2$

MONTH	FORECAST	MAD	DDLT	SALES	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April	163	107						743	
May	217	123					300	311	432
June	248	127					600	(60)	371
July	323	152			(60)		750	(385)	625
August	437	193					1500	(1000)	1215
September	486	199		1491	(1000)		900	(934)	684
October	429	207			(934)	1500	500	366	200
November	585	264			366	900	1350	(287)	1553
December	759	325		2166	(287)	500	1800	(1244)	1457
Jan 1981	834	330		2529	(1244)	1350	2250	(1030)	1136

TABLE 27.3

EXAMPLE 1: REORDER POINT, INVENTORY SIMULATION FOR P4

TABLE 27.3: P4: P4: P4

DATE	REORDER POINT	QTY ORDERED	QTY RECEIVED	QTY ORDERED	CLOSING STOCK	SALE
10/1	100	0	0	0	445	445
10/2	100	0	0	0	100	346
10/3	100	0	0	350	67	417
10/4	100	0	0	400	351	381
10/5	100	0	0	400	348	391
10/6	100	0	0	350	264	484
10/7	100	0	0	400	393	271
10/8	100	0	0	350	529	216
10/9	100	0	0	350	834	93

TABLE 27.4

EXAMPLE 2: REORDER POINT, INVENTORY SIMULATION FOR P4

TABLE 27.4: P4: P4: P4

DATE	REORDER POINT	QTY ORDERED	QTY RECEIVED	QTY ORDERED	CLOSING STOCK	SALE
10/1	100	0	0	150	460	460
10/2	100	0	0	150	422	422
10/3	100	0	0	150	478	478
10/4	100	0	0	150	410	410
10/5	100	0	0	100	310	310
10/6	100	0	0	150	213	213
10/7	100	0	0	100	216	216
10/8	100	0	0	100	261	261
10/9	100	0	0	100	331	331

APPENDIX 1.4

INVENTORY SIMILARITIES
RELATING THE UNDER POINT SOURCE
FOR A "B" SITE

TABLE 28.1
CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P5
USING MODEL 5 AND ORDER QUANTITY 50 UNITS

MONTH	FORECAST	MAO	DDLT	SS	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April		2,8			21,3				
May	14	2,8			37,0	39		21	19
June	23	2,8			57,0	21		(5)	26
July	32	2,1			77,0	(5)	50	(39)	34
August	31	4,7			74,0	(39)	50	50	
September	17	2,8			49,0	60		30	
October	23	2,6			66,0	40	50	63	17
November		2,1			63,0	83	50	43	
December	16	2,8			52,0	63		55	
Jan 1981	13	8,6			48,0	35		85	

TABLE 28.2
CONTINUOUS REVIEW, INVENTORY SIMULATION FOR P6
USING MODEL 5 WITH ORDER QUANTITY = NEAREST 10 UNITS TO FORECAST

MONTH	FORECAST	MA	DDLT	SS	OP	OPENING STOCK	QUANTITY RECEIVED	QTY ORDERED	CLOSING STOCK	SALES
End April					21				39	
May	14				37				21	19
June	23				57	21		50	(5)	26
July	32				77	(5)		60	(39)	34
August	31				74	(39)	50	60		
September	17				49	(100)	60		40	
October	23				66	40	60		83	17
November					63	83			63	
December	16				52	63			55	
Jan 1981					48					



Author Jagoe M

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