## <u>APPENDIX D</u> MAGNETIC SALIENCY AND THE GENERATOR TRANSIET VOLTAGE

This appendix shows magnetic saliency affects the value the transient generator voltage has.

## D.1 $|E'_{KBG}|$ WHEN MAGNETIC SALIENCY IS CONSIDERED

The steady state operating point of the Koeberg generator of the improved two generator model shown in Chapter 3, figure 3.25 is P = 450 MW, Q = 13.6 MVAR and  $|V_{KBG LV}| = 1.005$  per unit.

The q-axis synchronous reactance of the Koeberg machine, expressed on a 1072 MVA base, is  $x_q = 2.28$  per unit.

The angle,  $\delta$ , between the generator q-axis and the terminal voltage can be computed using (Appendix F, equation F.7):

$$\delta = \tan^{-1} \left( \frac{x_q P}{V^2 + x_q Q} \right) \tag{D.1}$$

 $\delta$  obtained for the Koeberg generator is:

$$\delta = \tan^{-1} \left( \frac{x_q P}{V^2 + x_q Q} \right)$$
  
=  $\tan^{-1} \left[ \frac{2.28 * \left( \frac{450}{1072} \right)}{(1.005)^2 + 2.28 * \left( \frac{13.6}{1072} \right)} \right]$   
= 42.65° (D.2)

The d- and q-axis components of the terminal voltage, V, at Koeberg can be computed by using equation F.8.  $V_d$  and  $V_q$  are:

$$V_{d} = V \sin(\delta)$$
  
= 1.005 sin(42.65°)  
= 0.6809 (D.3-a)  
$$V_{q} = V \cos(\delta)$$
  
= 1.005 cos(42.65°)  
= 0.7392 (D.3-b)

The d- and q-axis components of the stator current at Koeberg, expressed on a 1072 MVA base, are (Appendix F, equation F.16):

$$\begin{split} I_{d} &= \frac{-PV_{d} - QV_{q}}{-V_{d}^{2} - V_{q}^{2}} \\ &= \frac{-\left(\frac{450}{1072}\right) * 0.6809 - \left(\frac{13.6}{1072}\right) * 0.7392}{-(0.6809)^{2} - (0.7392)^{2}} \\ &= 0.2923 \text{ per unit; } S_{BASE} = 1072 \text{ MVA} \end{split}$$
(D.4-a)  
$$I_{q} &= \frac{QV_{d} - PV_{q}}{-V_{d}^{2} - V_{q}^{2}} \\ &= \frac{\left(\frac{13.6}{1072}\right) * 0.6809 - \left(\frac{450}{1072}\right) * 0.7392}{-(0.6809)^{2} - (0.7392)^{2}} \\ &= 0.2987 \text{ per unit; } S_{BASE} = 1072 \text{ MVA} \end{split}$$
(D.4-b)

The d- and q-axis transient reactances of the Koeberg machine, expressed on a 1072 MVA base are  $x'_{d} = 0.395$  per unit and  $x'_{q} = 0.689$  per unit. Hence, the transient voltage of the Koeberg generator is (Appendix F, equation F.1):

$$E'_{KBG} = (V_d - x'_q I_q) + j (V_q + x'_d I_d)$$
  
=  $E'_d + j E'_q$   
=  $(0.6809 - 0.689 * 0.2987) + j (0.7392 + 0.395 * 0.2923)$   
=  $0.4751 + j 0.8547$   
=  $0.9778 \angle (90^0 - 60.93^\circ)$   
=  $0.9778 \angle 29.07^\circ$  (D.5)

## D.2 $|E'_{KBG}|$ WHEN MAGNETIC SALIENCY IS NOT CONSIDERED

For the case where the generator is modelled using the constant voltage behind transient reactance model  $E'_{KBG}$  can be computed using [1, 187]:

$$\boldsymbol{E}_{\boldsymbol{K}\boldsymbol{B}\boldsymbol{G}}^{'} = \boldsymbol{V} + (\boldsymbol{R}_{a} + \boldsymbol{j} \boldsymbol{x}_{i}^{'}) \boldsymbol{I}$$
(D.6)

 $R_a$  is very small and is usually neglected.

The constant voltage behind transient reactance generator model does not consider magnetic saliency.

When magnetic saliency is not modelled armature reaction,  $x_i$ , should be computed using [41, p84]:

$$x'_{i} = \left(\frac{x'_{d} + x'_{q}}{2}\right) \tag{D.7-a}$$

For the Koeberg generator  $x_i$ , expressed on a 1072 MVA base, is:

$$= \left(\frac{0.395 + 0.689}{2}\right)$$
$$= 0.542$$
(D.7-b)

Hence,  $E'_{KBG}$  is:

$$E'_{KBG} = V + j x'_{i} \frac{S}{V}$$
  
= 1.005 + j 0.542  $\frac{\sqrt{\left(\frac{450}{1072}\right)^{2} + \left(\frac{13.6}{1072}\right)^{2}}}{1.005}$   
= 1.005 + j 0.2265  
 $|E'_{KBG}| = 1.03 \text{ p.u.}$  (D.8)